

Temperature Echoes in Proteins

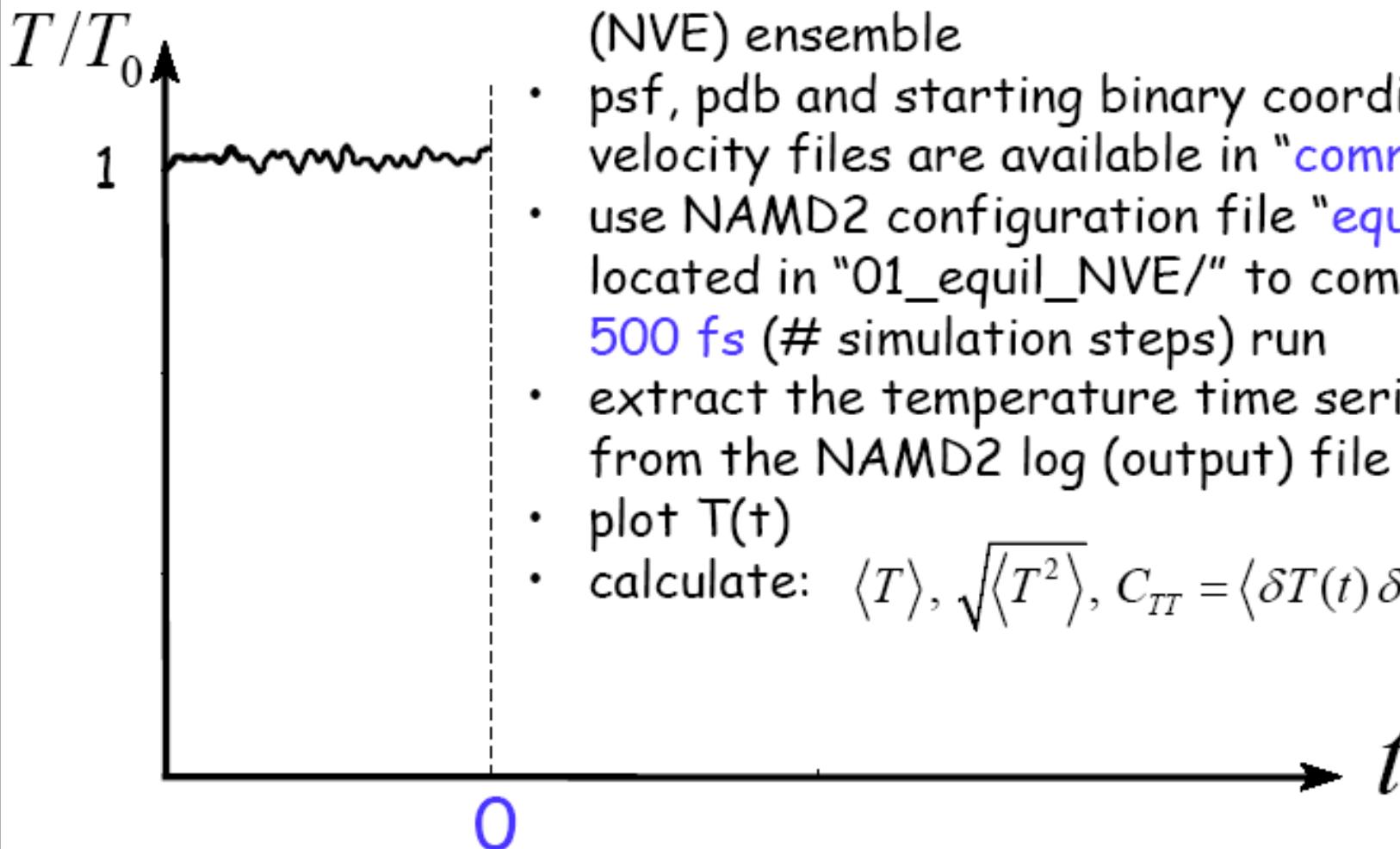
- ▶ Coherent motion in proteins: Echoes
 - ▶ Generation of echoes in *ubiquitin* via velocity reassessments
 - 1) Temperature quench echoes
 - 2) Constant velocity reassignment echoes
 - 3) Velocity reassignment echoes
- temperature \Leftrightarrow velocities

kinetic temperature:

