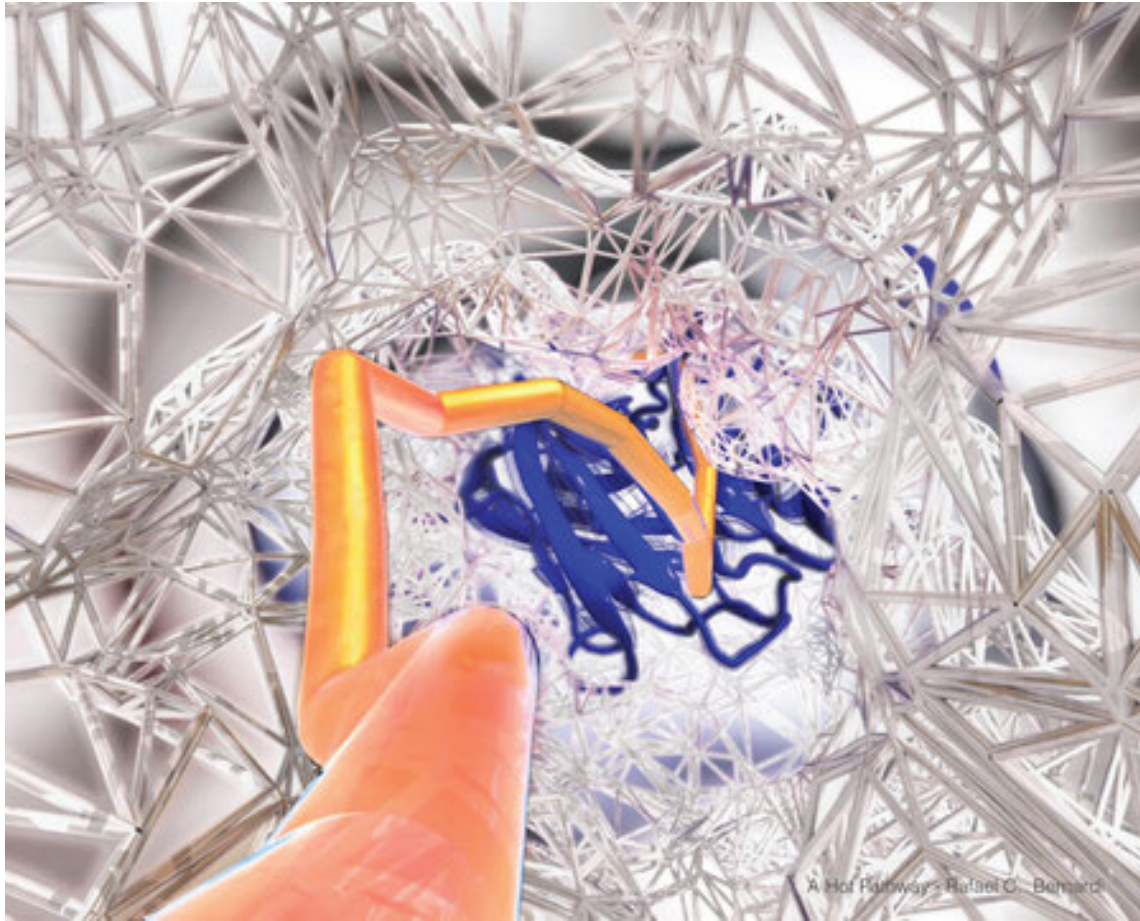


# Hands-on Workshop on Computational Biophysics

May 30 - June 2, 2017  
Pittsburgh Supercomputing Center

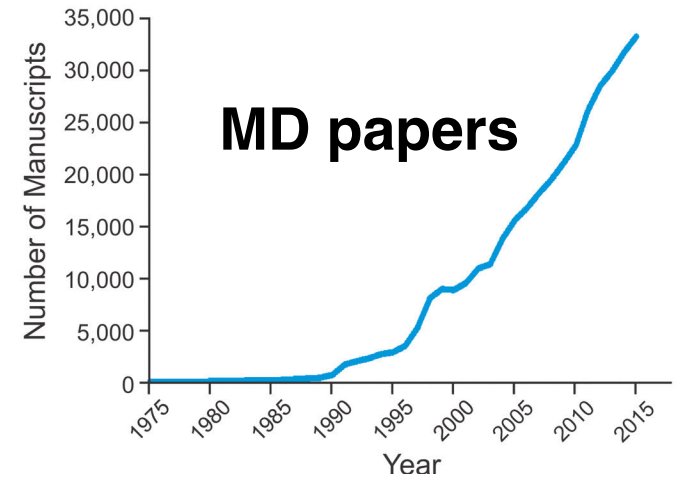


**Emad Tajkhorshid**

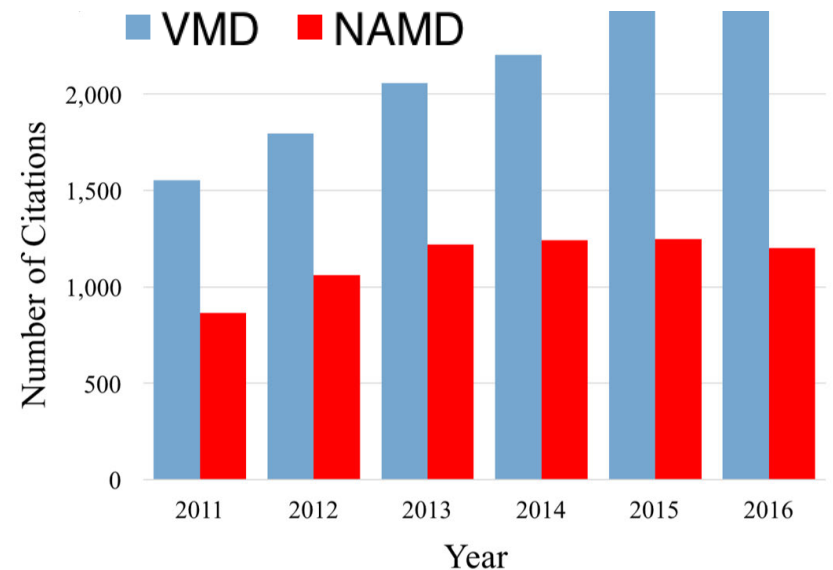
NIH Center for Macromolecular Modeling and Bioinformatics  
Beckman Institute for Advanced Science and Technology  
University of Illinois at Urbana-Champaign

