

*Part II - Applications of MultiSeq
Evolution of Translation: Dynamics of
Recognition in RNA:Protein Complexes*

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Biology

Workshop 2012 – UIUC Beckman

NIH Center Macromolecular Modeling and
Bioinformatics

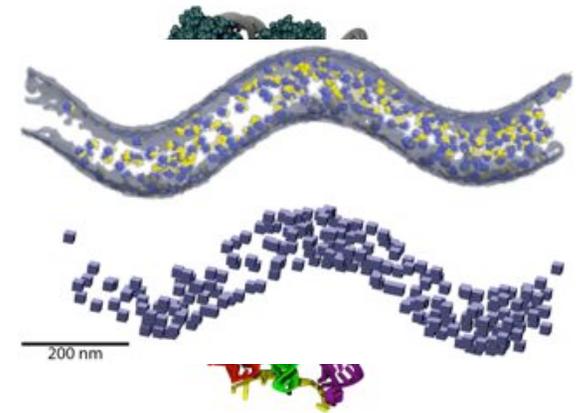
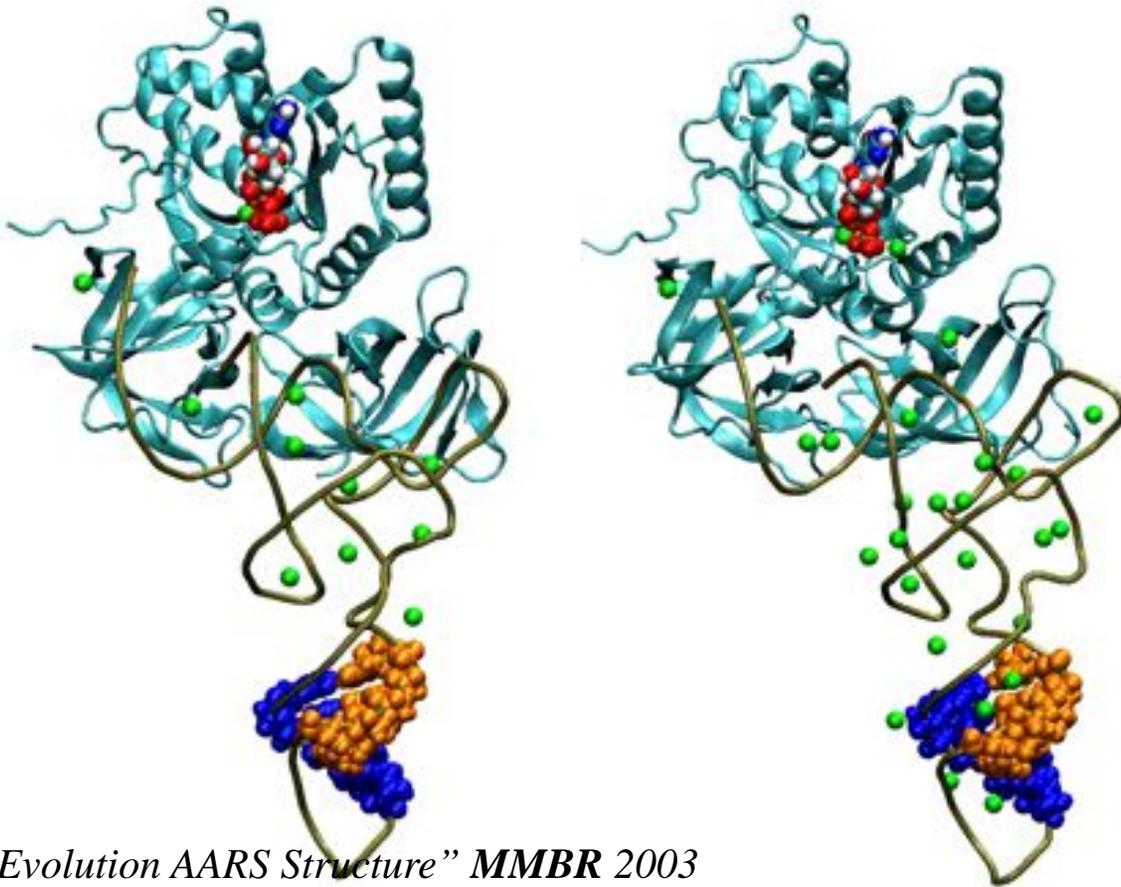


ILLINOIS

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

Protein:RNA Complexes in Translation

Evolution, Dynamics, Analysis



**Proteins/RNA
Polyribosomes
Ribosome**

“Evolution AARS Structure” *MMBR* 2003

“Evol. Profiles Class I&II AARS” *JMB* 2005

“Evolution SepRS/CysRS” *PNAS* 2005

“Dynamic Signaling Network” *PNAS* 2009

“Exit Strategy Charged tRNA” *JMB* 2010

“Mistranslation in *Mycoplasma*” *PNAS* 2011

“Dynamical Recognition Novel

Amino Acids” *JMB* 2008

“tRNA Dynamics” *FEBS* 2010

“Signatures ribosomal evolution”

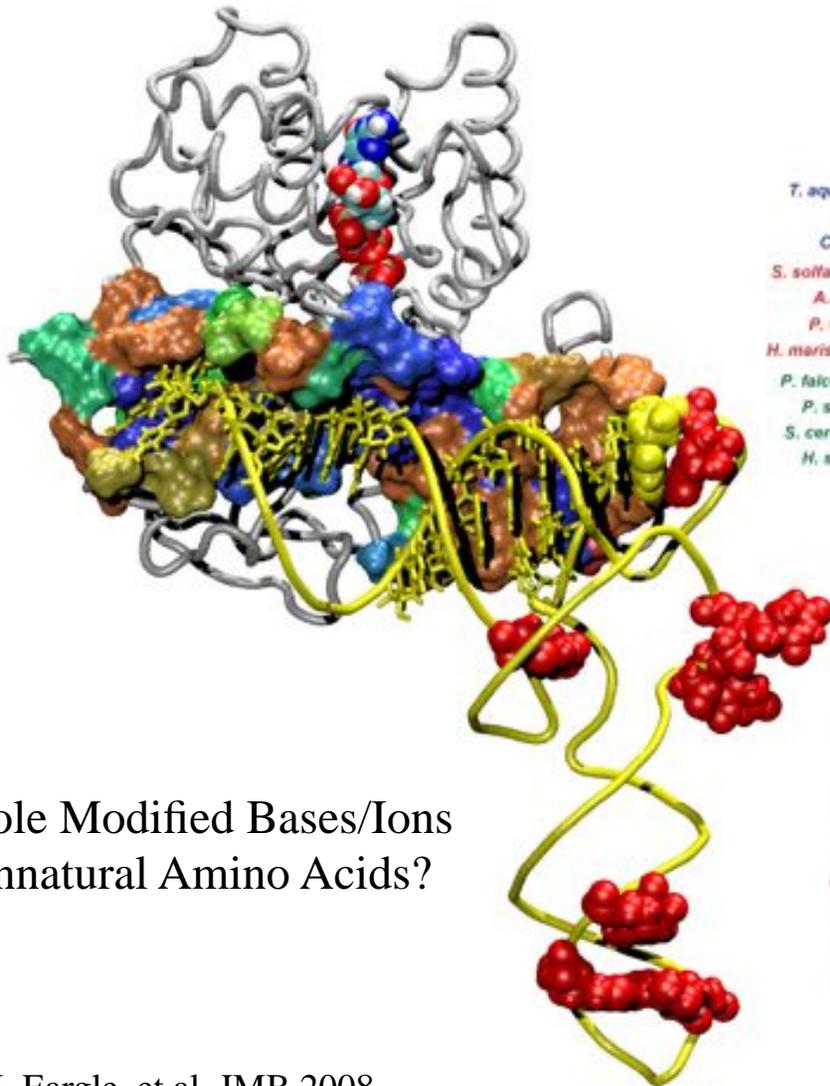
PNAS 2008, *BMC* 2009, *BJ* 2010

“Motion L1 Stalk:tRNA” *JMB* 2010

“Whole cell simulations on GPUs”

IEEE 2009, *Plos CB* 2011, *PRL* 2011

Evolution of Protein/RNA Interfaces: Dynamics of EF-Tu/tRNA Recognition



	Switch I					Switch II					Domain II																							
	50	+	+	*	57	85	*	●	*	●	92	224	*											240										
<i>T. aquaticus</i>	I	D	K	A	P	E	E	R	H	A	D	V	I	K	N	M	P	V	E	D	V	F	T	I	T	G	R	G	T	V	A	T	G	B
<i>E. coli</i>	I	D	N	A	P	E	E	K	H	A	D	V	V	K	N	M	P	I	E	D	V	F	S	I	S	G	R	G	T	V	V	T	G	A
<i>C. jejuni</i>	I	D	N	A	P	E	E	K	H	A	D	V	V	K	N	M	P	I	E	D	V	F	S	I	S	G	R	G	T	V	V	T	G	E
<i>S. solfataricus</i>	L	D	R	L	K	E	E	R	H	R	D	F	V	K	N	M	P	I	G	D	V	V	S	I	S	G	V	G	T	V	P	V	G	
<i>A. pernix</i>	L	D	K	M	K	E	E	R	H	R	D	F	V	K	N	M	P	V	Q	N	V	V	S	I	P	G	A	G	T	V	P	V	G	
<i>P. woesei</i>	M	D	R	L	R	E	E	R	H	R	D	F	V	K	N	M	P	I	G	D	V	V	S	I	K	G	V	G	T	V	P	V	G	
<i>H. marismortui</i>	M	D	N	L	A	E	E	R	H	R	D	F	V	K	N	M	P	I	G	D	V	V	T	I	S	G	I	G	T	V	P	V	G	
<i>P. falciparum</i>	L	D	K	L	K	A	E	R	H	K	D	F	I	K	N	M	P	L	G	D	V	V	K	I	G	G	I	G	T	V	P	V	G	
<i>P. sativum</i>	L	D	K	L	K	A	E	R	H	R	D	F	I	K	N	M	P	L	G	D	V	V	K	I	G	G	I	G	T	V	P	V	G	
<i>S. cerevisiae</i>	L	D	K	L	K	A	E	R	H	R	D	F	I	K	N	M	P	L	Q	D	V	V	K	I	G	G	I	G	T	V	P	V	G	
<i>H. sapiens</i>	L	D	K	L	K	A	E	R	H	R	D	F	I	K	N	M	P	L	Q	D	V	V	K	I	G	G	I	G	T	V	P	V	G	

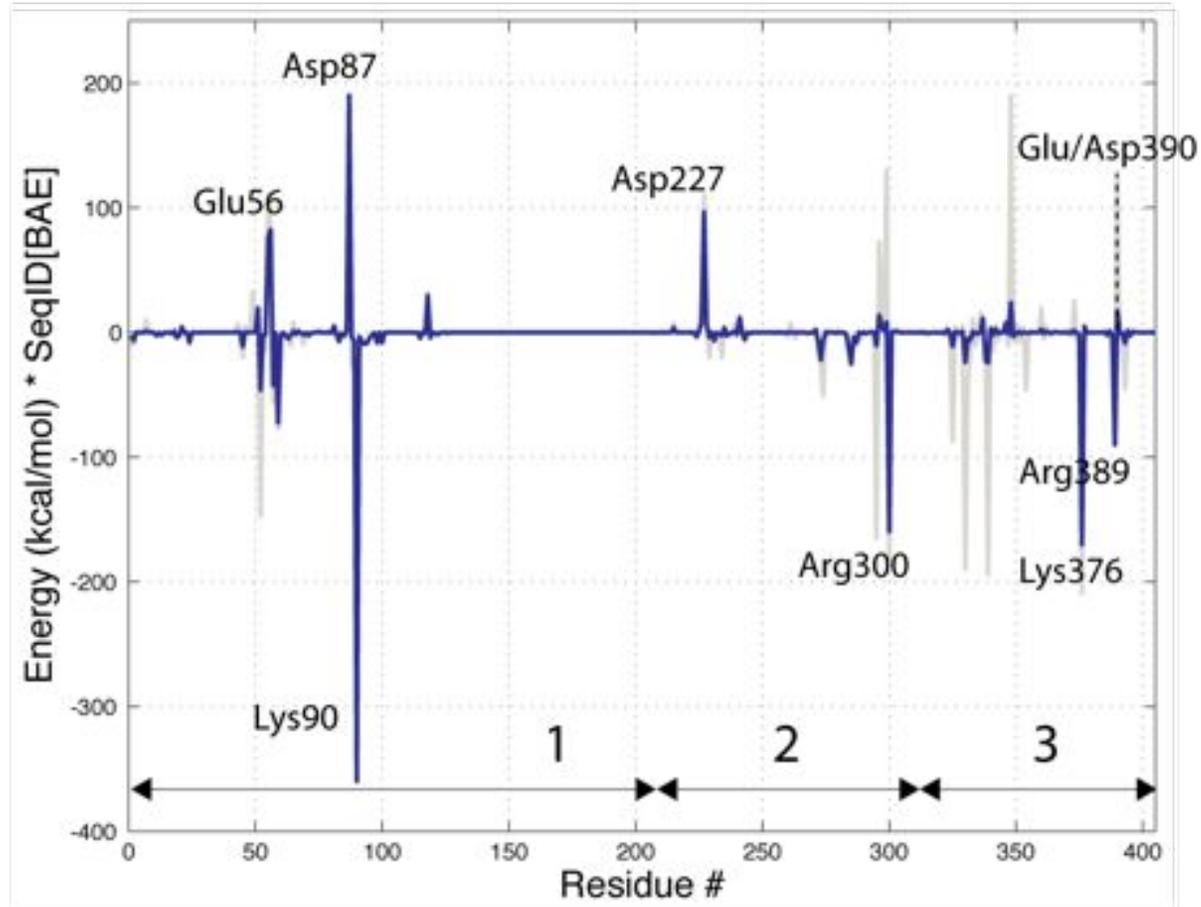
	Domain II																																
	271																			●	+	+	*	302									
<i>T. aquaticus</i>	E	N	H	R	K	T	L	G	E	G	I	A	G	D	N	V	G	L	L	R	G	V	S	R	E	E	V	E	R	G	G	B	
<i>E. coli</i>	E	N	F	R	K	L	L	D	E	G	R	A	G	E	N	V	G	V	L	L	R	G	I	K	R	E	E	I	E	R	G	D	A
<i>C. jejuni</i>	E	N	F	R	K	E	M	D	Q	G	E	A	G	D	N	V	G	V	L	L	R	G	T	K	K	E	E	V	I	R	O	M	E
<i>S. solfataricus</i>	E	T	H	H	T	K	M	D	K	A	E	P	G	D	N	I	G	F	N	V	R	G	V	E	K	K	D	I	K	R	G	D	
<i>A. pernix</i>	E	N	H	Y	Q	Q	L	Q	A	E	P	G	D	N	I	G	F	A	V	R	G	V	S	K	S	D	I	K	R	G	D		
<i>P. woesei</i>	E	N	H	H	E	P	L	E	E	A	L	P	G	D	N	I	G	F	N	V	R	G	V	S	K	H	D	I	K	R	G	D	
<i>H. marismortui</i>	E	N	H	H	E	E	V	P	K	A	E	P	G	D	N	V	G	F	N	V	R	G	V	G	K	D	D	I	K	R	G	D	
<i>P. falciparum</i>	E	N	H	X	E	V	L	E	E	A	R	P	G	D	N	I	G	F	N	V	K	N	V	S	V	K	E	I	K	R	G	V	
<i>P. sativum</i>	E	N	H	H	E	A	L	T	E	A	L	P	G	D	N	V	R	F	N	V	K	N	V	A	V	K	D	L	K	H	C	L	
<i>S. cerevisiae</i>	E	N	H	H	E	Q	L	E	Q	D	V	P	G	D	N	V	G	F	N	V	K	N	V	S	V	K	E	I	R	R	G	N	
<i>H. sapiens</i>	E	N	H	H	E	A	L	S	E	A	L	P	G	D	N	V	G	F	N	V	K	N	V	S	V	K	D	V	R	R	G	N	

Role Modified Bases/Ions
Unnatural Amino Acids?