$$T(t) = \frac{2}{(3N-6)k_B} \sum_{n=1}^{3N-6} \frac{m_n v_n^2(t)}{2}$$

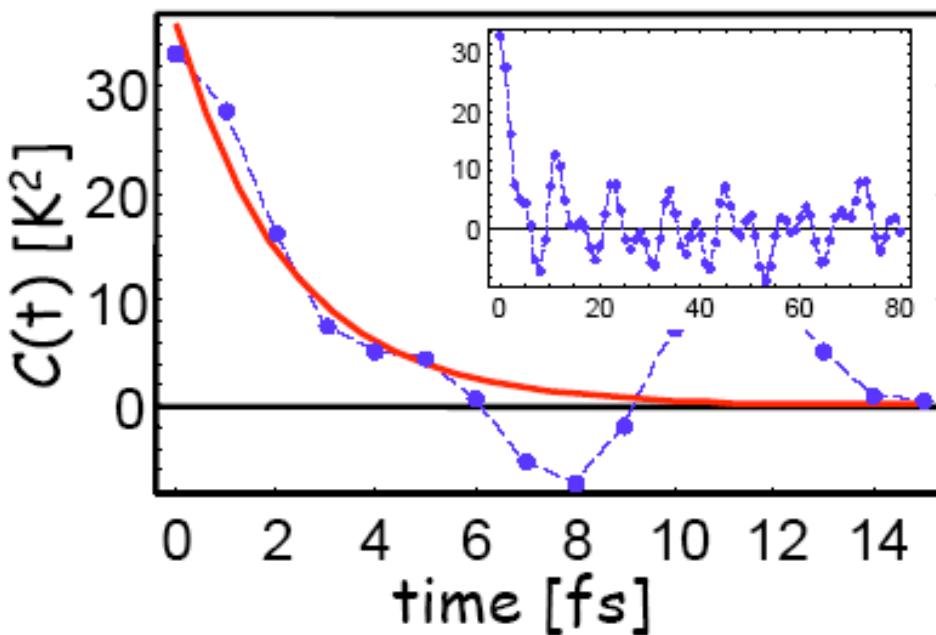
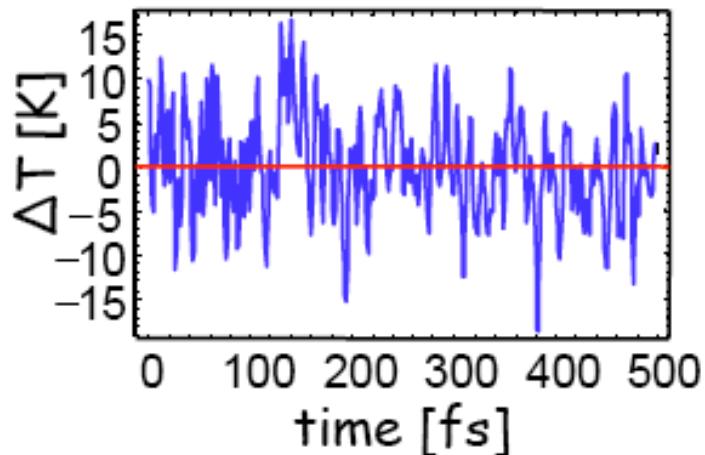
Generating T-Quench Echo: Step1

- your system is ubiquitin (1UBQ) in vacuum, pre-equilibrated at $T_0=300K$
- run all simulations in the *microcanonical* (NVE) ensemble
- psf, pdb and starting binary coordinate and velocity files are available in "common/"
- use NAMD2 configuration file "equil.conf" located in "01_equil_NVE/" to complete a **500 fs** (# simulation steps) run
- extract the temperature time series $T(t)$ from the NAMD2 log (output) file
- plot $T(t)$
- calculate: $\langle T \rangle$, $\sqrt{\langle T^2 \rangle}$, $C_{TT} = \langle \delta T(t) \delta T(0) \rangle$