# NIH P41 Center for Macromolecular Modeling and Bioinformatics University of Illinois at Urbana-Champaign

**Serving the large and fast growing community**  
of biomedical researchers employing molecular  
modeling and simulation technologies

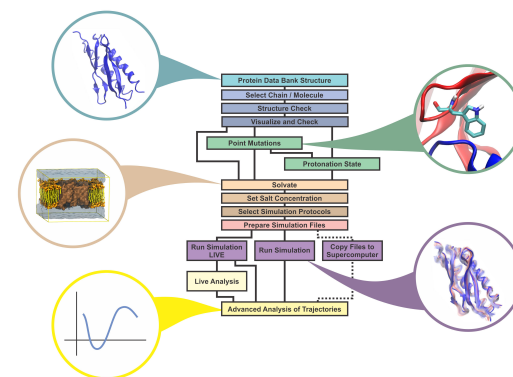
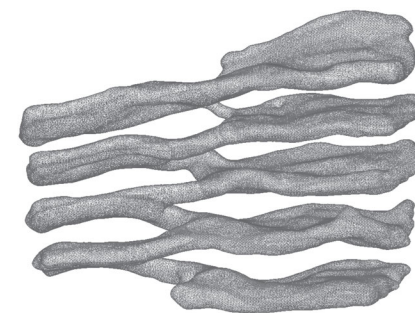


**103,000** VMD users  
**19,000** NAMD users  
**17,000** NIH funded  
**1.4 million** web visitors  
**228,000** tutorial views