Dynamical Recognition EF-Tu/tRNA (E.coli)

Combining MD with Evolutionary Analysis (MultiSeq)

Non-bonded Interaction Energy

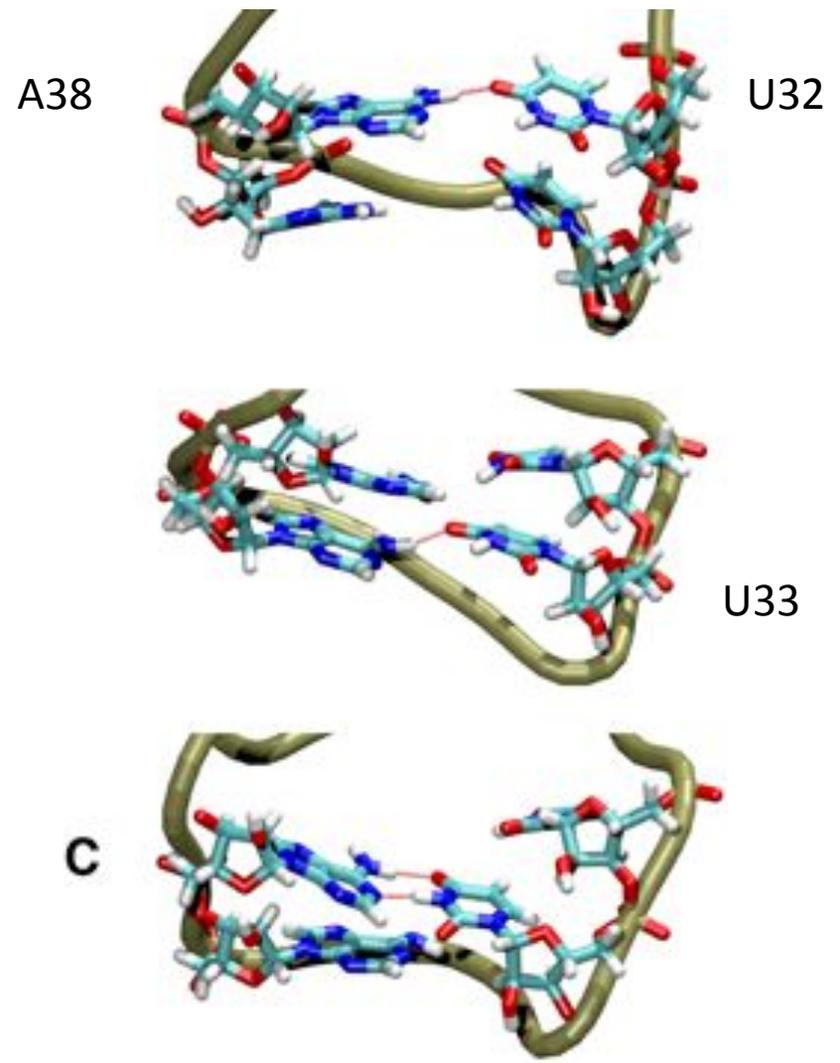
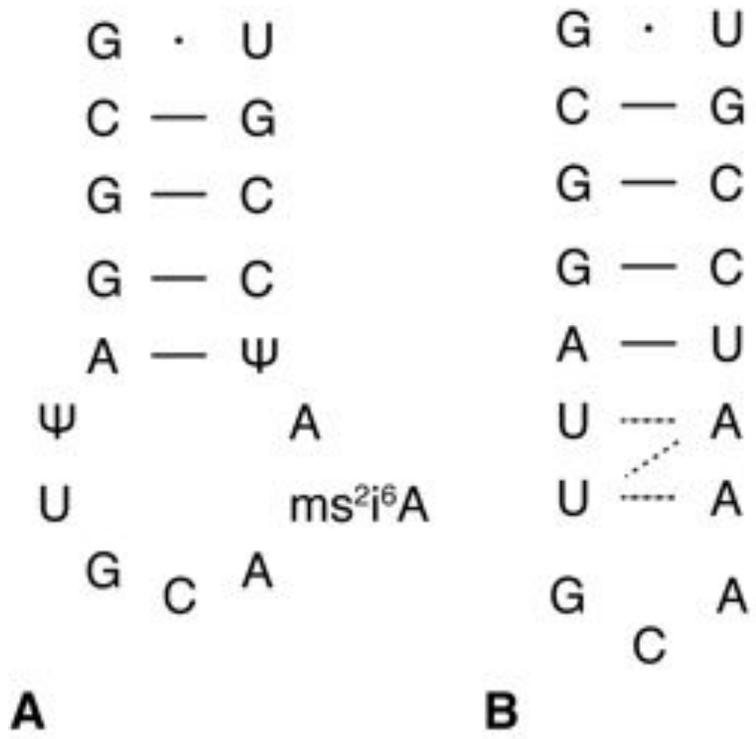


BAE

*J. Eargle, A. Sethi, A. Black, L. Trabuco & Z. Luthey-Schulten. JMB
"Dynamics of Recognition in EF-Tu/tRNA Complex" (2008)*

Effects of Modified Bases on Dynamics of AC Stem/Loop

MD simulations of unmodified tRNA:Cys



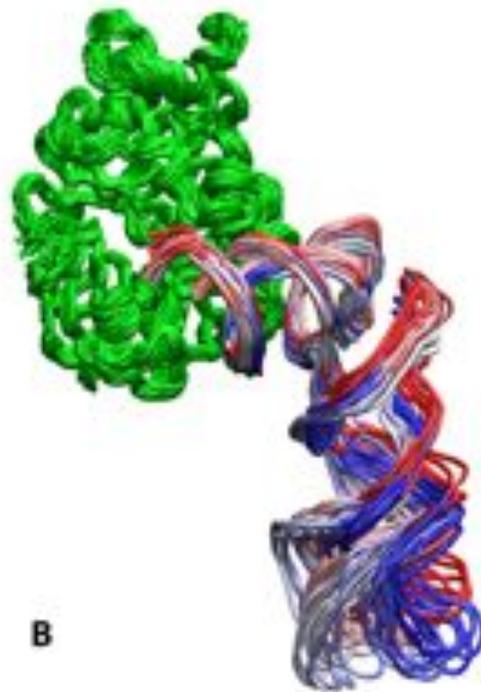
Similar NMR structures for unmodified tRNA-Phe
 Nikonowicz, *JMB* 2002, *personal communication*

Eargle, et al. *JMB* (2008))

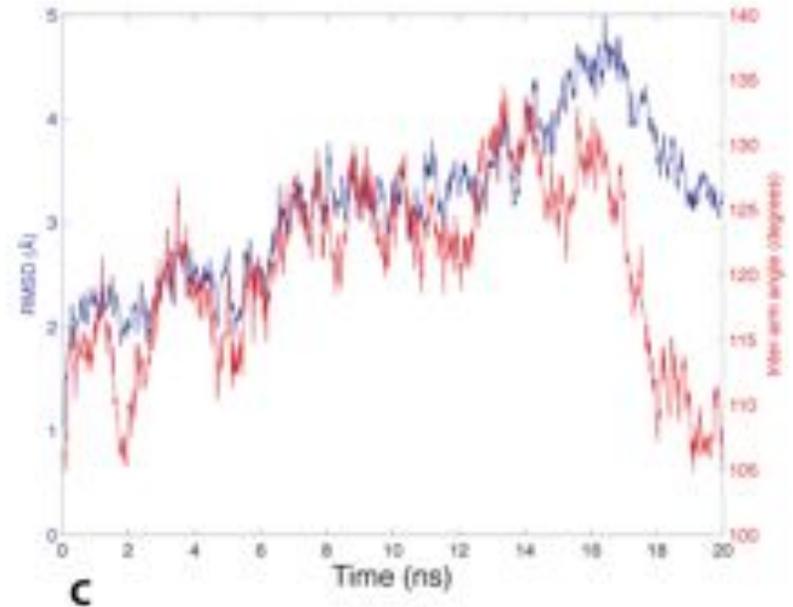
Flexibility in tRNA structures observed in crystallography and simulations



X-ray 5 tRNAs



MD EF-Tu:tRNA:cys

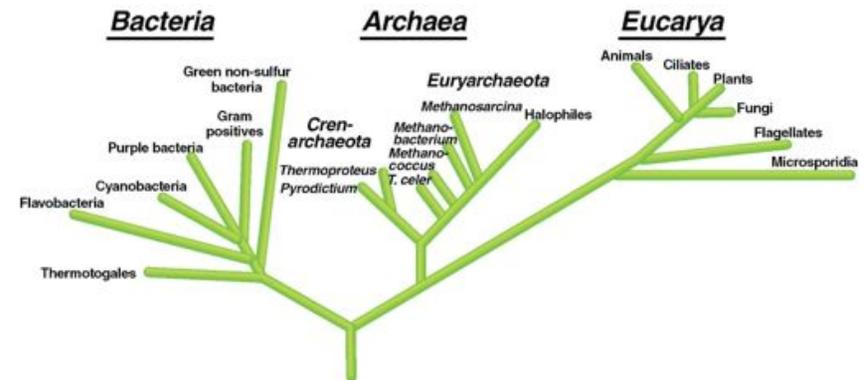
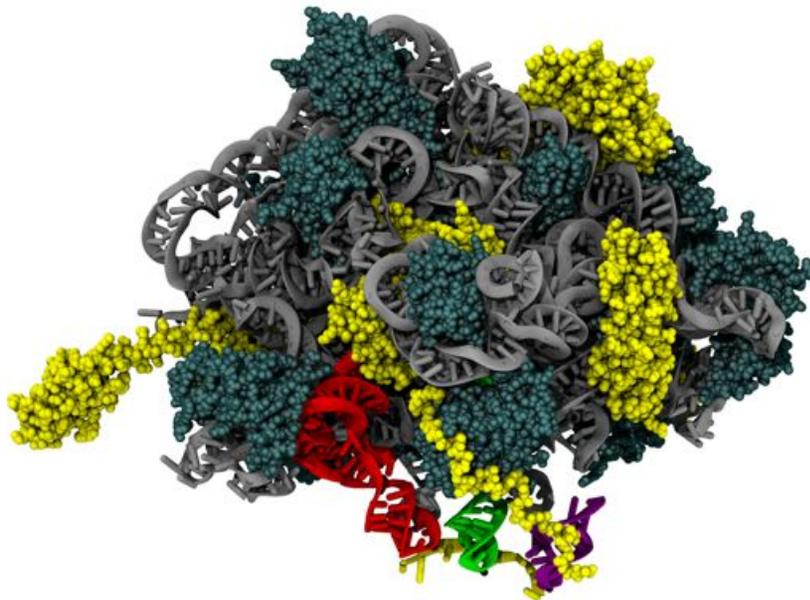


MD: RMSD and Interarm Angle in tRNA:cys

Molecular Signatures in Ribosome Evolution

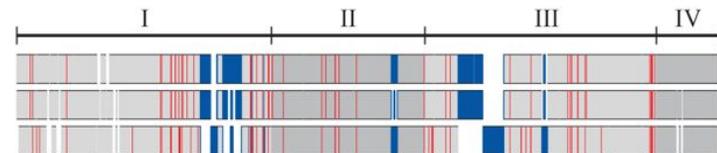
Archaeal - LSU

Universal Phylogenetic Tree



16S rRNA

E. coli
T. thermophilus
H. marismortui



Dynamical function of ribosomal signatures: idiosyncrasies in ribosomal RNA and/or proteins characteristic of the domains of life

Roberts, Sethi, Montoya, Woese, Luthey-Schulten (2008) *PNAS* 105:13953

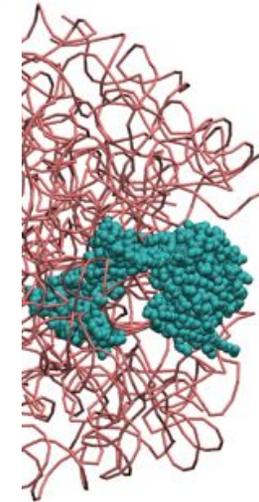
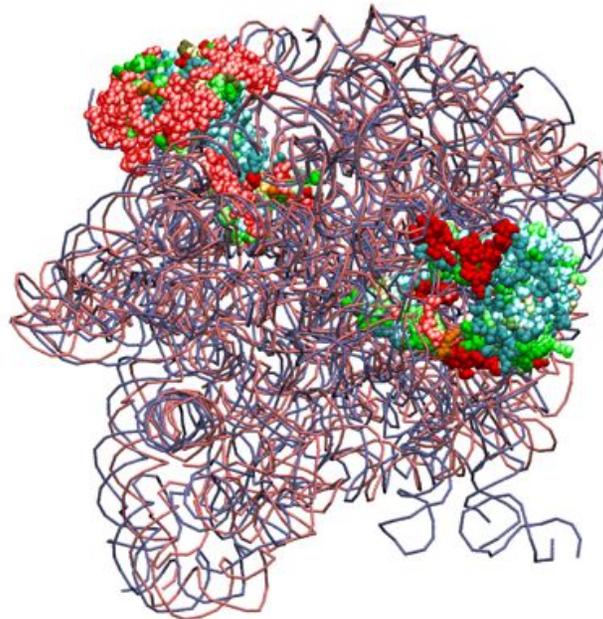
Chen, Eargle, Sarkar, Gruebele, Luthey-Schulten (2010) *Biophysical Journal*

Structural Overlaps with STAMP

Comparing ribosomal large subunit with r-proteins L2 and L3
 180,000 atoms in 4 rRNAs and 58 proteins



E. coli



arismortui

Sequence Name	50	60	70	80	90																																					
23S rRNA																																										
<input type="checkbox"/> 2aw4_B	A	U	G	A	A	B	A	C	B	U	B	C	U	A	A	B	B	U	C	B	B	U	A	A	B	B	U	G	A													
<input type="checkbox"/> 1s72_0	C	A	A	G	C	U	B	C	G	A	A	A	G	C	C	A	U	G	G	G	A	G	C	C	G	C	A	C	G	G	A	A	G	A								
5S rRNA																																										
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Ribosomal Protein L2																																										
<input type="checkbox"/> 2aw4_C	-	-	-	G	R	N	H	N	G	R	I	T	I	R	H	I	G	D	G	H	K	G	A	Y	R	I	V	D	F	K	R	N	K	D	-	-	G	I	P	A		
<input type="checkbox"/> 1s72_A	R	G	T	S	T	F	-	-	-	-	-	-	-	-	-	R	A	-	-	P	S	H	R	Y	K	A	D	L	E	H	R	K	V	E	D	G	D	V	I	A	G	
Ribosomal Protein L3																																										
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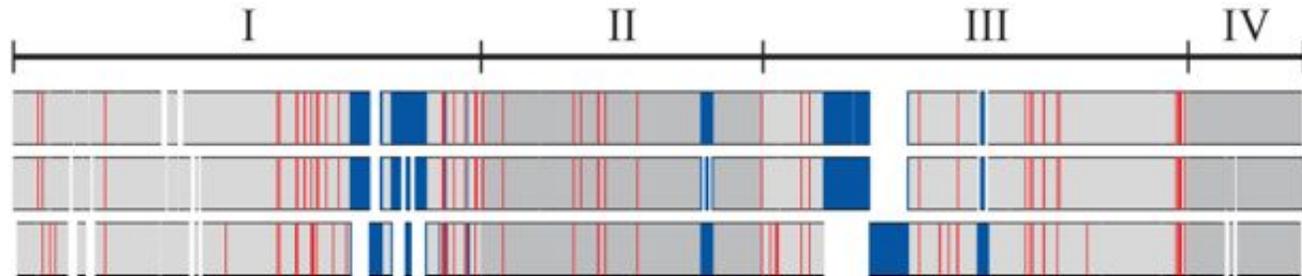
Sequence and Structure Signatures in Ribosomal RNA

16S rRNA

E. coli

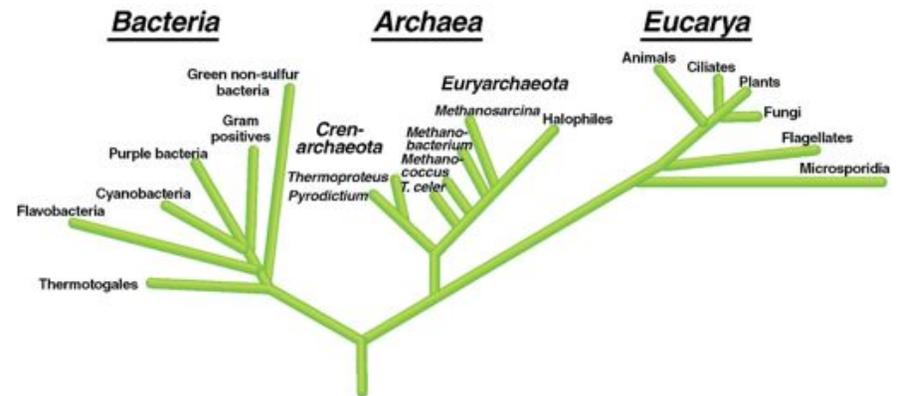
T. thermophilus

H. marismortui



Ribosomal Signatures: Idiosyncrasies in rRNA and/or rproteins characteristic of the domains of life

69 (119) & 6 (14) in 16S (23S)