Temperature Autocorrelation Function

$$\Delta T(t) = T(t) - \langle T(t) \rangle$$



$$C(t) = \langle \Delta T(t) \Delta T(0) \rangle$$

$$\rightarrow C(t_i) \approx \frac{1}{N-i} \sum_{n=1}^{N-i} \Delta T(t_{n+i}) \Delta T(t_n)$$

$$C(t) = C(0) \exp(-t/\tau_0)$$

Temperature relaxation time:

$$\tau_0 \approx 2.2 \text{ fs}$$

Mean temperature:

$$\langle T \rangle = 299 \text{ K}$$

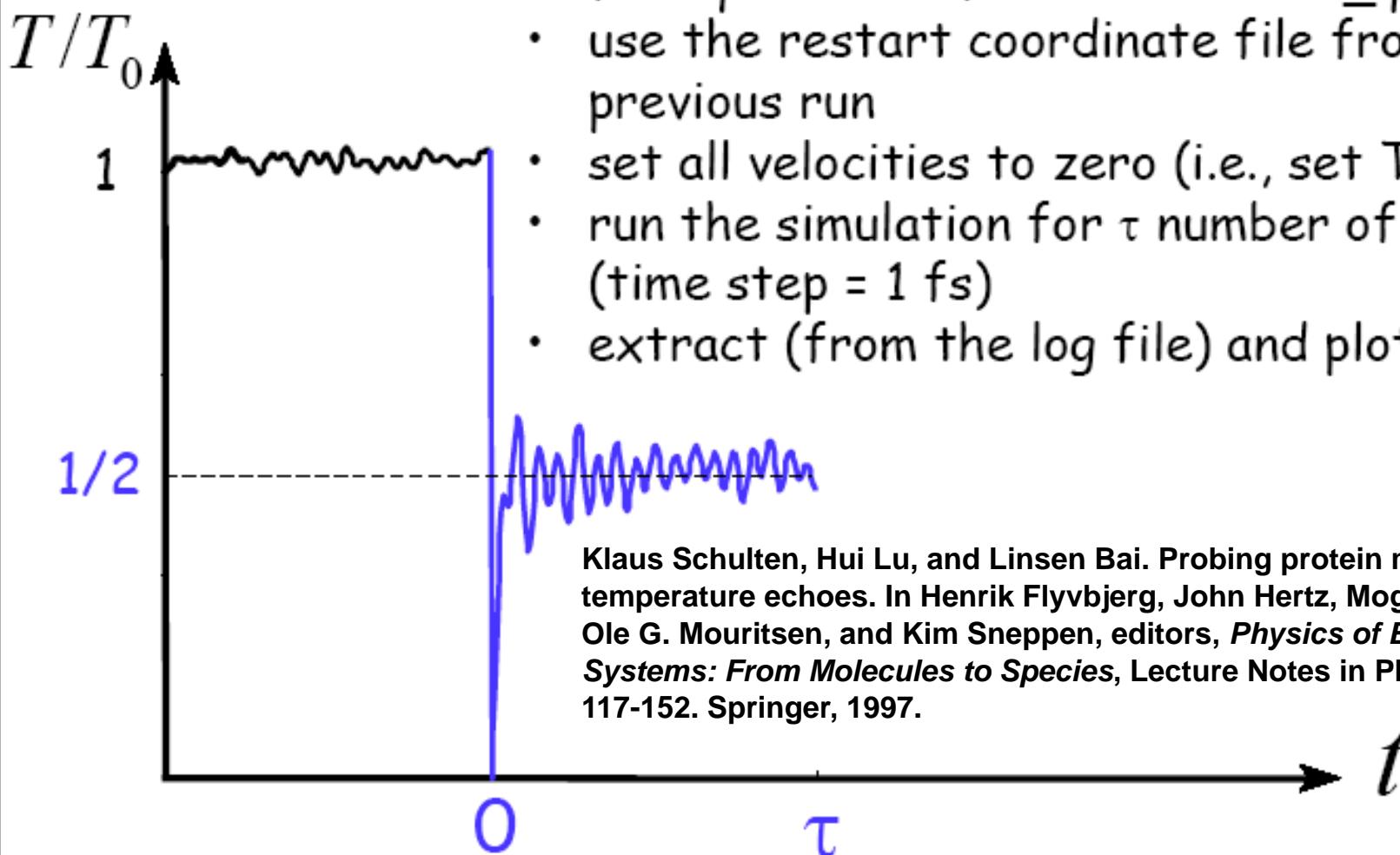
RMS temperature:

$$\sqrt{\langle (\Delta T)^2 \rangle} = \sqrt{C(0)} = 6 \text{ K}$$

Generating T-Quench Echo: Step2

Perform the 1st temperature quench

- start a new simulation using configuration file "quench.conf" located in "O2_quencha/"
- use the restart coordinate file from the previous run
- set all velocities to zero (i.e., set $T=0$)
- run the simulation for τ number of steps (time step = 1 fs)
- extract (from the log file) and plot $T(t)$