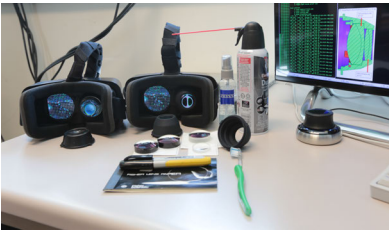
# Serving a Large and Fast Growing Community

- Deploying Center's flagship programs NAMD and VMD on all major computational platforms from commodity computers to supercomputers
- Consistently adding user-requested features
  - simulation, visualization, and analysis
- Covering broad range of scales (orbitals to cells) and data types
- Enhanced software accessibility
  - QwikMD, interactive MDFF, ffTk, simulation in the Cloud, remote visualization



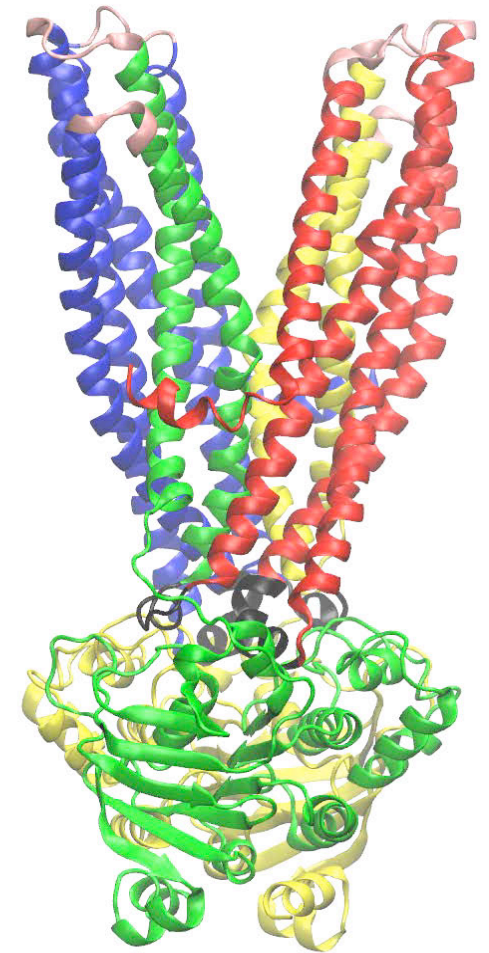
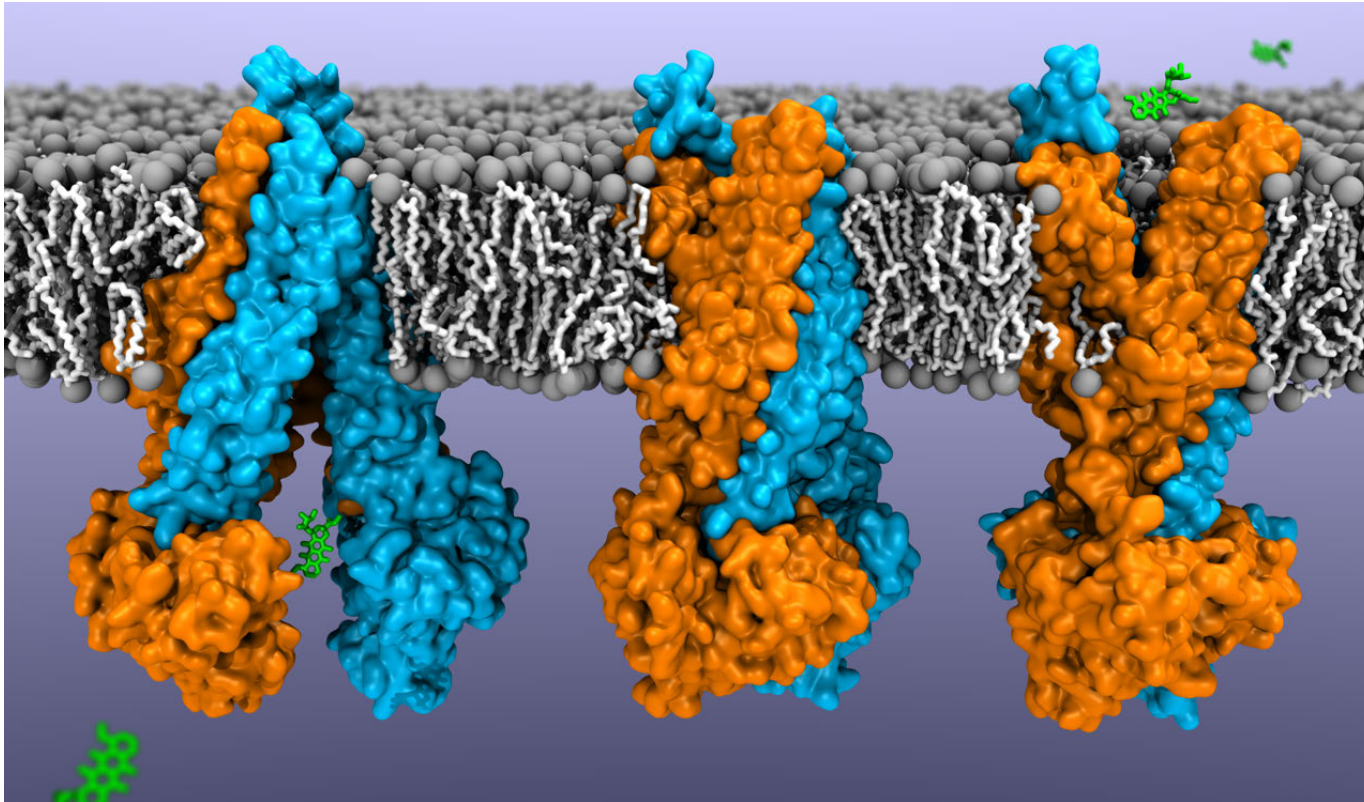
# Exploiting State of the Art Hardware Technology