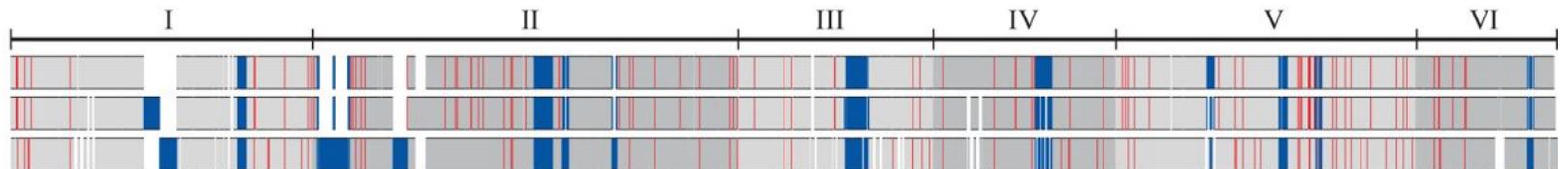


23S rRNA

E. coli

T. thermophilus

H. marismortui



Signature analysis

- Signatures are sequence and/or structural features that are characteristic of a domain of life*.
- Identify the sequence signatures in the 16S rRNA and proteins using MultiSeq
- MultiSeq has a coloring based on signatures, but use Scripts to collect quantitative data about the signatures: position, composition.
- Signature analysis can be applied to any set of sequences/groupings

* E. Roberts, A. Sethi, J. Montoya, C. Woese, Z Luthy-Schulten (2008) *PNAS*

Signature analysis script

```
proc get_taxa_signatures {args} {

    initializeMultiSeqEnvironment

    # Load the alignment.
    set sequenceIDs [::SeqData::Fasta::loadSequences $alignmentFilename]

    # Find the reference species.
    set refSequenceIDs {}
    foreach species $referenceSpecies {
        set found 0
        foreach sequenceID $sequenceIDs {
            if {[string toupper [::SeqData::getScientificName $sequenceID]] == [string toupper $species]} {
                lappend refSequenceIDs $sequenceID
                set found 1
                break
            }
        }
    }

    # Group the sequence ids.
    array set groupData {names {}}
    foreach sequenceID $sequenceIDs {

        set group ""
        if {$rankName == "domain"} {
            set group [::SeqData::getDomainOfLife $sequenceID]
        } else {
            set group [::SeqData::getLineageRank $sequenceID $rankName]
        }
        if {![info exists groupData($group)]} {
            lappend groupData(names) $group
            set groupData($group) {}
        }
        lappend groupData($group) $sequenceID
    }
}
```

Signature analysis script (cont)

```
# Calculate the signatures for the groups.
set signatures [::SeqEdit::Metric::Signatures::calculateSignatures $sequenceGroups $groupConsensusCutoff \
               $otherGroupMaxCutoff $otherGroupMaxGapFraction $maxConservedBlockDistance $minConservedBlockSize]

# Print the signatures.
puts ""
puts "Ordered Signatures"
printSignatureHeader $groups $refSequenceIDs
for {set position 0} {$position < [llength [lindex $signatures 0]]} {incr position} {

    # Get the signature for each of the groups.
    set isSignature 0
    for {set groupIndex 0} {$groupIndex < [llength $groups]} {incr groupIndex} {
        set groupSignature [lindex [lindex $signatures $groupIndex] $position]
        if {[string length $groupSignature] == 1} {
            set isSignature 1
        }
    }

    if {$isSignature} {
        printSignatureLine $position $groups $refSequenceIDs $signatures $sequenceGroups
    }
}
}
```

Signature analysis script (cont)

```
proc getCompositionString {sequenceIDs position} {  
  # Go through each group to count the elements.  
  array set counts {values {}}  
  foreach sequenceID $sequenceIDs {  
    set element [::SeqData::getElement $sequenceID $position]  
    if {![info exists counts($element)]} {  
      lappend counts(values) $element  
      set counts($element) 1  
    } else {  
      incr counts($element)  
    }  
  }  
  
  set ret ""  
  foreach element $counts(values) {  
    set percentage [expr round(100.0*double($counts($element))/double([llength $sequenceIDs]))]  
    if {$percentage > 5} {  
      if {$ret != ""} {  
        append ret "/"  
      }  
      append ret "${element}($percentage\%)"  
    }  
  }  
  
  return $ret  
}
```

Signature script output

Ordered Signatures

Pos	E._coli	T._therm	H._maris	Archaea	Bacteria
35	33	33	27	U(28%)/C(72%)	*A(96%)
42	39	39	33	*U(100%)	*G(95%)
51	47	47	42	*G(97%)	C(85%)/U(7%)/G(8%)
59	53	53	49	*C(100%)	A(83%)/G(14%)
222	113	106	87	*C(100%)	*G(95%)
661	248	243	227	*G(97%)	C(75%)/G(9%)/U(11%)
749	314	309	293	*G(100%)	*C(97%)
753	317	312	296	*G(97%)	*U(91%)/G(7%)
777	338	333	317	*G(97%)	A(89%)/N(9%)
779	339	334	318	*G(97%)	*C(98%)
780	340	335	319	*C(94%)	*U(92%)/A(6%)
790	349	344	328	G(86%)/N(11%)	*A(92%)
791	350	345	329	C(67%)/U(19%)/N(11%)	*G(98%)
800	358	353	337	*G(100%)	*U(91%)/C(7%)
802	359	354	338	*C(97%)	G(59%)/U(9%)/C(9%)/A(20%)
804	361	356	340	*C(94%)	G(84%)/A(14%)
809	365	360	344	*A(92%)/U(8%)	*U(97%)
811	367	362	346	C(83%)/G(14%)	*U(97%)
823	377	372	356	C(89%)/U(11%)	*G(92%)
833	386	381	365	*G(94%)	C(89%)/U(6%)
840	393	388	372	G(83%)/C(14%)	*A(97%)
851	403	398	382	*A(100%)	C(89%)
920	447	441	416	C(31%)/U(67%)	*G(92%)
990	487	471	424	G(89%)/A(8%)	*A(91%)
1083	508	491	446	*A(97%)	*U(92%)
1085	510	493	448	*G(97%)	*A(97%)
1087	512	495	450	*C(92%)/U(8%)	*U(97%)
1089	514	497	452	*G(92%)/N(6%)	C(89%)/U(8%)
1101	523	506	461	*C(94%)/A(6%)	*A(96%)
1119	537	520	475	*C(100%)	*G(91%)/A(8%)
1121	539	522	477	*G(92%)/A(6%)	A(89%)/G(10%)
1134	549	532	487	*U(94%)	*C(99%)

Draw signature figure

- Want to create a graphical representation of the signatures.
- Can use the TCL graphics object to draw figures.

```
proc draw_one_d_alignment {args} {  
  
    # Load the alignment.  
    set alignment [::SeqData::Fasta::loadSequences $alignmentFilename]  
    set numberSequences [llength $alignment]  
    set numberPositions [::SeqData::getSeqLength [lindex $alignment 0]]  
    puts "Loaded $numberSequences sequences of length $numberPositions"  
  
    # Create the drawing canvas.  
    set canvasWidth [expr $draw(xBorder)+($numberPositions*$draw(positionWidth))+$draw(xBorder)]  
    set canvasHeight [expr $draw(yBorder)+($numberSequences*$draw(sequenceHeight))+(($numberSequences-1)*\  
                                                                    $draw(sequenceSpacing))+$draw(yBorder)]  
  
    set g [canvas .drawing -width $canvasWidth -height $canvasHeight]  
  
    # Draw the alignment.  
    for {set i 0} {$i < $numberSequences} {incr i} {  
        set sequenceID [lindex $alignment $i]  
        set y1 [expr $draw(yBorder)+($i*($draw(sequenceHeight)+$draw(sequenceSpacing)))]  
        set y2 [expr $y1+$draw(sequenceHeight)]  
        drawSequencePositions $g $draw(xBorder) $y1 $y2 $sequenceID 0 [expr $numberPositions-1] \  
                               $draw(positionWidth) $draw(sequenceColor) $draw(borderColor) $draw(borderWidth)  
    }  
  
    # Save the canvas.  
    $g postscript -x 0 -y 0 -width $canvasWidth -height $canvasHeight -file $outputFilename  
  
    cleanupMultiSeqEnvironment  
}
```

Draw signature figure (cont)

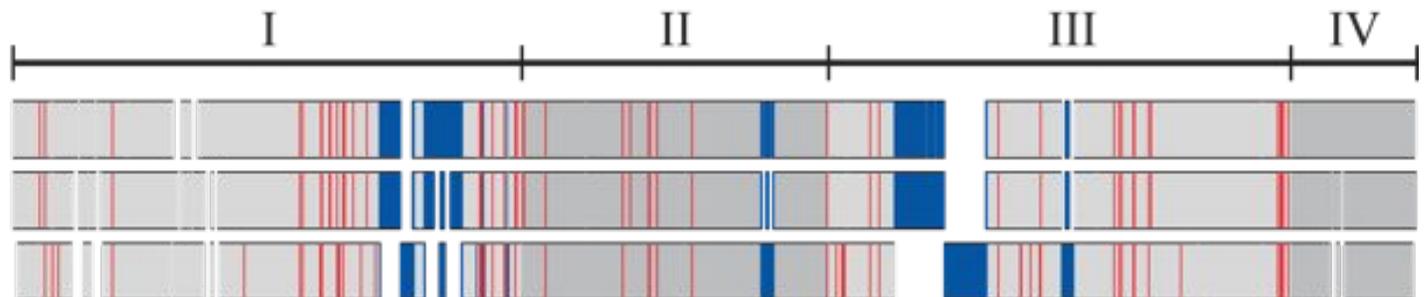
```
proc drawSequencePositions {g x y1 y2 sequenceID firstPosition lastPosition positionWidth sequenceColor borderColor  
                                                                    borderWidth}  
{  
  set startPosition ""  
  for {set j $firstPosition} {$j <= $lastPosition} {incr j} {  
    set element [::SeqData::getElement $sequenceID $j]  
  
    # If this is the beginning of a sequence block, record that one started.  
    if {$element != "-" && $startPosition == ""} {  
      set startPosition $j  
    }  
  
    # If this is the end of a sequence block, draw the block.  
    if {($element == "-" || $j == $lastPosition) && $startPosition != ""} {  
      if {$element == "-"} {  
        set endPosition [expr $j-1]  
      } else {  
        set endPosition [expr $j]  
      }  
      set x1 [expr $x+($startPosition*$positionWidth)]  
      set x2 [expr $x+((($endPosition+1)*$positionWidth)]  
      $g create rectangle $x1 $y1 $x2 $y2 -fill $sequenceColor -outline $sequenceColor -width $borderWidth  
      $g create line $x1 $y1 $x2 $y1 -fill $borderColor -width $borderWidth  
      $g create line $x1 $y2 $x2 $y2 -fill $borderColor -width $borderWidth  
      set startPosition ""  
    }  
  }  
}
```

16S rRNA

E. coli

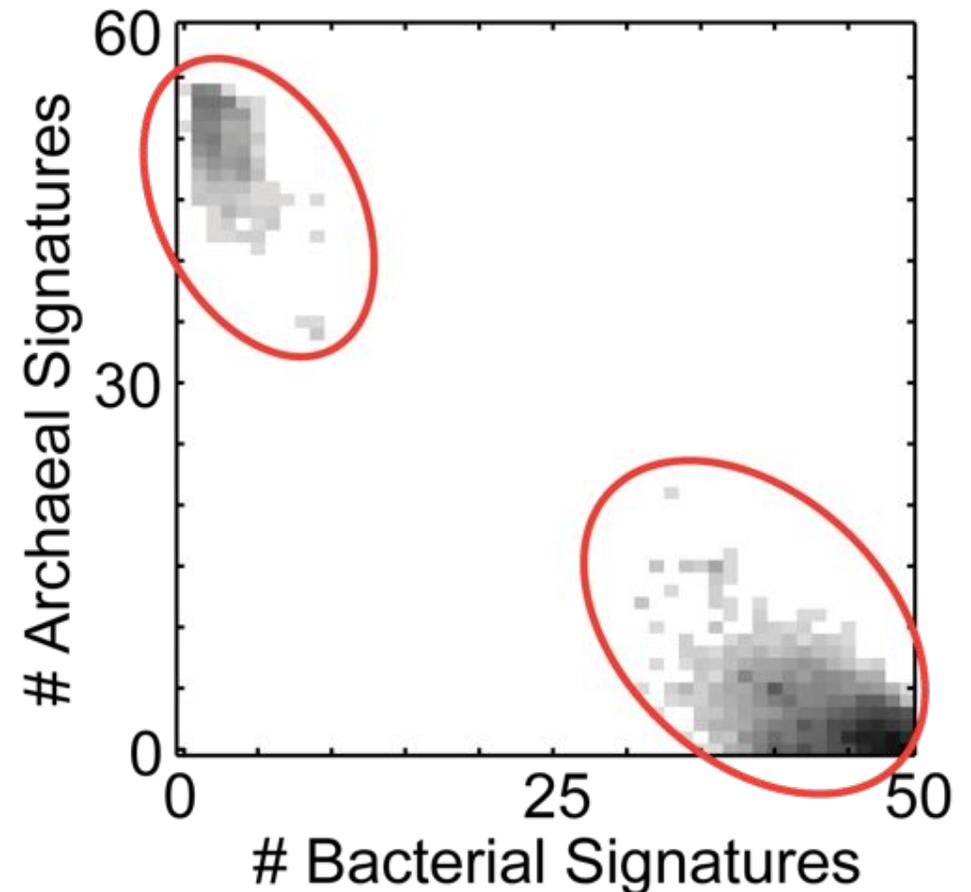
T. thermophilus

H. marismortui

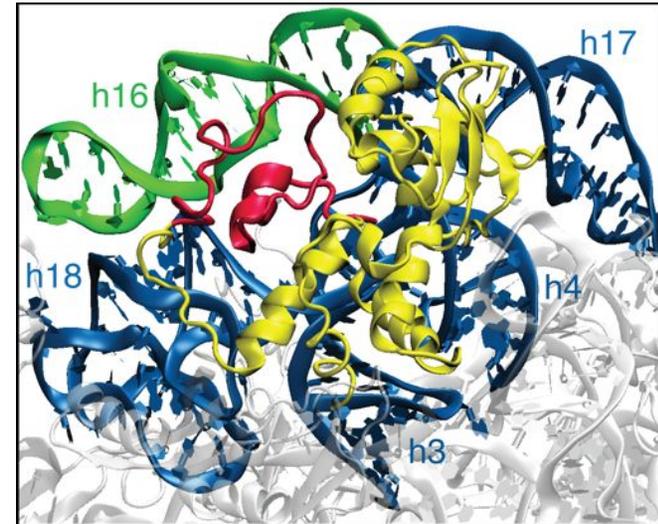
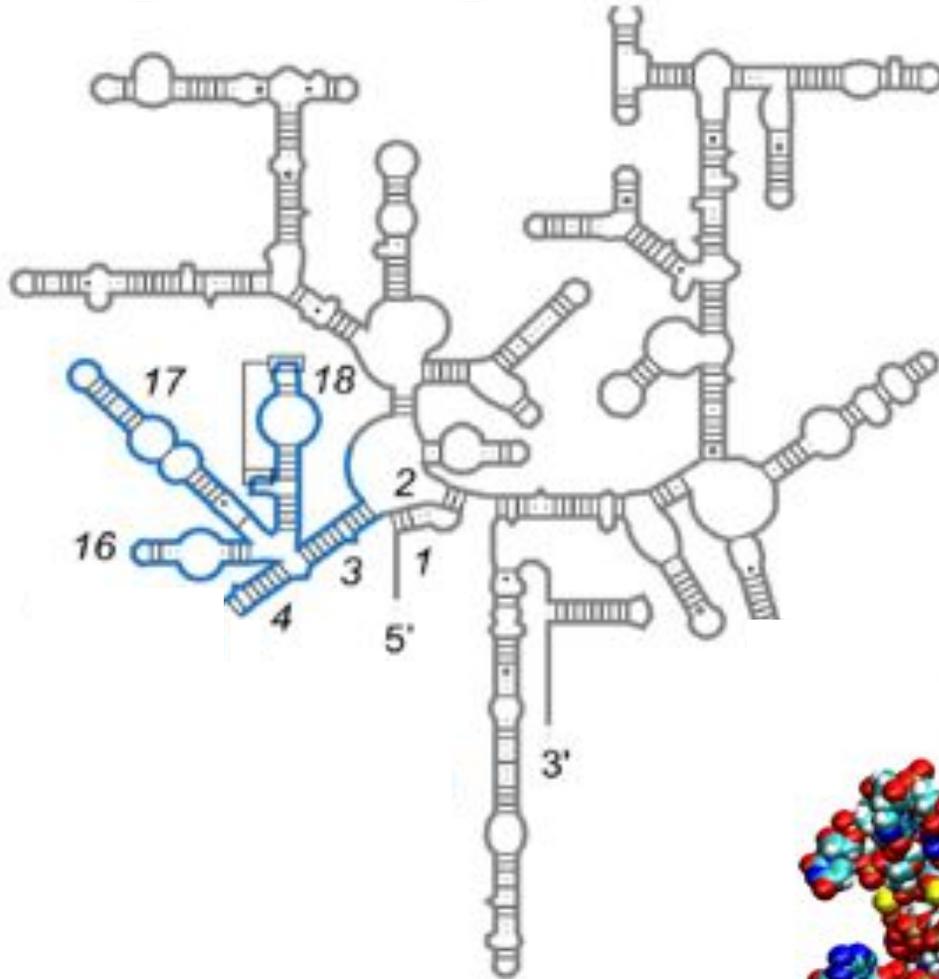