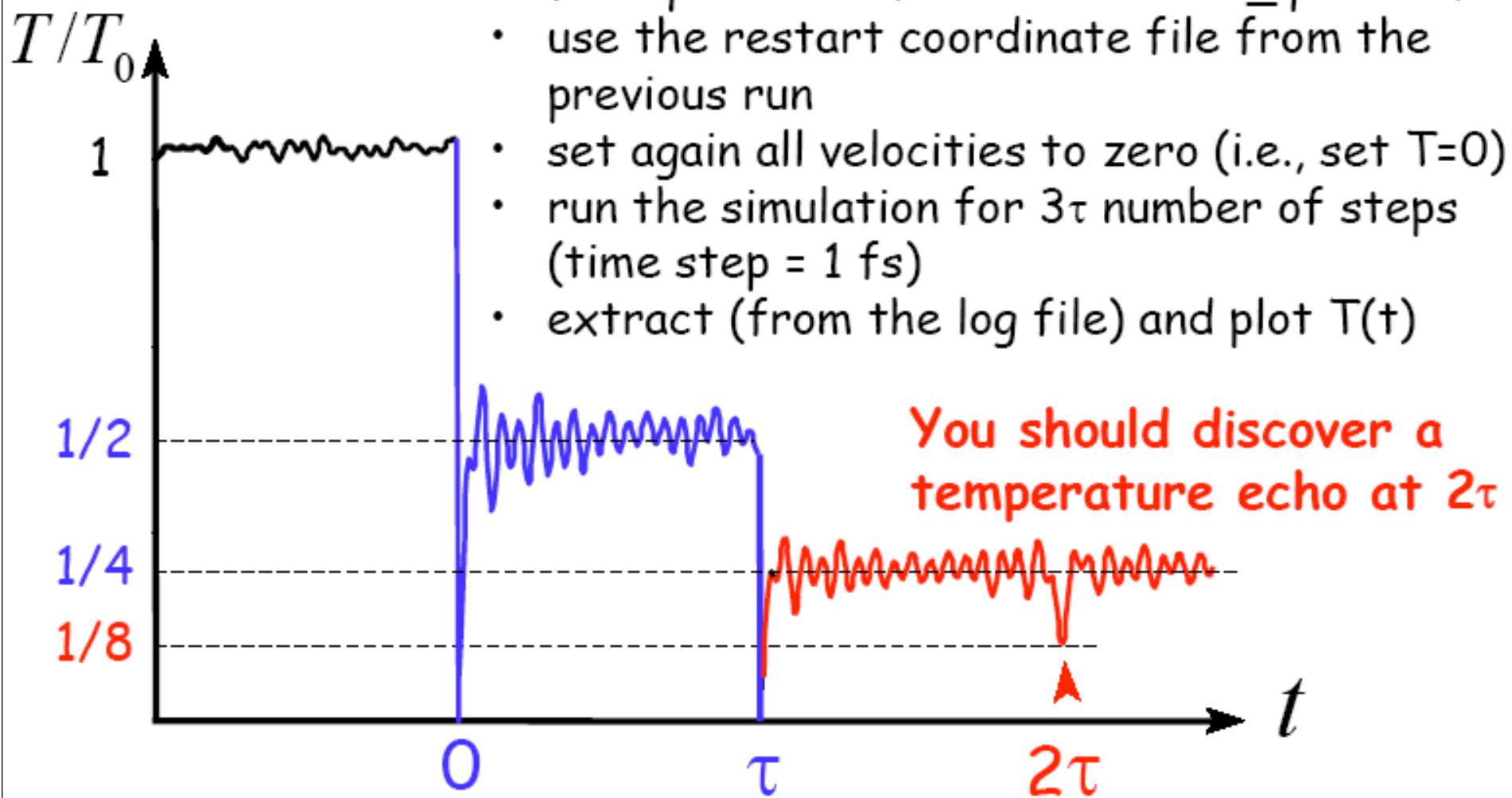


Klaus Schulten, Hui Lu, and Lisen Bai. Probing protein motion through temperature echoes. In Henrik Flyvbjerg, John Hertz, Mogens H. Jensen, Ole G. Mouritsen, and Kim Sneppen, editors, *Physics of Biological Systems: From Molecules to Species*, Lecture Notes in Physics, pp. 117-152. Springer, 1997.