- Software available and optimized on all national supercomputing platforms (even before they come online)
- Decade-long, highly productive relationship with NVIDIA
- The first CUDA Center of Excellence funded by NVIDIA
- Consistently exploring opportunities for new hardware technology
  - Remote visualization
  - Virtual Reality
  - Handheld devices



# Computational Structural Biology

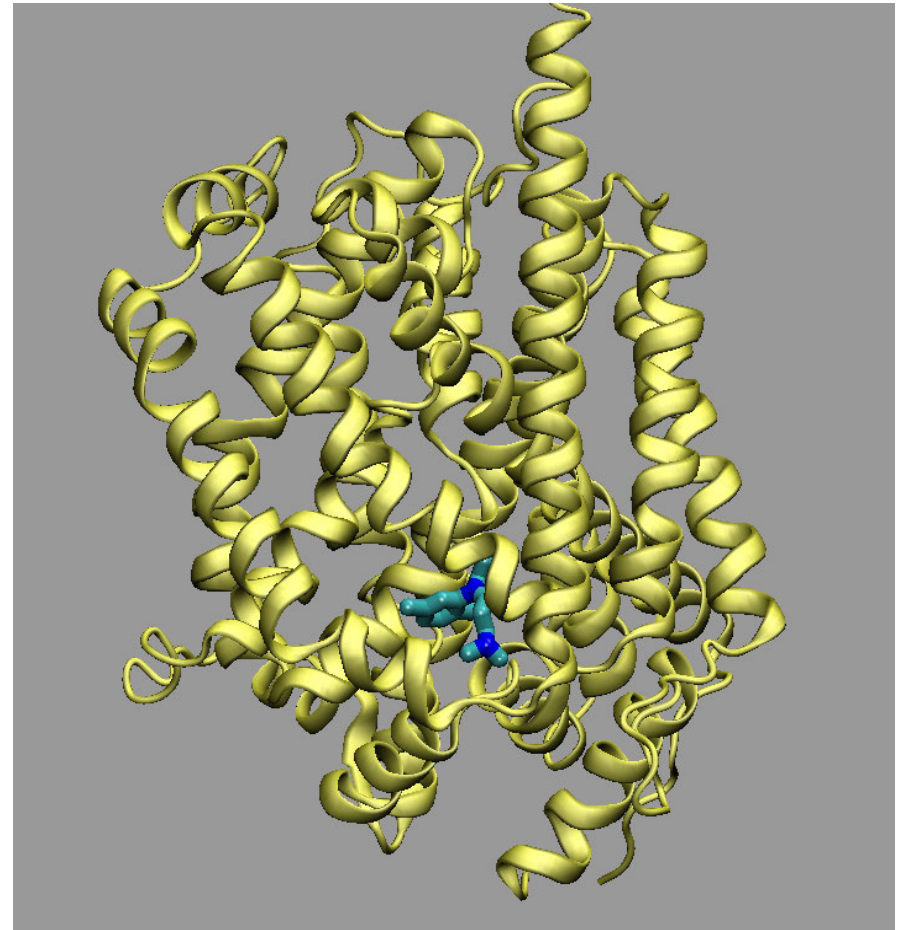
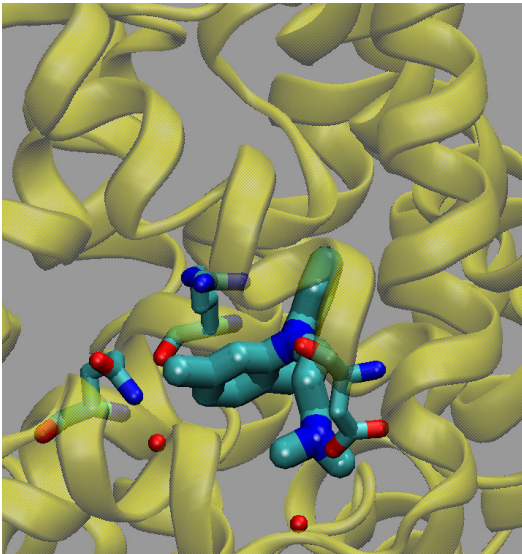
## Describing Biomolecules at Nanoscale