90,000 Environmental 16S rRNA Distinct A & B Sequence Signatures

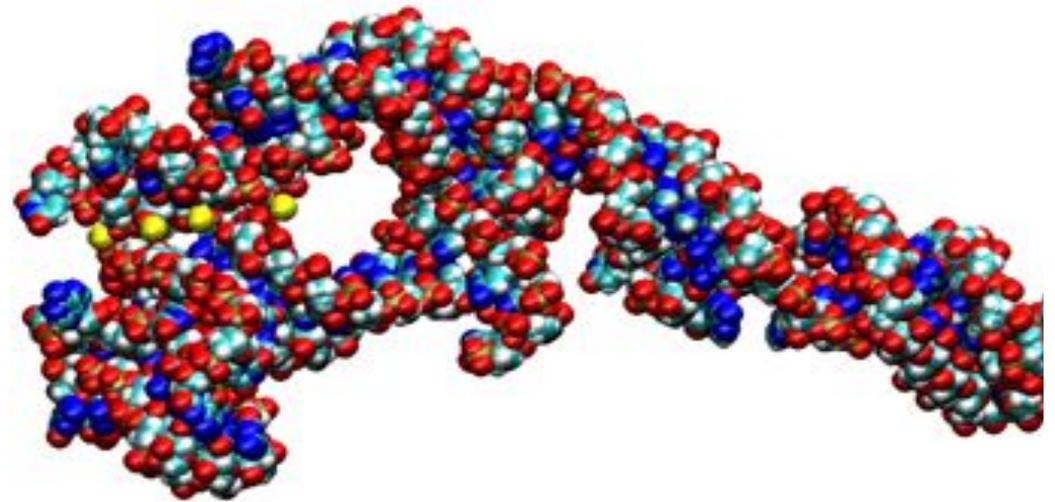
- Analysis of the ribosomal signatures in 90,000 new environmental samples shows that no “gray” area exists: a ribosome is either bacterial or archaeal in nature.
- Split across cluster: 10,000 sequence on each node



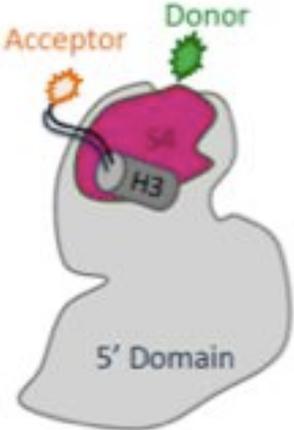
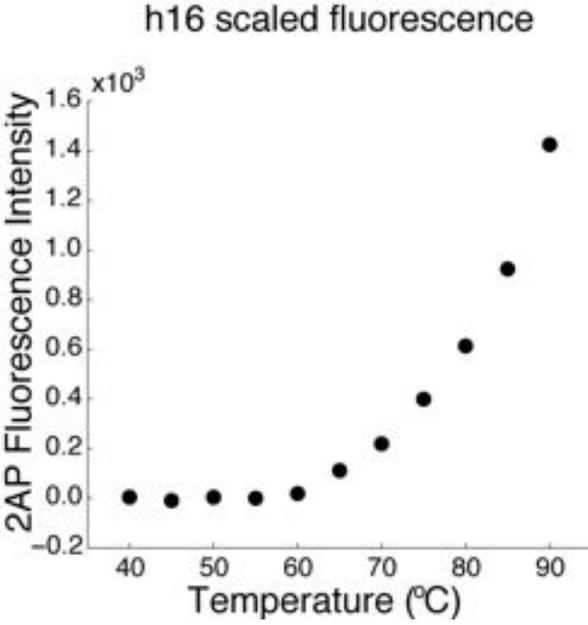
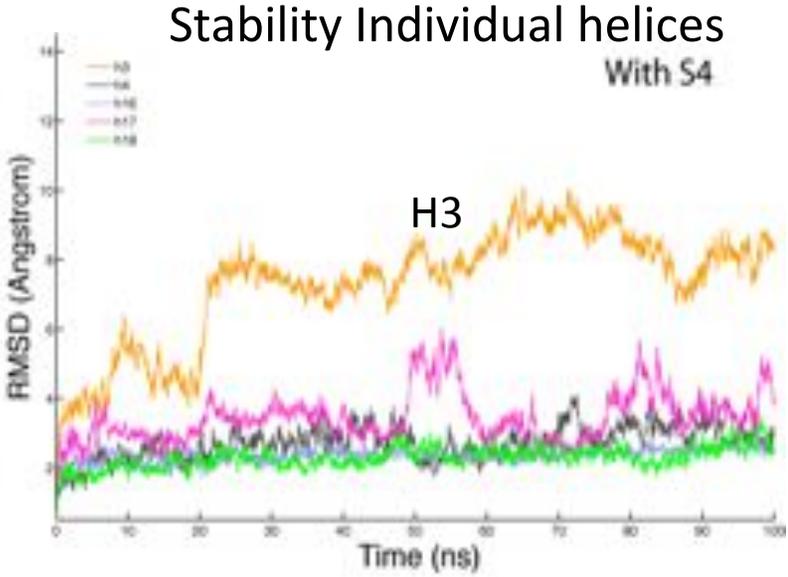
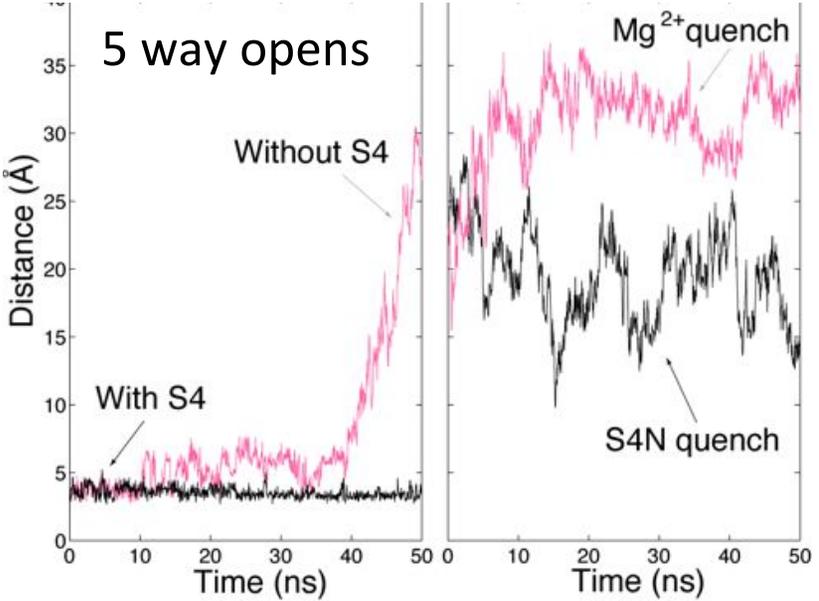
Largest signature region in the SSU



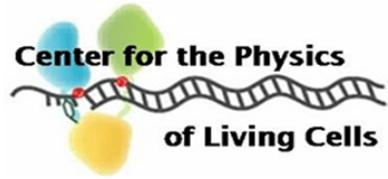
5-way helical junction rRNA with S4



Stability of 5-way junction helices with/without S4

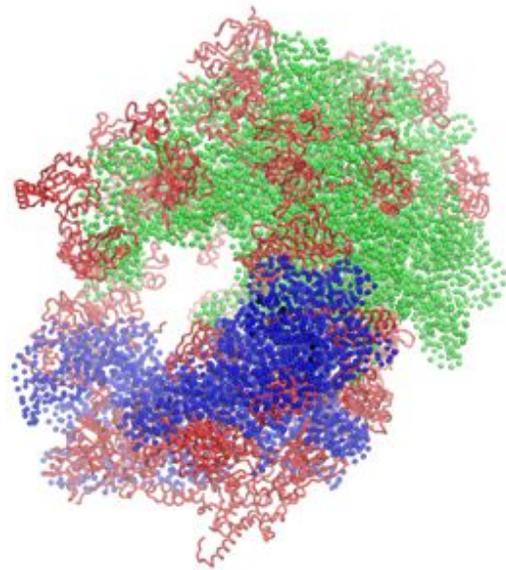


Model for Assembly ?

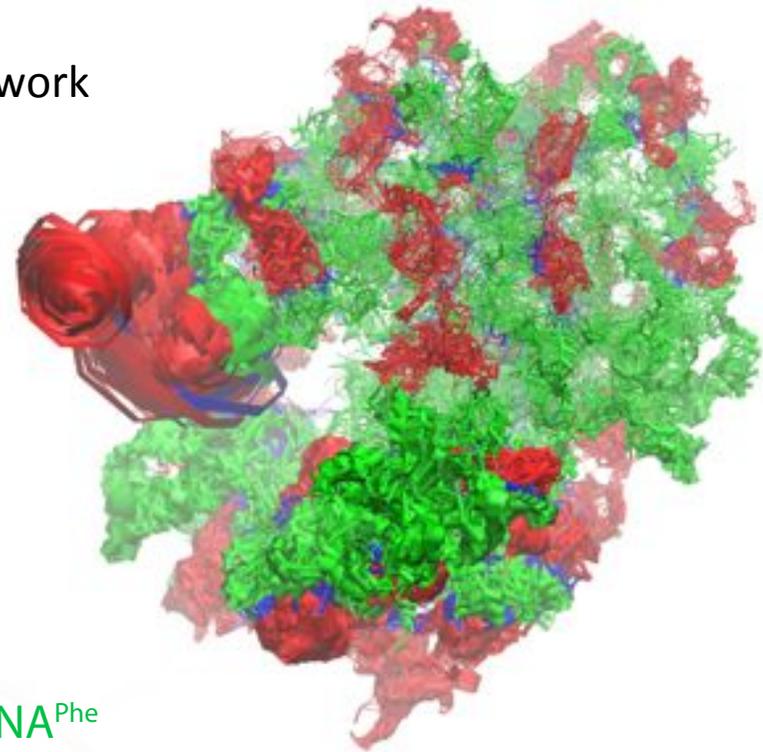


Collaboration with Gruebele, Ha, Woodson labs

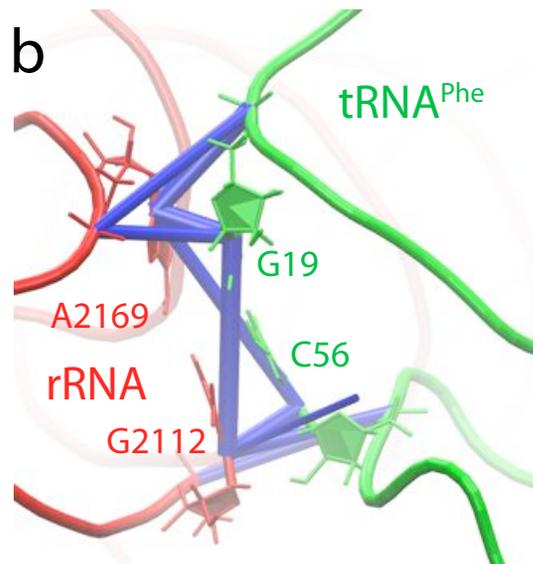
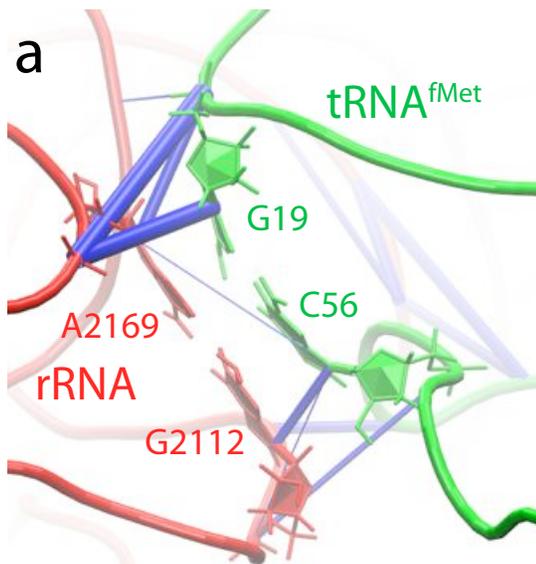
Signaling Networks in LSU & S5U



MD 140ns network



P/E site tRNA:rRNA network



L. Trabuco, E. Schreiner, J. Eargle
et al. JMB 2010

VMD/MultiSeq Tutorials

1. Evolution of Translation: AARS:tRNA
2. Evolution of Translation: EF-Tu:tRNA
3. Evolution of Translation: Ribosome
4. Dynamical Network Analysis - new

Molecular Dynamics Simulations

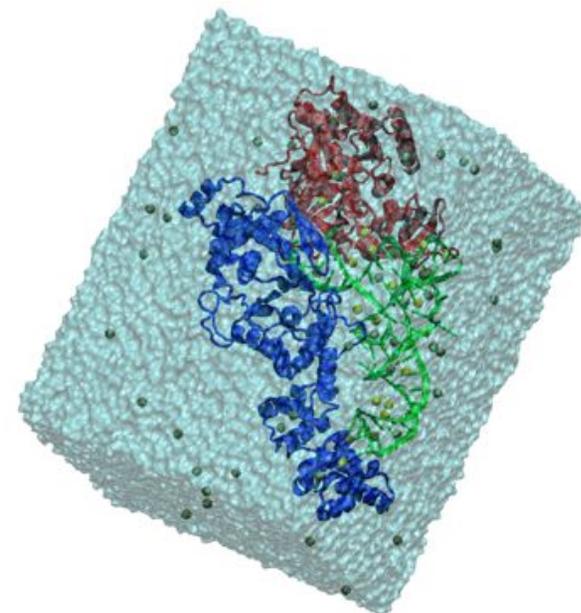
MD performed with NAMD2 (1) - System Setup

Simulation Parameters

Minimization: 290,000 steps
Production run: 108 ns
Forcefields: CHARMM27 (2), AMBER (3)
Time step: 1 fs
VdW frequency: 2 fs
VdW cutoff: 12 Å
Switching distance: 10 Å
Pair list distance: 14 Å
Particle Mesh Ewald
Full electrostatic update: 4 fs
Ensemble: NPT
Langevin temperature: 298.15 K
Langevin pressure: 1 atm
Periodic boundary conditions

Contents of System(4)

GluRS
Glu-tRNA^{Glu}
EF-Tu
GTP
Ions: Mg²⁺, K⁺
H₂O: ~27,000 molecules
System: ~130,000 atoms