Generating T-Quench Echo: Step3

Perform the 2nd temperature quench

- start a new simulation using configuration file "quench.conf" located in "03_quenchb/"
- use the restart coordinate file from the previous run
- set again all velocities to zero (i.e., set T=0)
- run the simulation for 3τ number of steps (time step = 1 fs)
- extract (from the log file) and plot T(t)



Explanation of the T-Quench Echo

Assumption: protein \approx collection of weakly interacting harmonic oscillators with dispersion $\omega = \omega_\alpha$, $\alpha = 1, \dots, 3N - 6$

Step1: $t < 0$

$$x(t) = A_0 \cos(\omega t + \theta_0)$$
$$v(t) = -\omega A_0 \sin(\omega t + \theta_0)$$

Step2: $0 < t < \tau$

$$\left. \begin{array}{l} x_1(t) = A_1 \cos(\omega t + \theta_1) \\ v_1(t) = -\omega A_1 \sin(\omega t + \theta_1) \end{array} \right\} \xrightarrow{v_1(0)=0} \left\{ \begin{array}{l} A_1 = A_0 \cos \theta_0 \\ \theta_1 = 0 \end{array} \right.$$

Step3: $t > \tau$

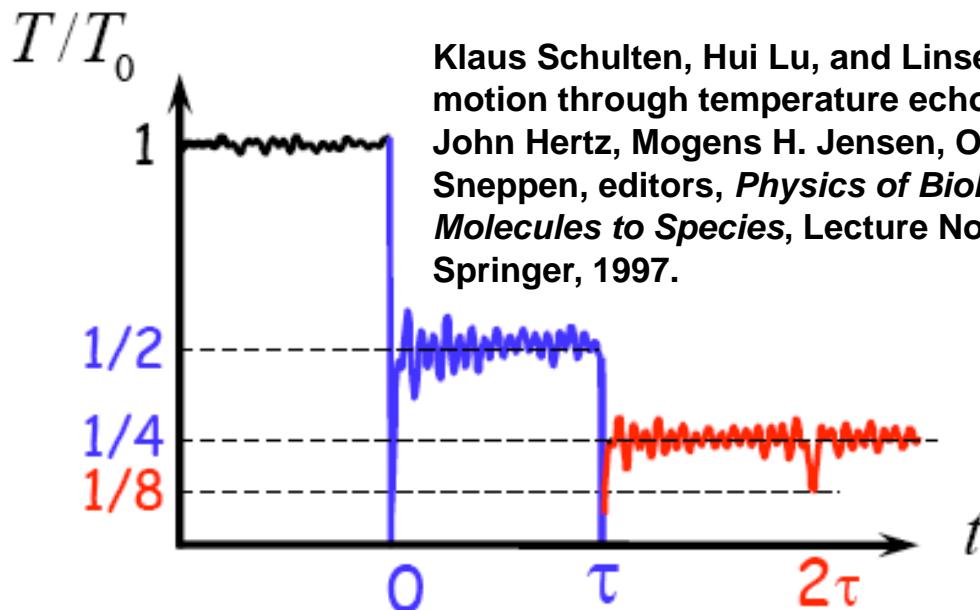
$$\left. \begin{array}{l} x_2(t) = A_2 \cos(\omega t + \theta_2) \\ v_2(t) = -\omega A_2 \sin(\omega t + \theta_2) \end{array} \right\} \xrightarrow{v_2(\tau)=0} \left\{ \begin{array}{l} A_2 = A_1 \cos \omega \tau \\ \theta_2 = -\omega \tau \end{array} \right.$$