**Structure / Dynamics**  
**@ nanoscale**

# Why Structural Biology at Nanoscale?

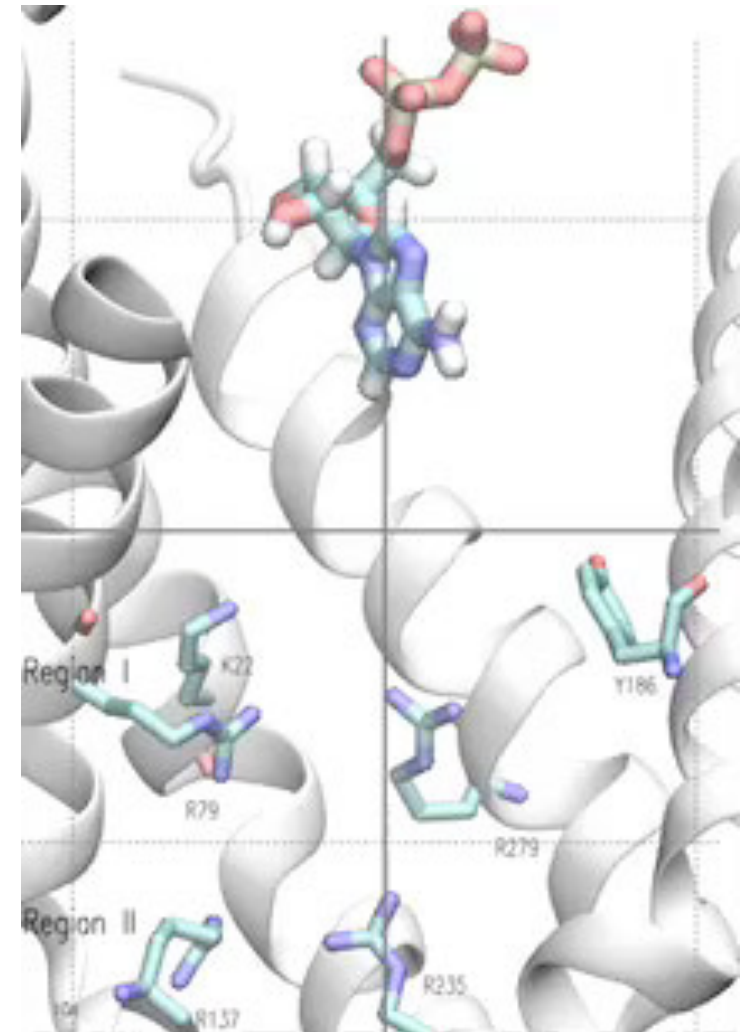
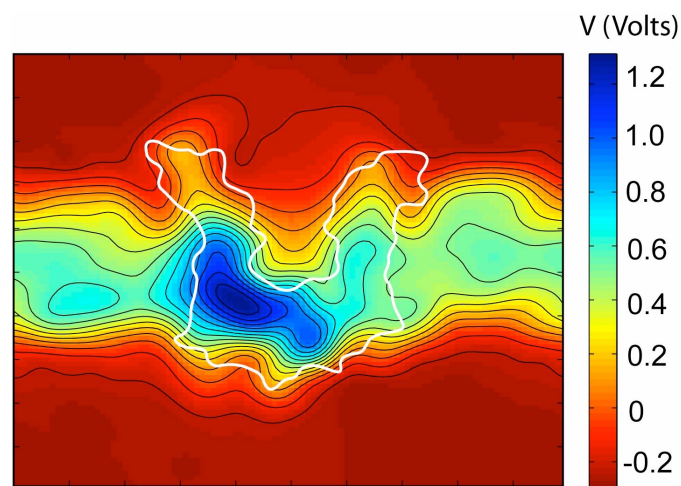
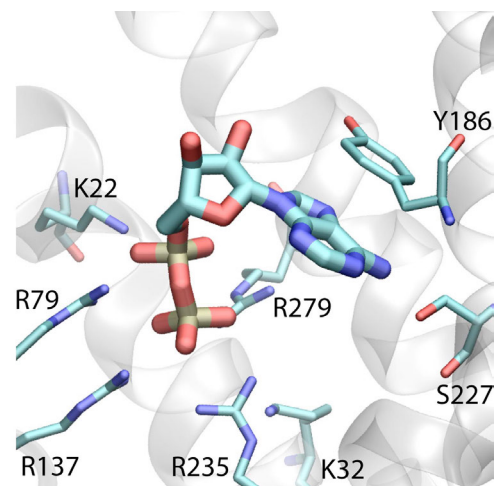
- ◆ Mechanisms in Molecular Biology
- ◆ Molecular Basis of Disease
- ◆ Drug Design
- ◆ Nano-biotechnology



Antidepressant binding site in a neurotransmitter transporter.  
Nature 448: 952-956 (2007)