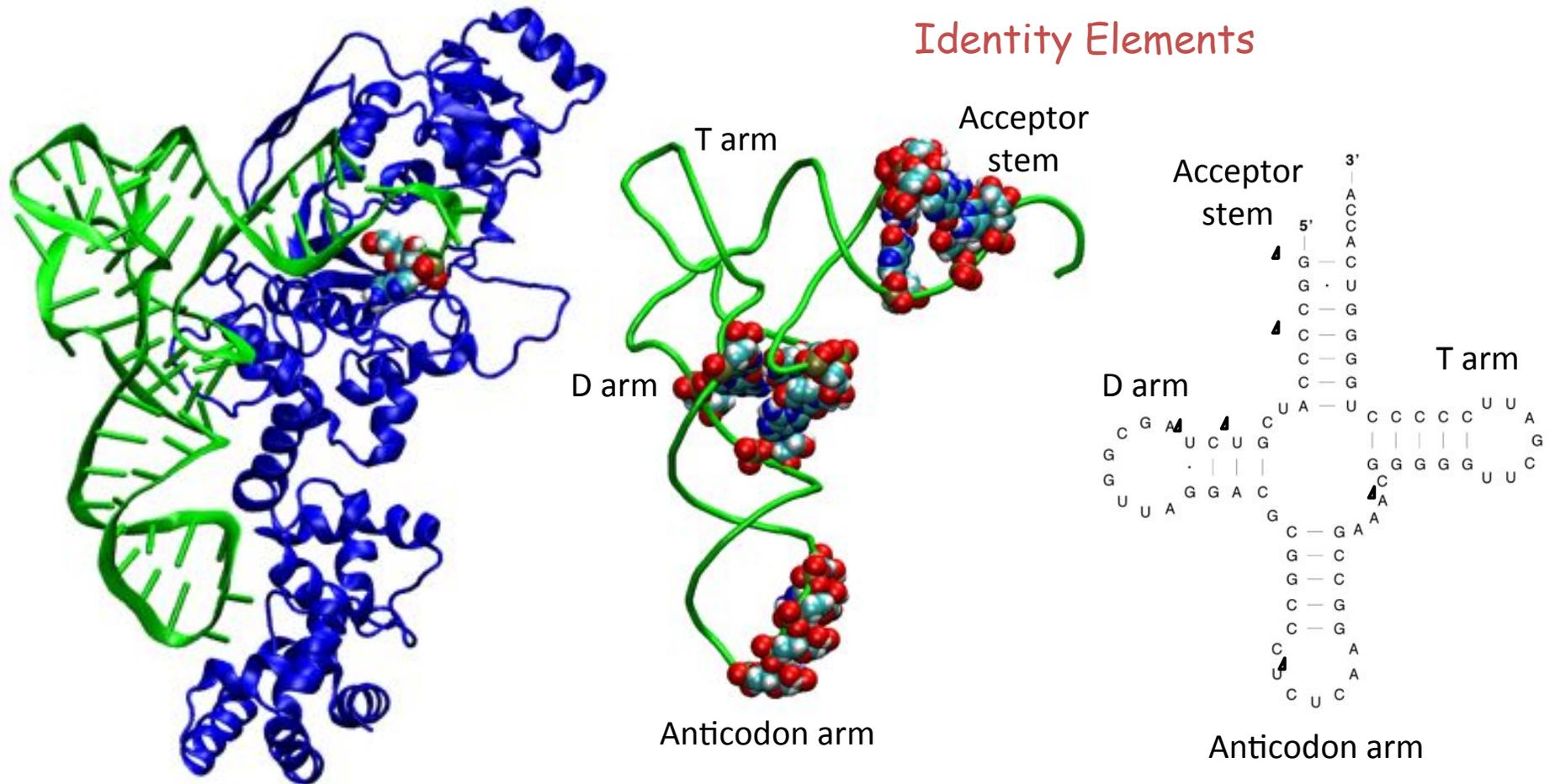


System Perturbations

Deprotonation/protonation of reactants (aa,NTs)
Changing rotamer states of residues (5)
involved in long-lived salt bridges

- (1) Phillips, J.C. et al. *J. Comput Chem*, (2005);
- (2) MacKerell, A. et al. *Biopolymers* (2001);
- (3) Case, D. et al. *J. Comput. Chem.* (2005);
- (4) Eargle, J. et al. *JMB* 2010, *FEBS Let.* 2010;
- (5) Dunbrack Jr. and Cohen. *Protein Sci.* (1997)

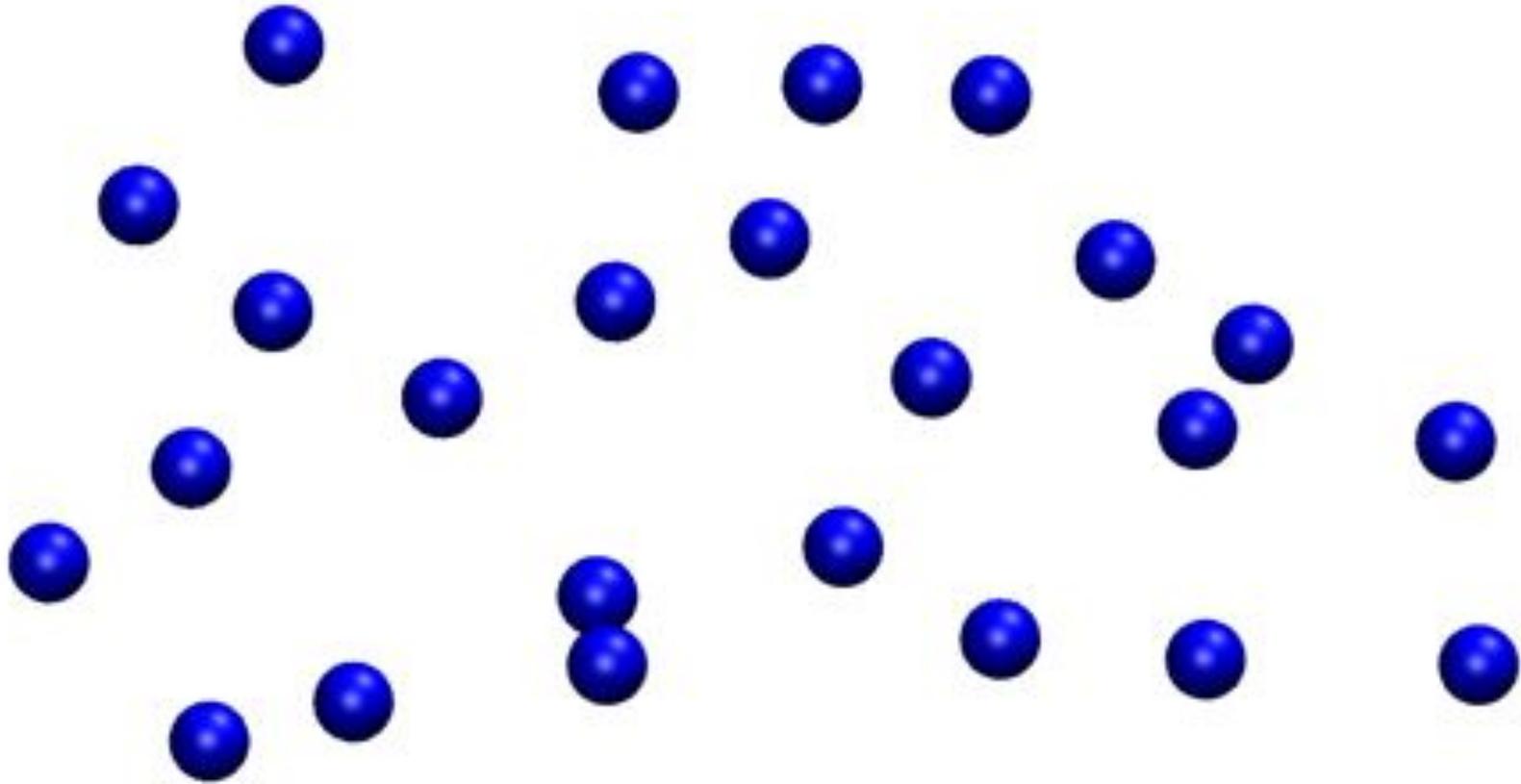
Charging tRNA through allosteric signaling



Overall Charging Reaction

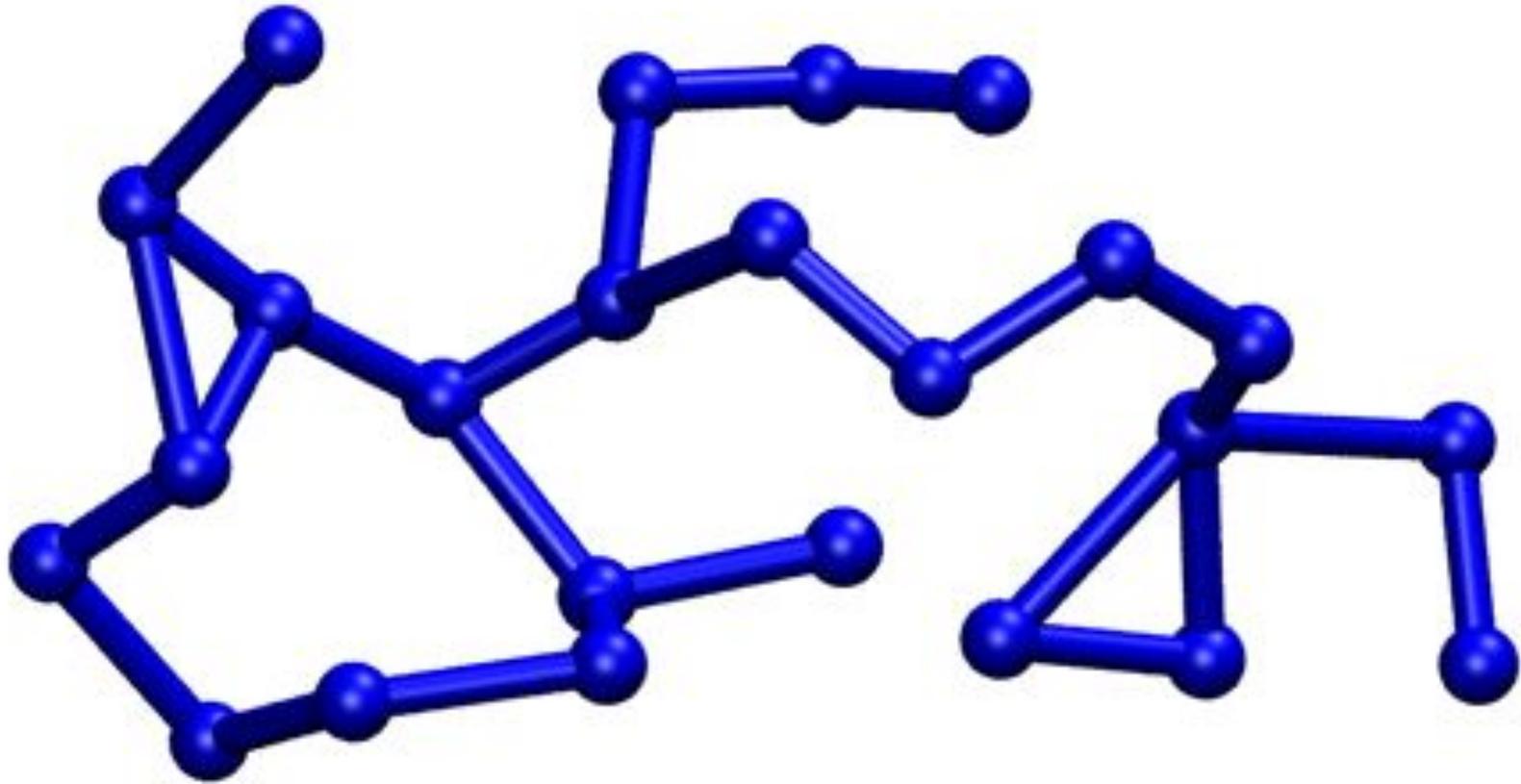


How to Construct a Network?



Nodes - defined at C_{α} (protein) and P (nucleotide) atoms

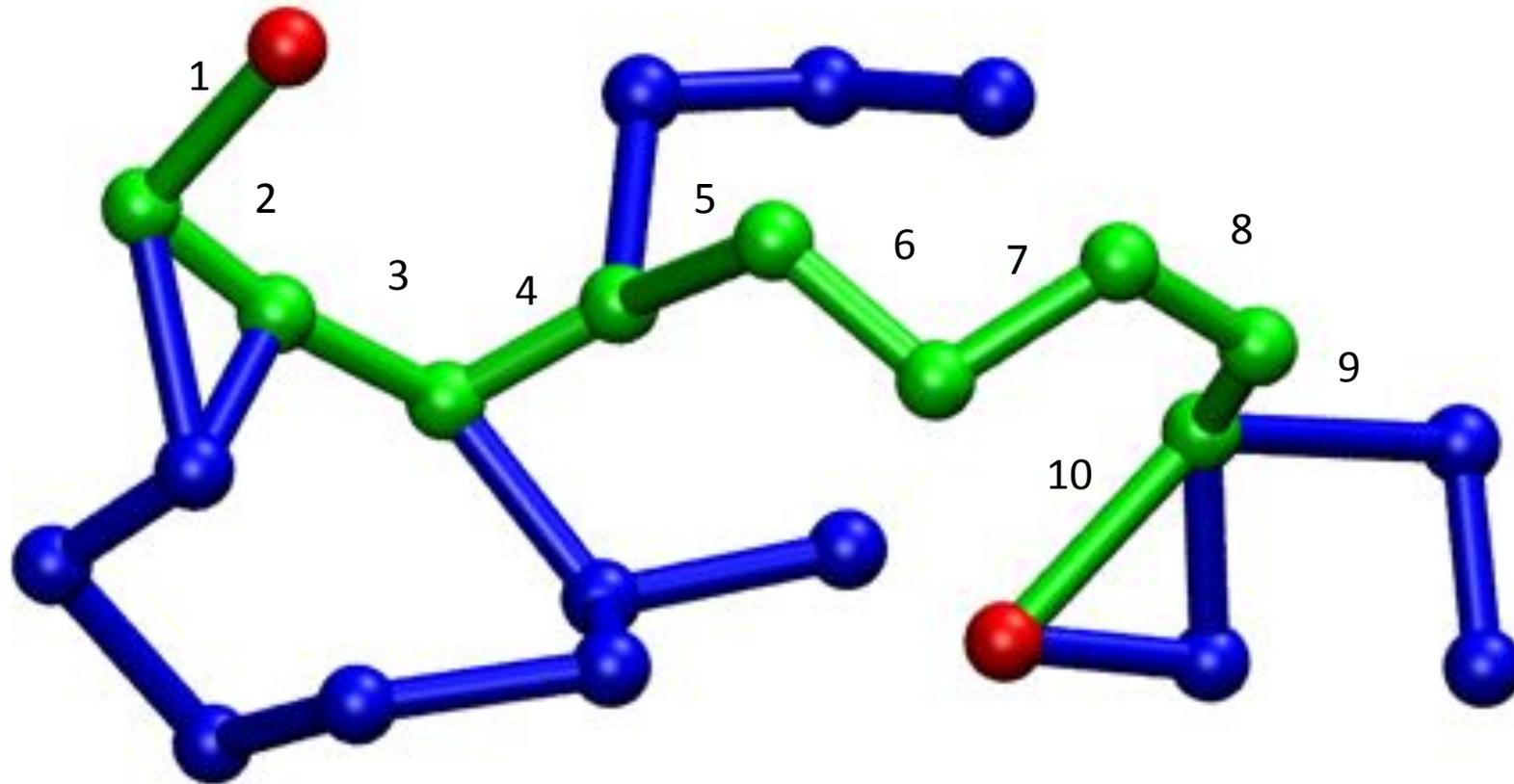
How to Construct a Network?



Edges - connect nodes that are within a contact distance threshold for more than 75% of an MD trajectory

Communication between Identity Elements and Site of Chemistry

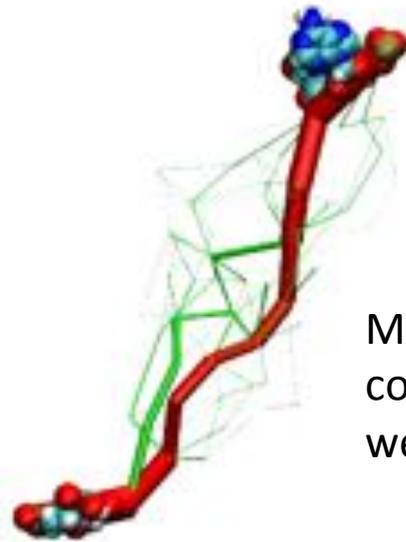
Different Paths can have Different Lengths



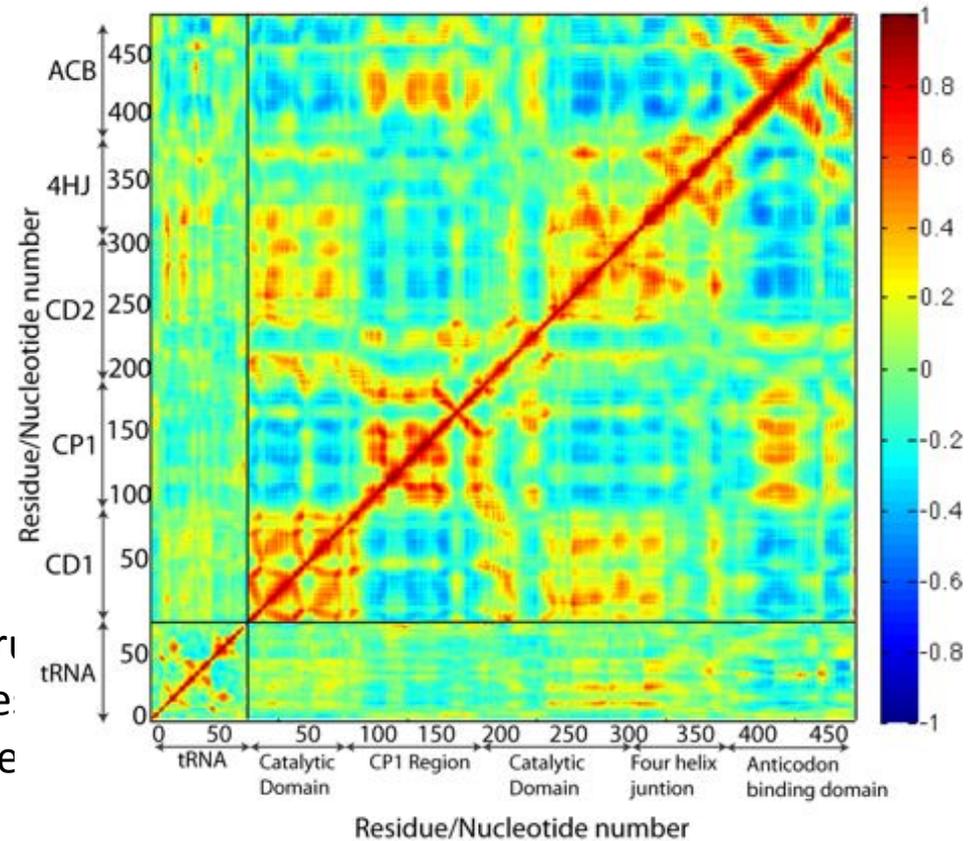
Path length = 10 (*unweighted*)