T-Quench Echo: Harmonic Approximation

$$T(t) \approx \frac{T_0}{4} \left[1 - \langle \cos(2\omega(t-\tau)) \rangle - \frac{1}{2} \langle \cos(2\omega(t-2\tau)) \rangle \right]$$

$$\approx \begin{cases} 0 & \text{for } t = \tau \\ T_0/8 & \text{for } t = 2\tau \\ T_0/4 & \text{otherwise} \end{cases}$$

$$\Rightarrow \text{echo depth} = T(2\tau) - T_0/4 = T_0/8$$



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$T(t)$ and $C_{TT}(t)$

It can be shown:

$$\langle \cos(2\omega t) \rangle = \frac{\langle \delta T(t) \delta T(0) \rangle}{\langle \Delta T^2 \rangle} = C_{TT}(t), \quad \delta T(t) = T(t) - \langle T \rangle$$

Accordingly,

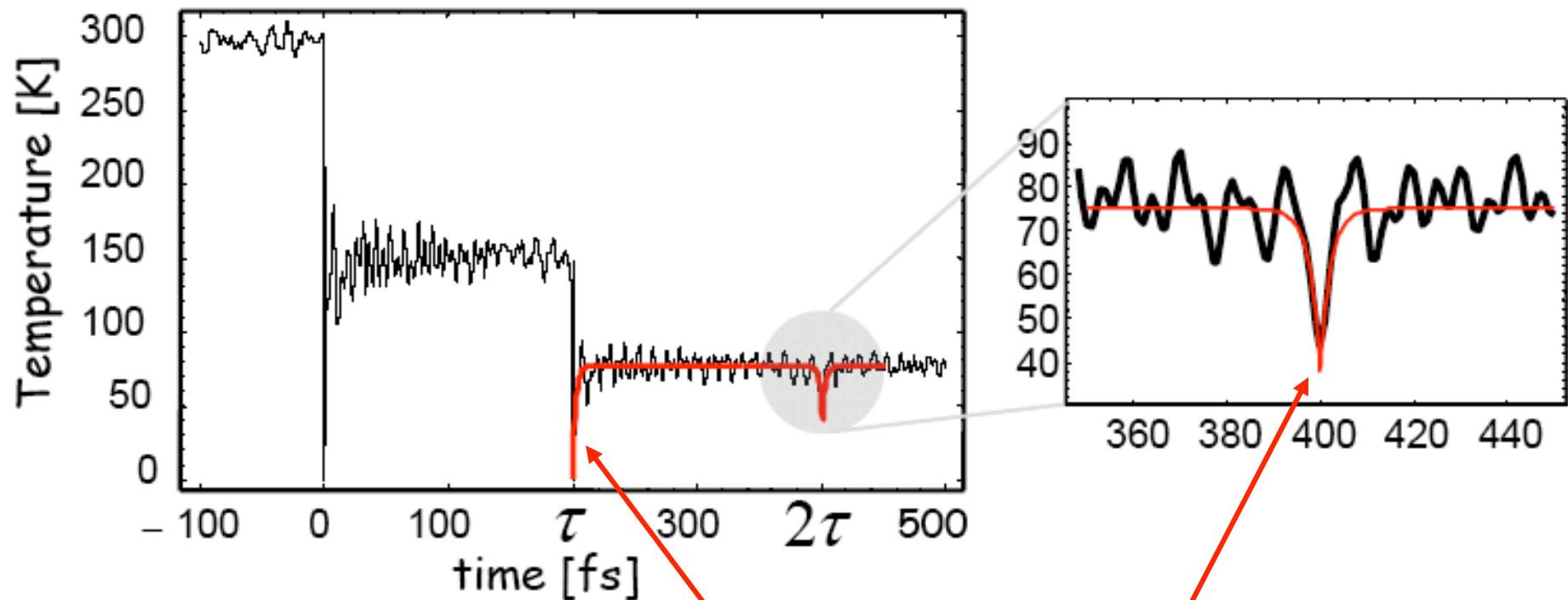
$$T(t) \approx \frac{T_0}{4} \left[1 - \langle \cos(2\omega(t - \tau)) \rangle - \frac{1}{2} \langle \cos(2\omega(t - 2\tau)) \rangle \right]$$



$$= \frac{T_0}{4} \left[1 - C_{TT}(t - \tau) - \frac{1}{2} C_{TT}(t - 2\tau) \right]$$

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T-Quench Echo: Harmonic Approximation