# Why Structural Biology at **Nanoscale**?

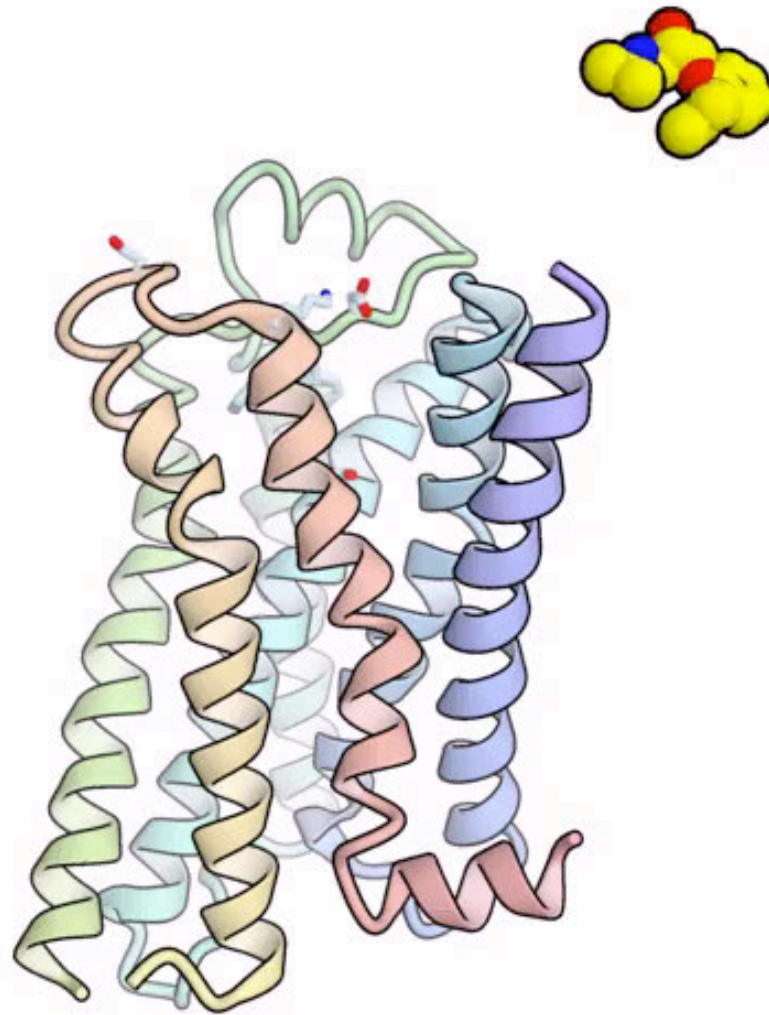
- ◆ Mechanisms in Molecular Biology
- ◆ Molecular Basis of Disease
- ◆ Drug Design
- ◆ Nano-biotechnology