Information transfer? *Weight contacts/links by correlations !*

Correlations (C_{ij}) define signaling pathways in GluRS:tRNA

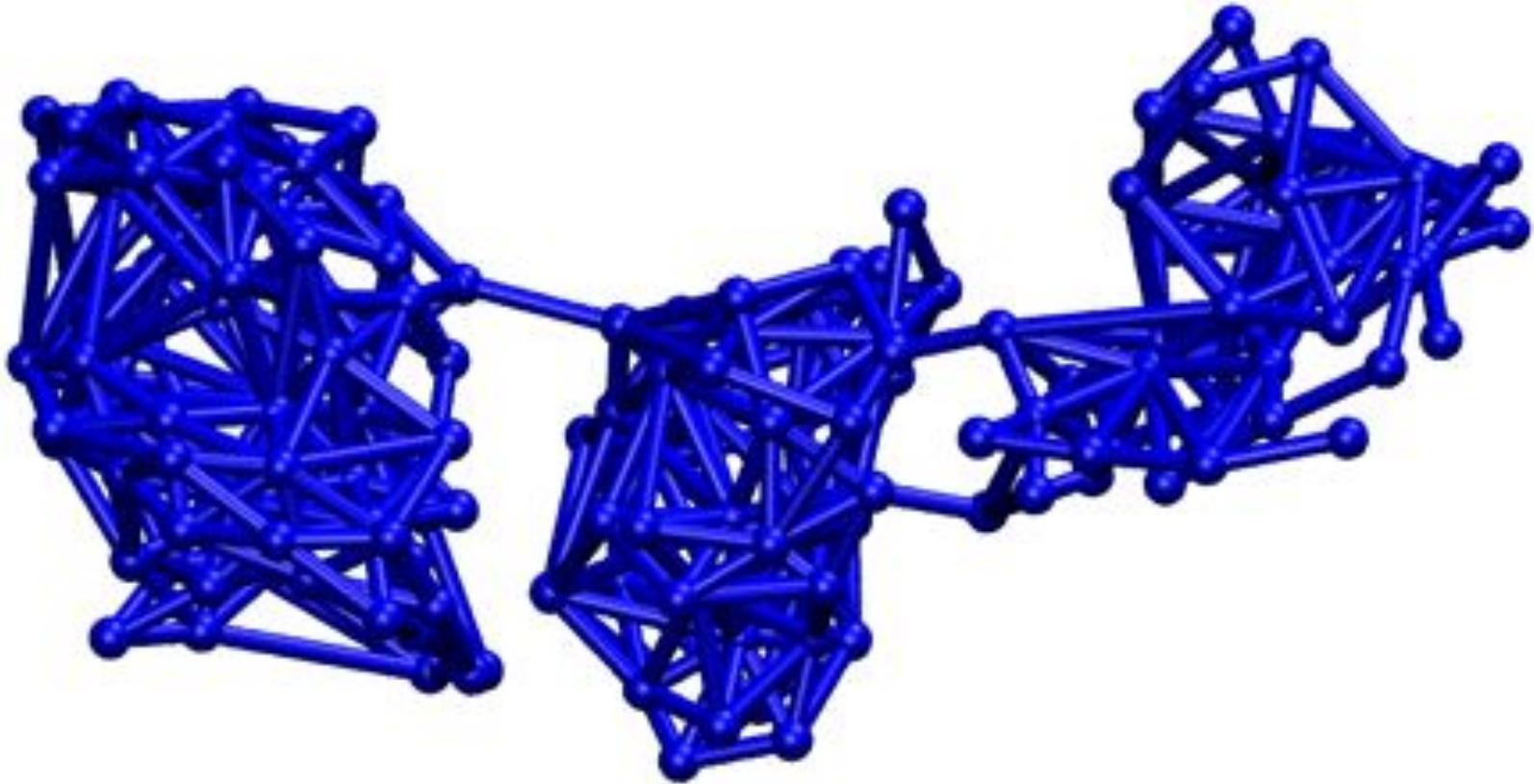


Modular str
communitie
weighted ne

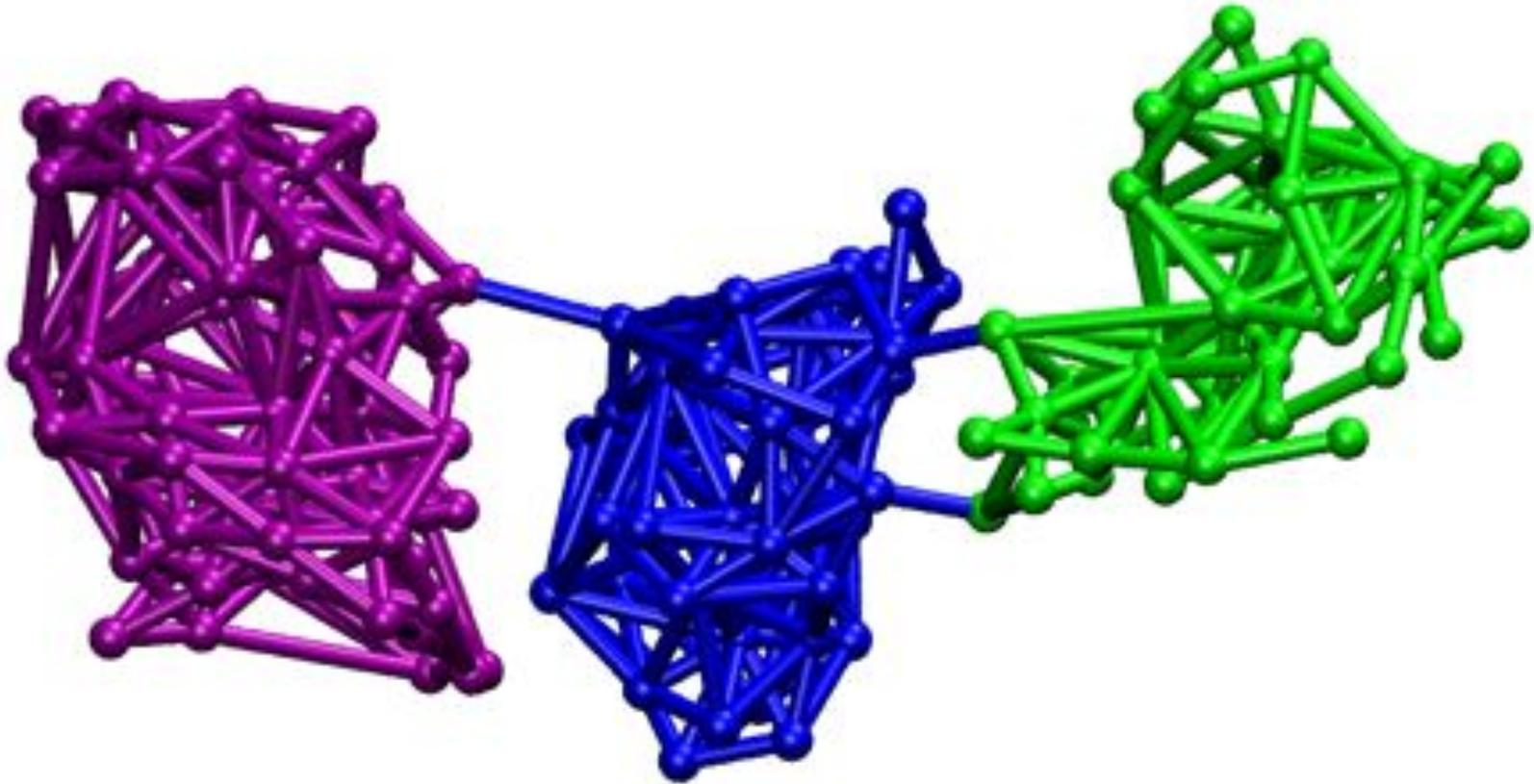


- MD simulations run with NAMD
- NTP ensemble
- Neutralized with Mg^{2+} and K^+
- C_{ij} values calculated over a 16-ns window

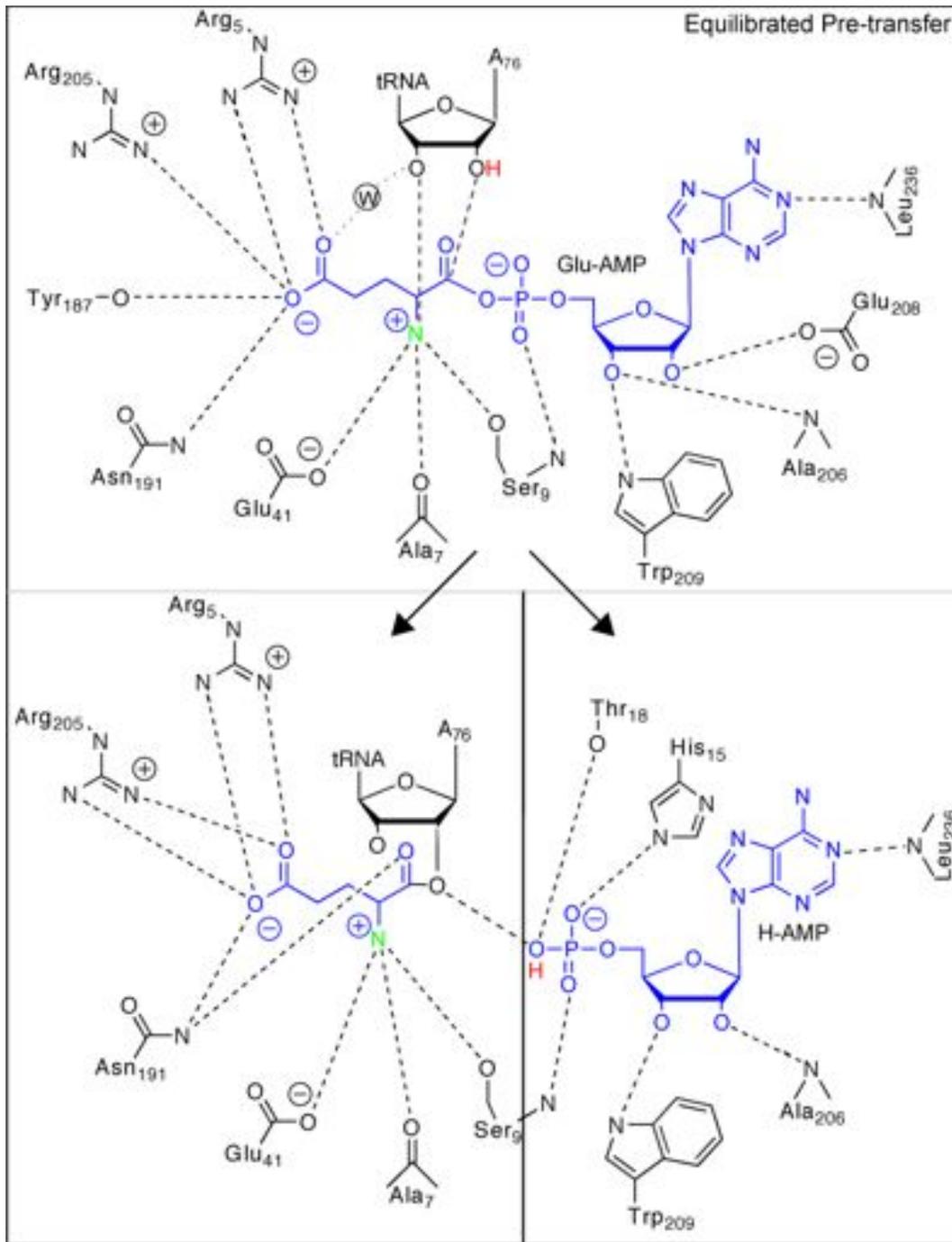
Nodes Cluster Together in Modules called
Communities



Nodes Cluster Together in Modules called Communities



Communities are subnetworks with many intracommunity edges but few intercommunity edges.



Reaction Mechanism for the Transfer of Glu to tRNA^{Glu}

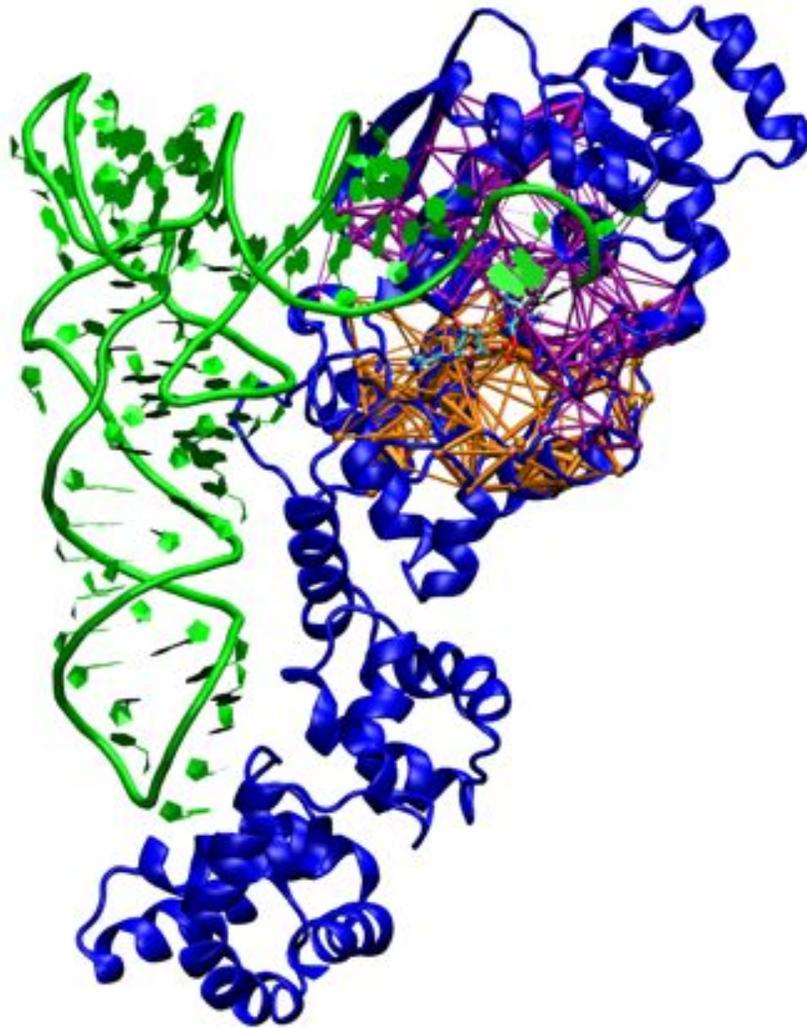
Perona JJ, Rould MA, Steitz TA
Biochemistry 1993

Black A, Eargle J, Sethi A,
Luthey-Schulten Z. *JMB* 2010
100s ns MD simulations

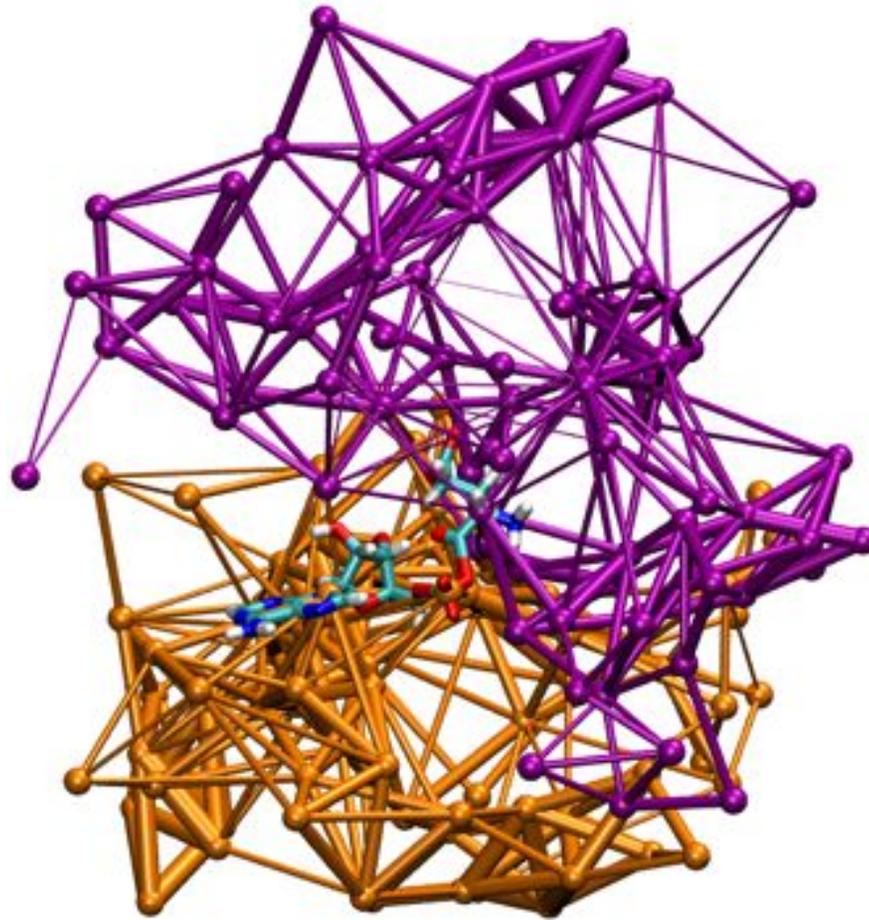
Community Structure Reveals Function in GluRS