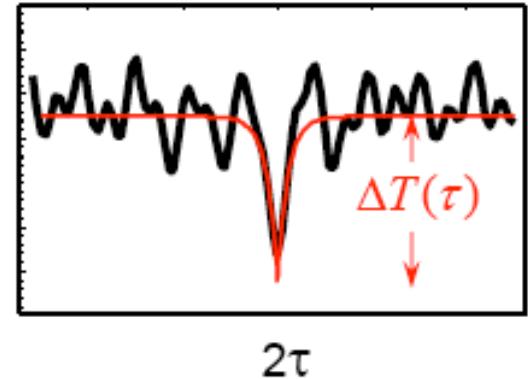
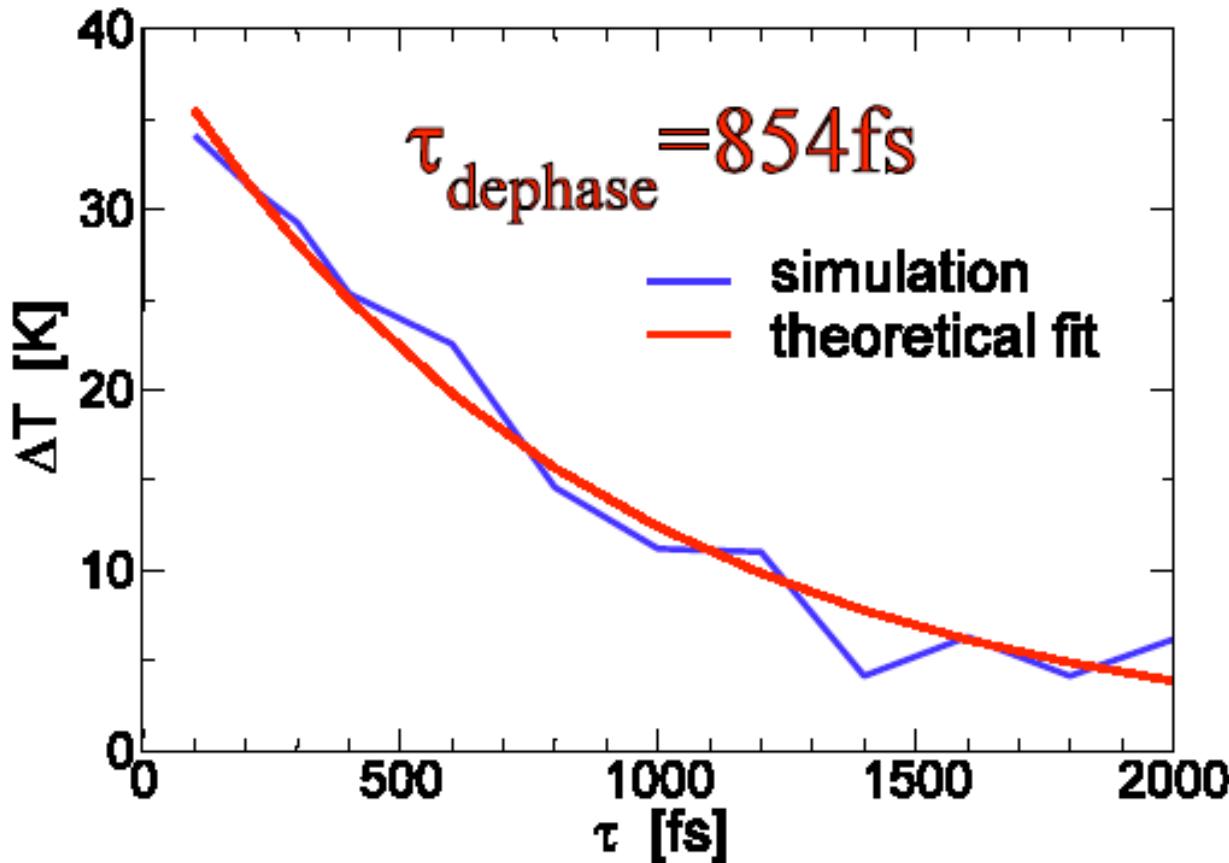


$$T(t) \approx \frac{T_0}{2} \left(1 - C_{TT}(t - \tau) - \frac{1}{2} C_{TT}(|t - 2\tau|) \right)$$

$$C_{TT}(t) = \exp(-t/\tau_0), \quad \tau_0 \approx 2.2 \text{ fs}$$

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Dephasing Time of T-Quench Echoes



$$\Delta T(\tau) = \Delta T(0) \exp[-\tau / \tau_{\text{dephase}}]$$

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