Binding of a small molecule to a binding site  
Y. Wang & E.T. PNAS 2010

# Why Structural Biology at Nanoscale?

0.00 us

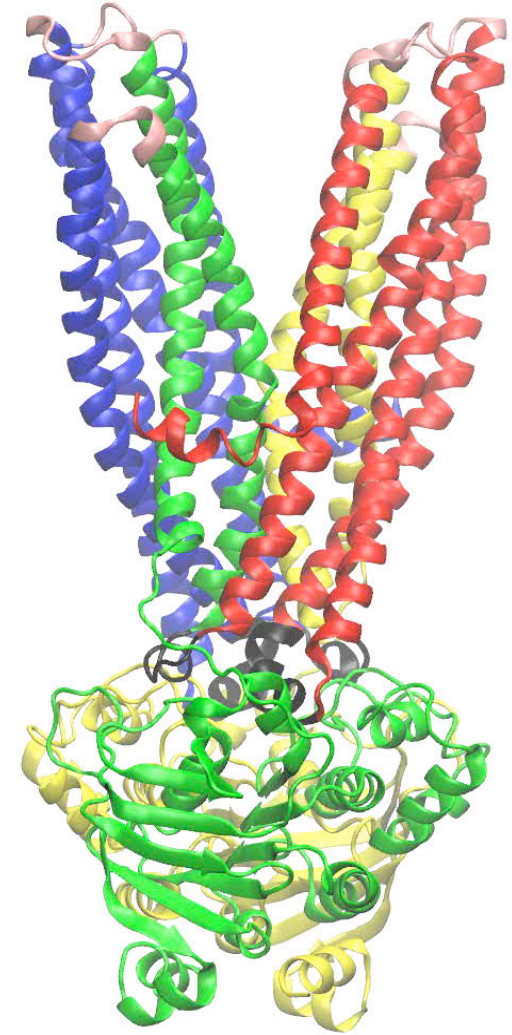


Dror et al., PNAS 2011



# Why Structural Biology at Nanoscale?

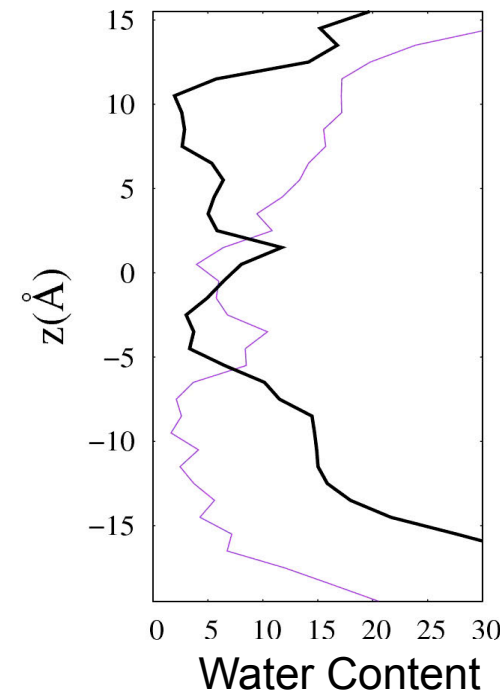