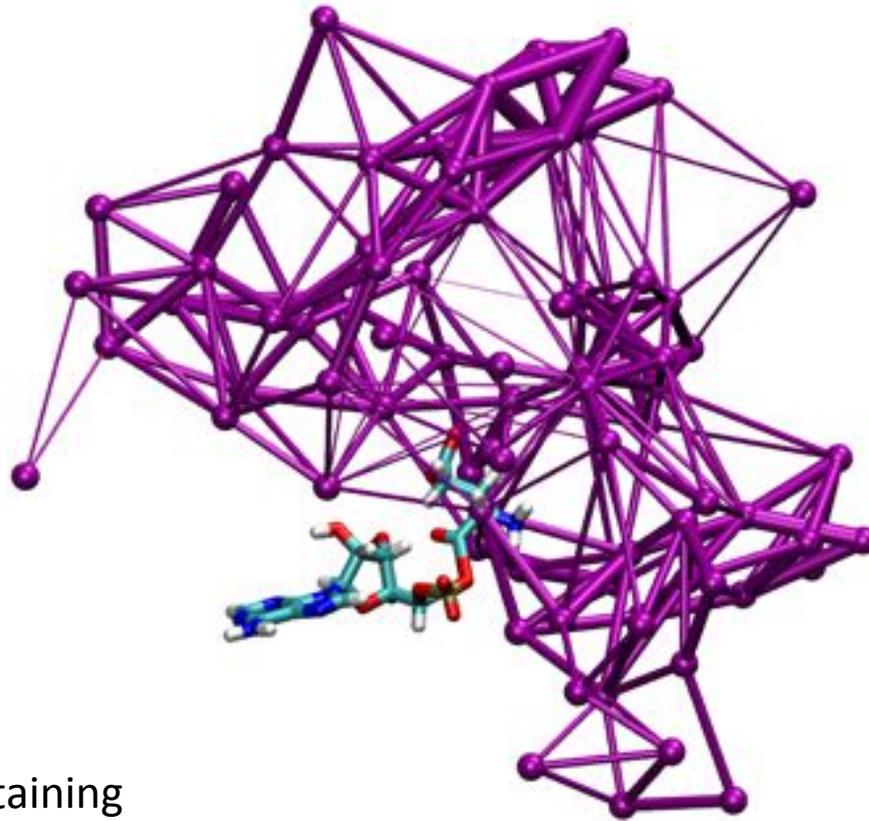
Community Structure Reveals Function in GluRS



Community Structure Reveals Function in GluRS



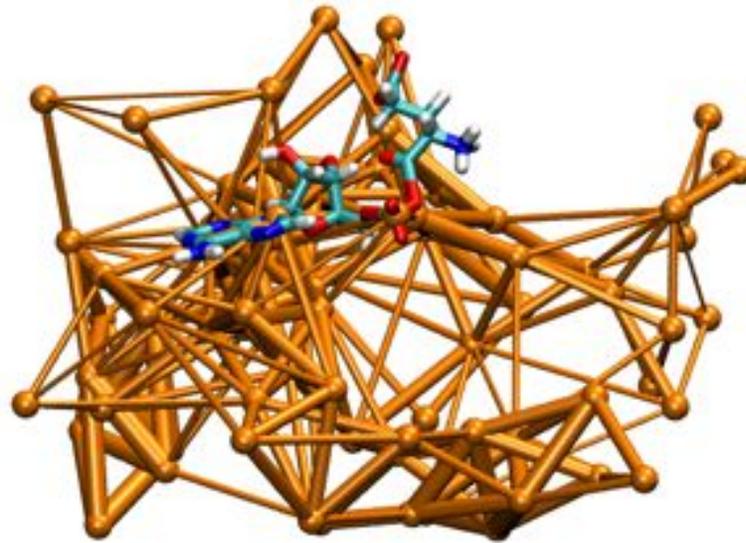
Community Structure Reveals Function in GluRS



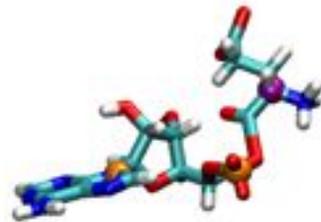
community containing
amino acid moiety

Community Structure Reveals Function in GluRS

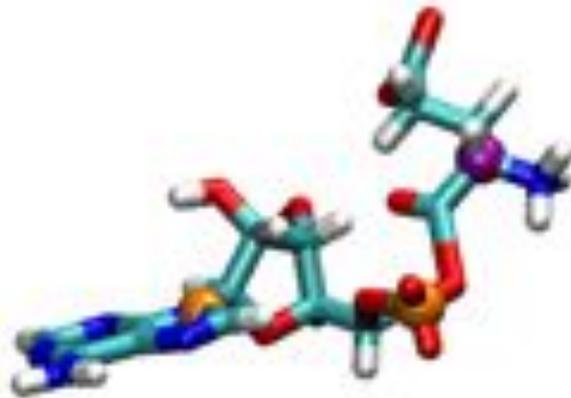
community containing
AMP moiety



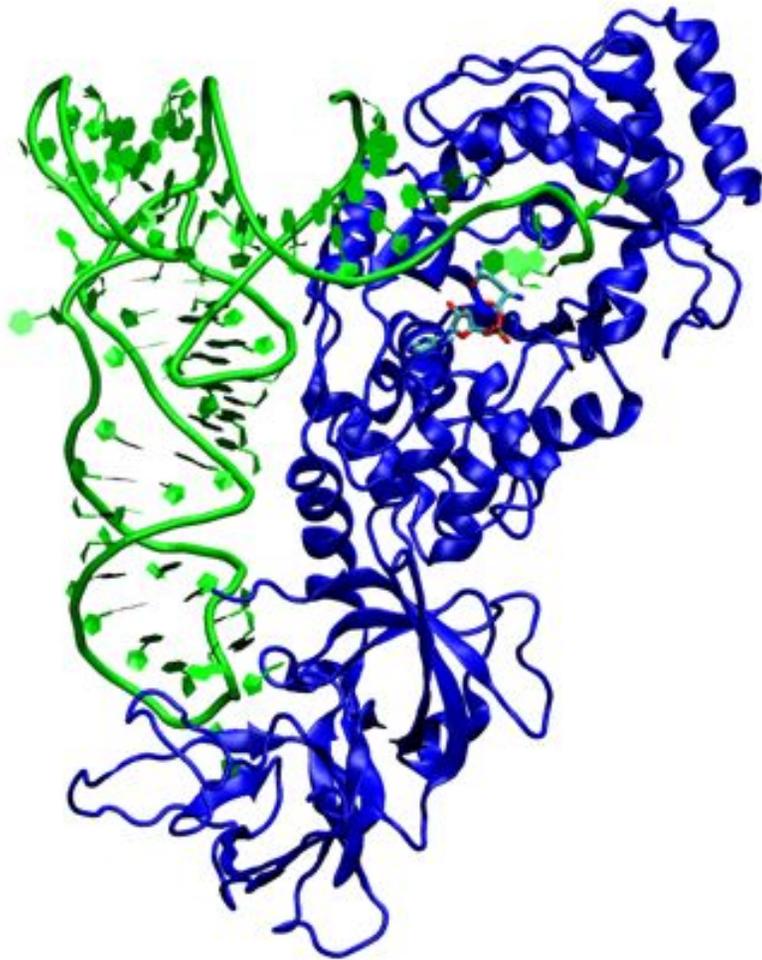
Community Structure Reveals Function in GluRS



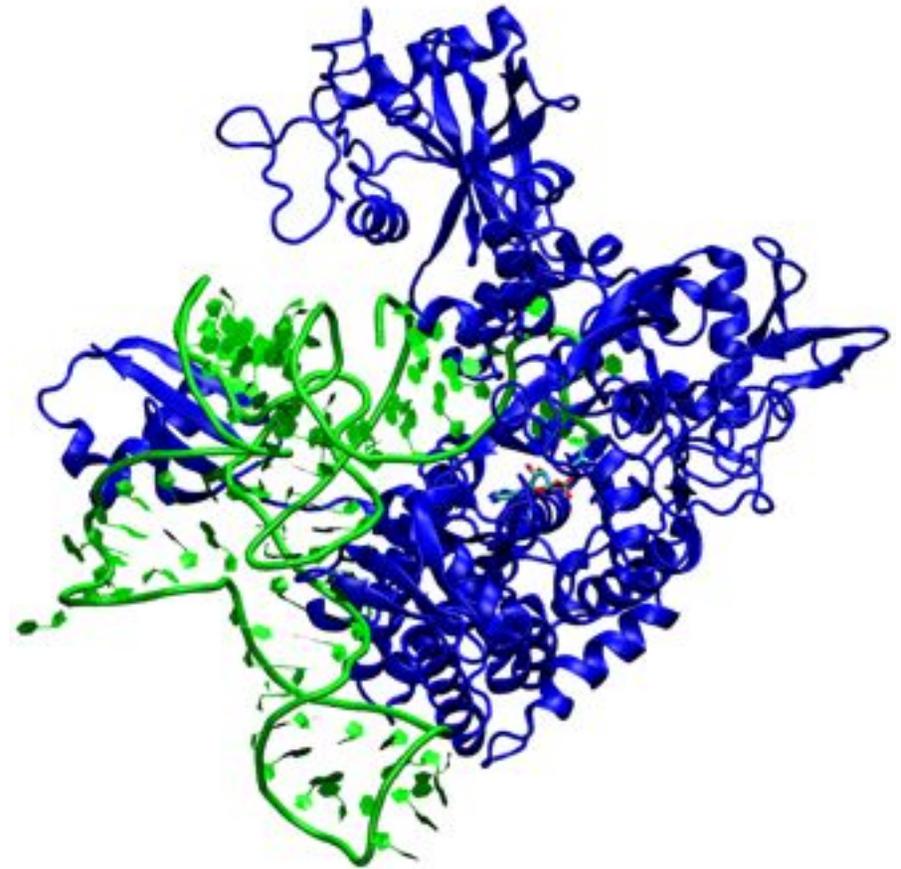
Community Structure Reveals Function in GluRS



Similar Ligand Separation in GlnRS and LeuRS

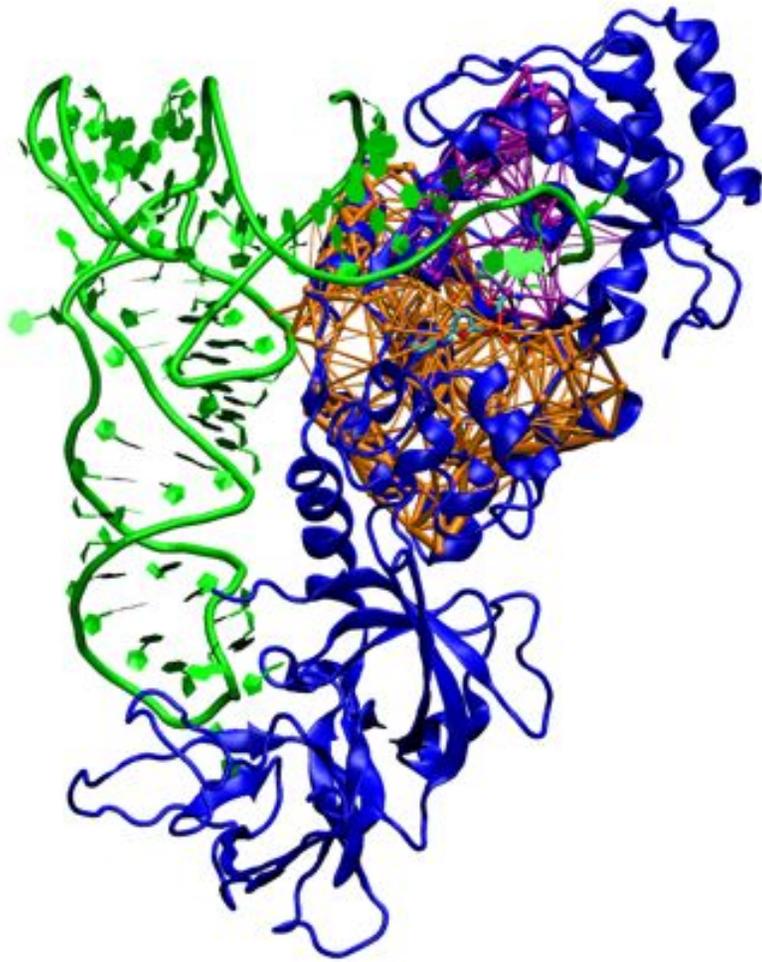


GlnRS

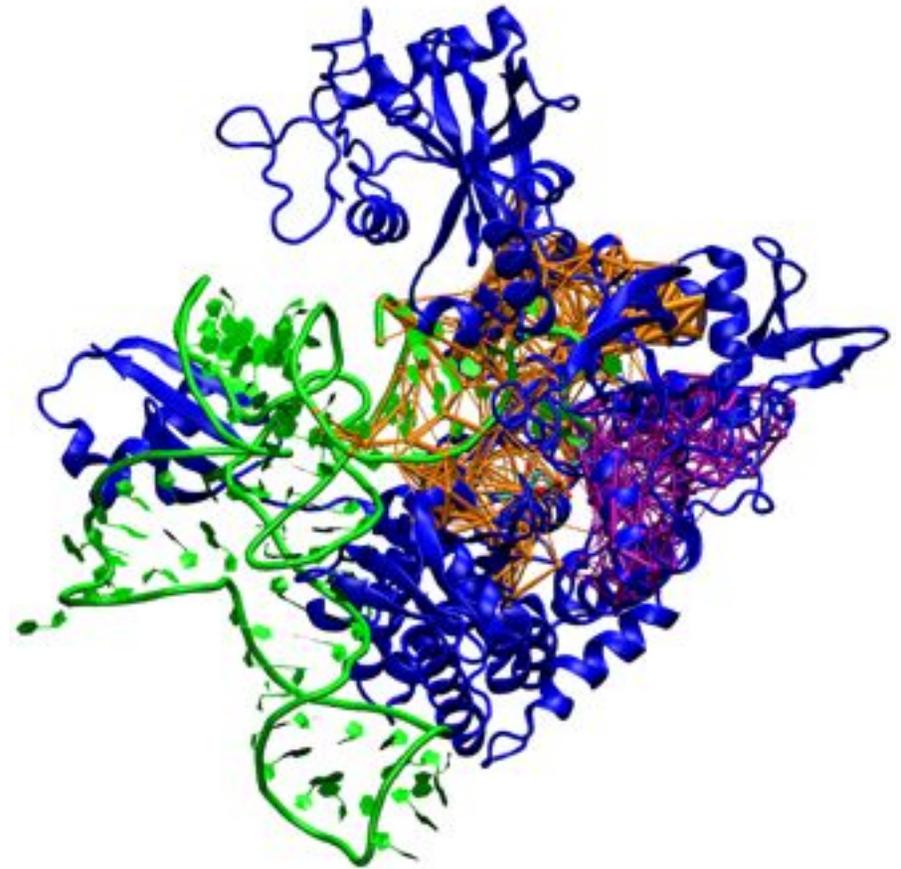


LeuRS

Similar Ligand Separation in GlnRS and LeuRS

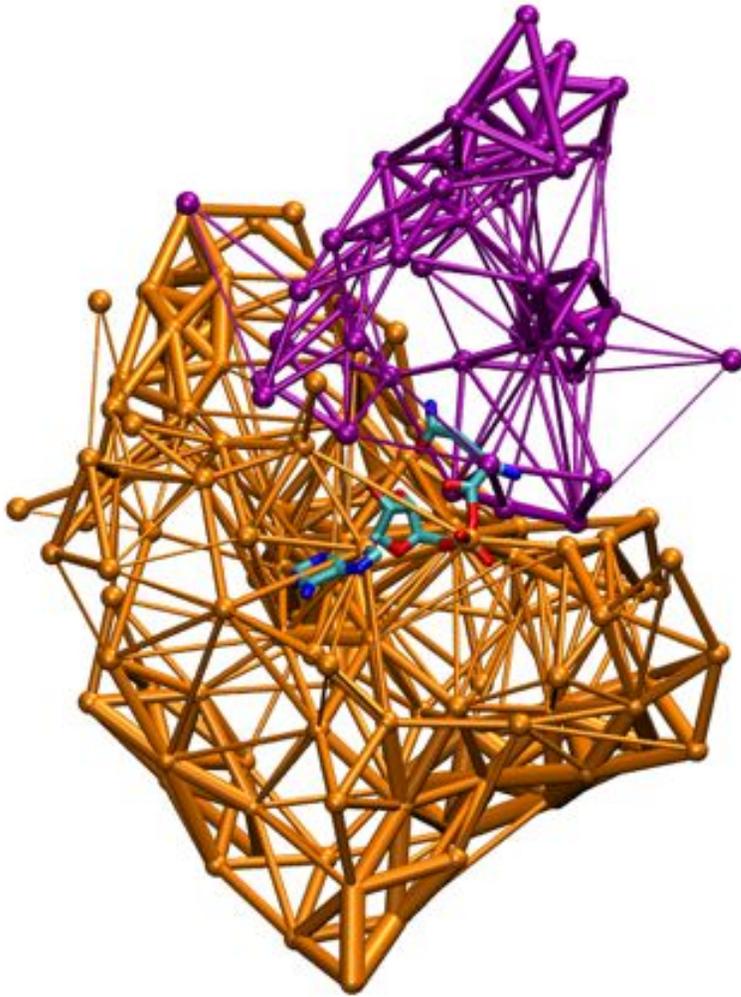


GlnRS

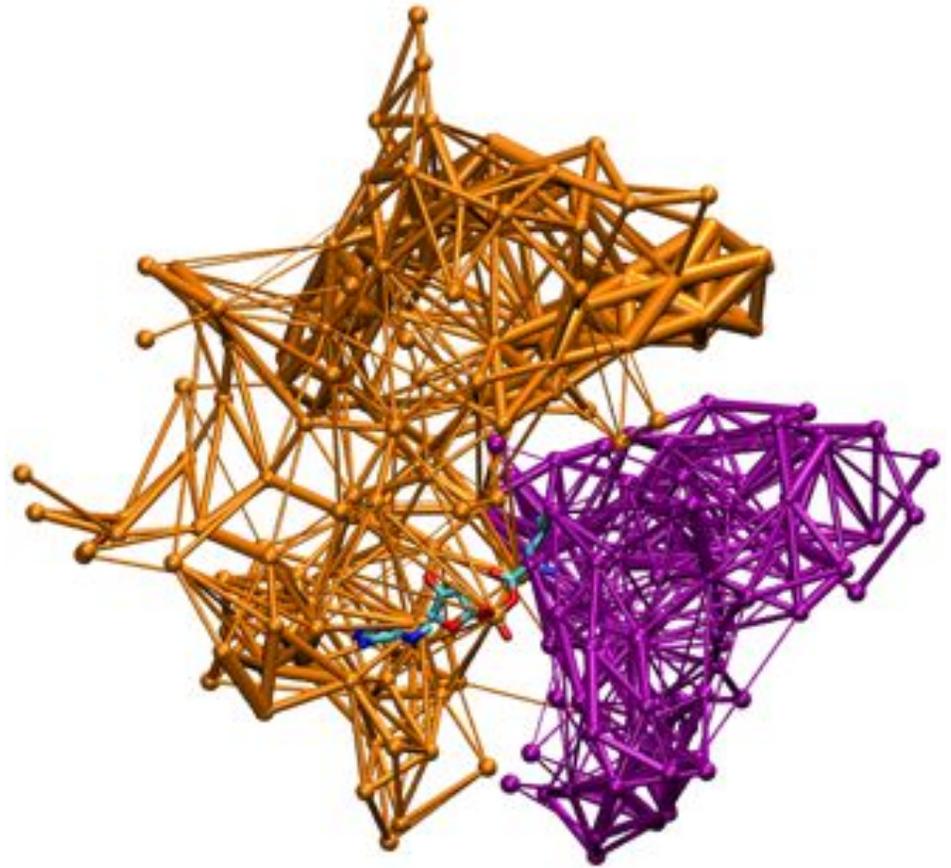


LeuRS

Similar Ligand Separation in GlnRS and LeuRS

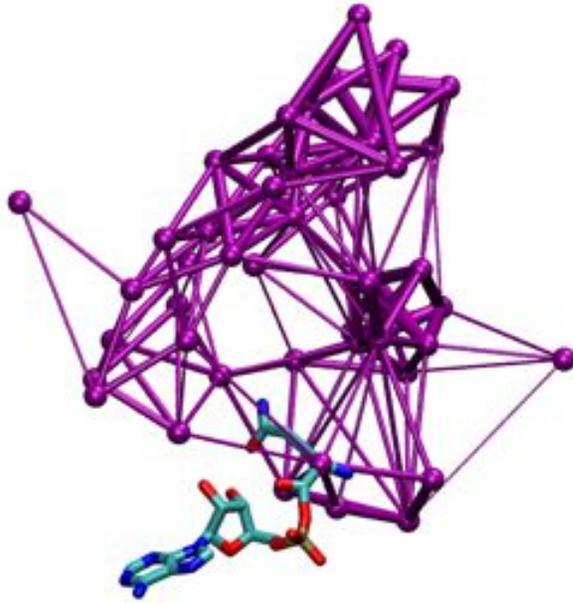


GlnRS



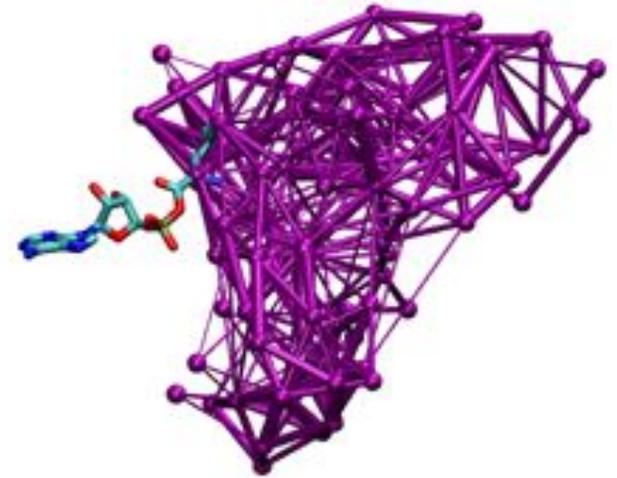
LeuRS

Similar Ligand Separation in GlnRS and LeuRS



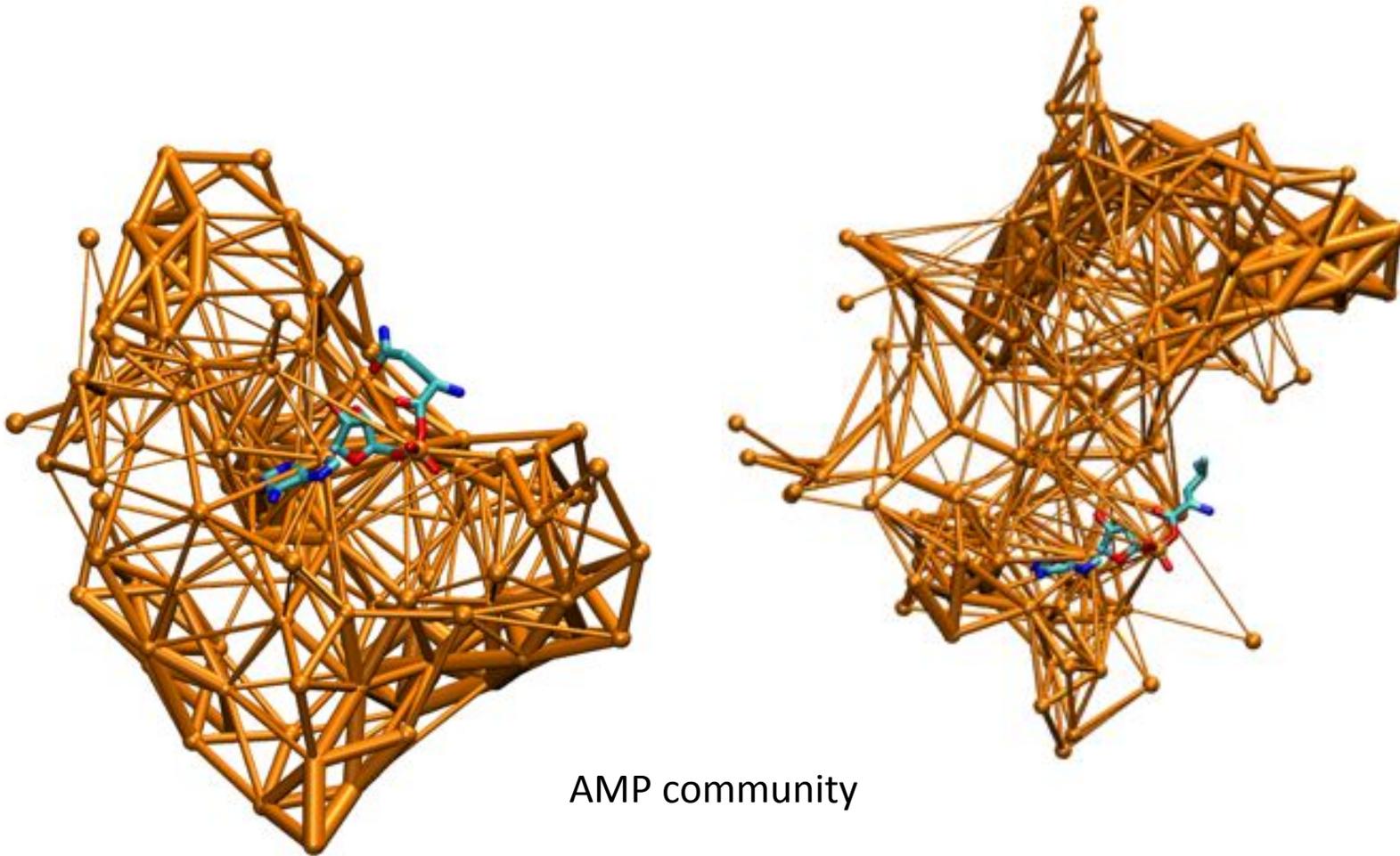
Amino acid community

GlnRS



LeuRS

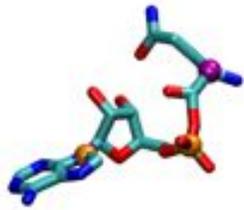
Similar Ligand Separation in GlnRS and LeuRS



GlnRS

LeuRS

Similar Ligand Separation in GlnRS and LeuRS

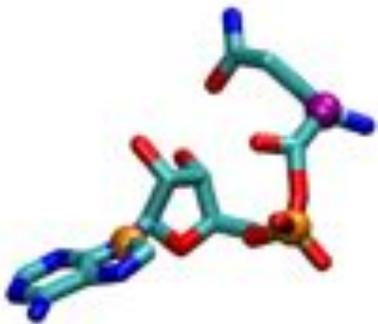


GlnRS

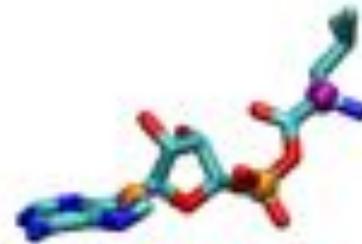


LeuRS

Similar Ligand Separation in GlnRS and LeuRS

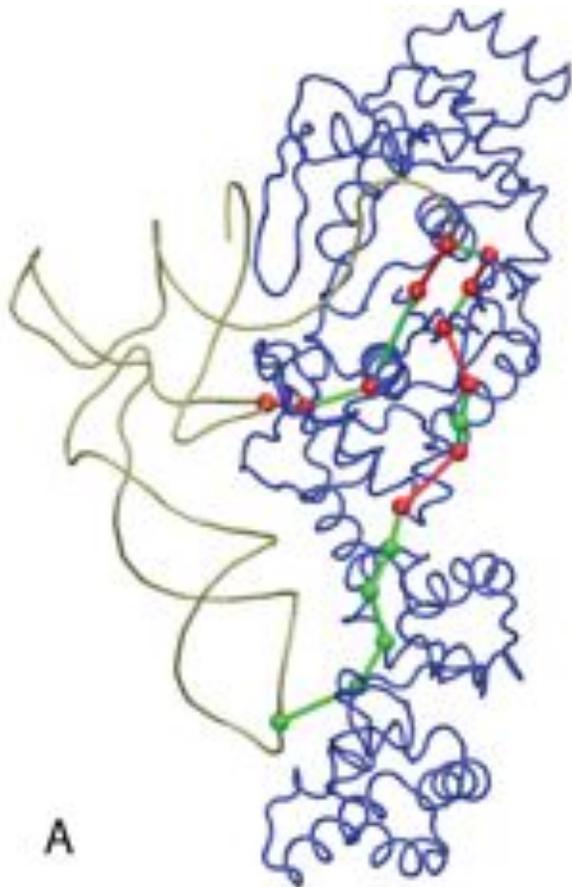


GlnRS

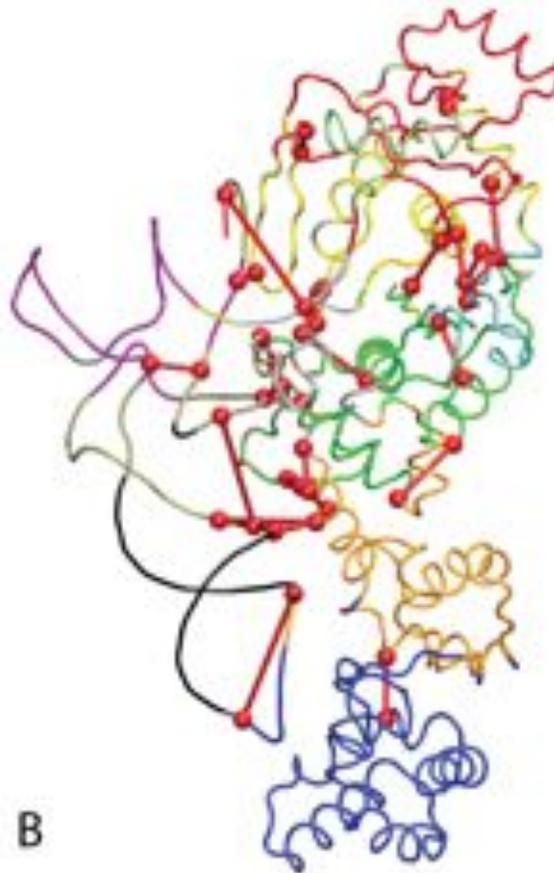


LeuRS

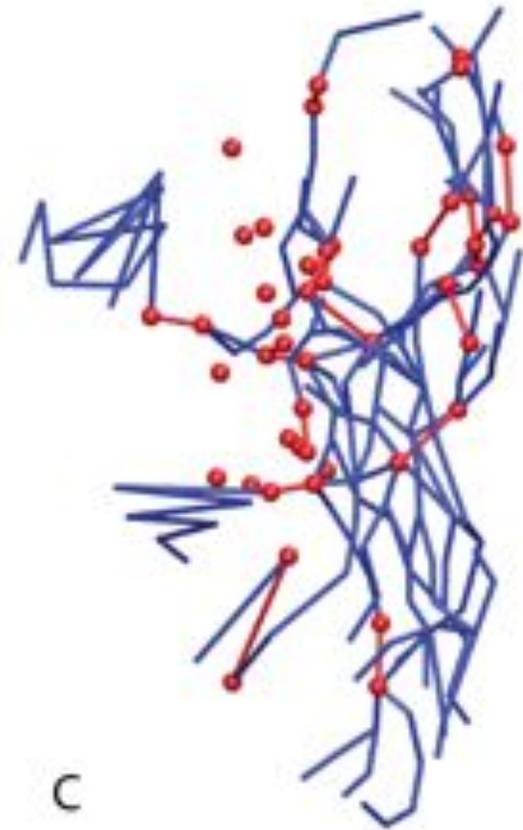
Dynamical Networks, Conservation, and Betweenness



Optimal signal pathways:
U13, U35 to A76



Critical(conserved) nodes
connecting communities



Betweenness routes - highest
density pair optimal paths