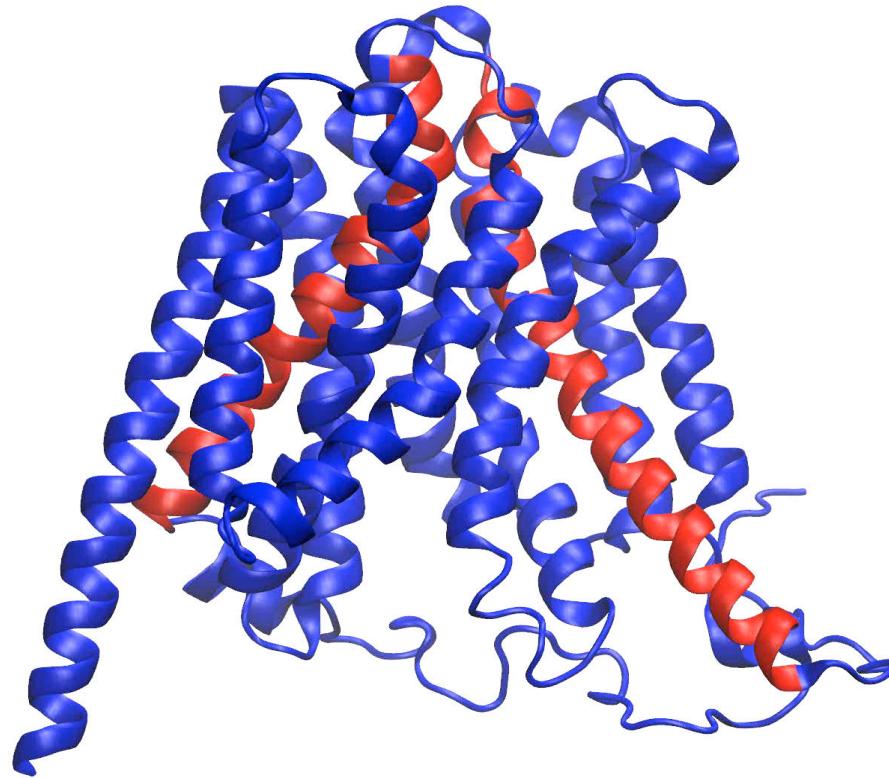
- ◆ Mechanisms in Molecular Biology
- ◆ Molecular Basis of Disease
- ◆ Drug Design
- ◆ Nano-biotechnology



Structural changes underlying function  
M. Moradi & E. T. PNAS 2013

# Why Structural Biology at Nanoscale?

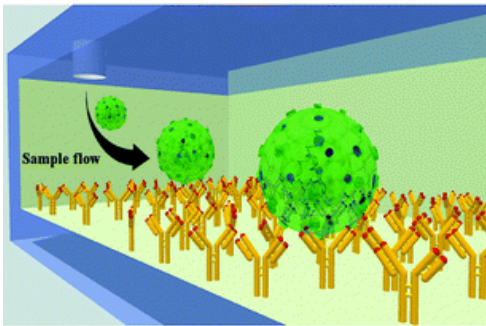
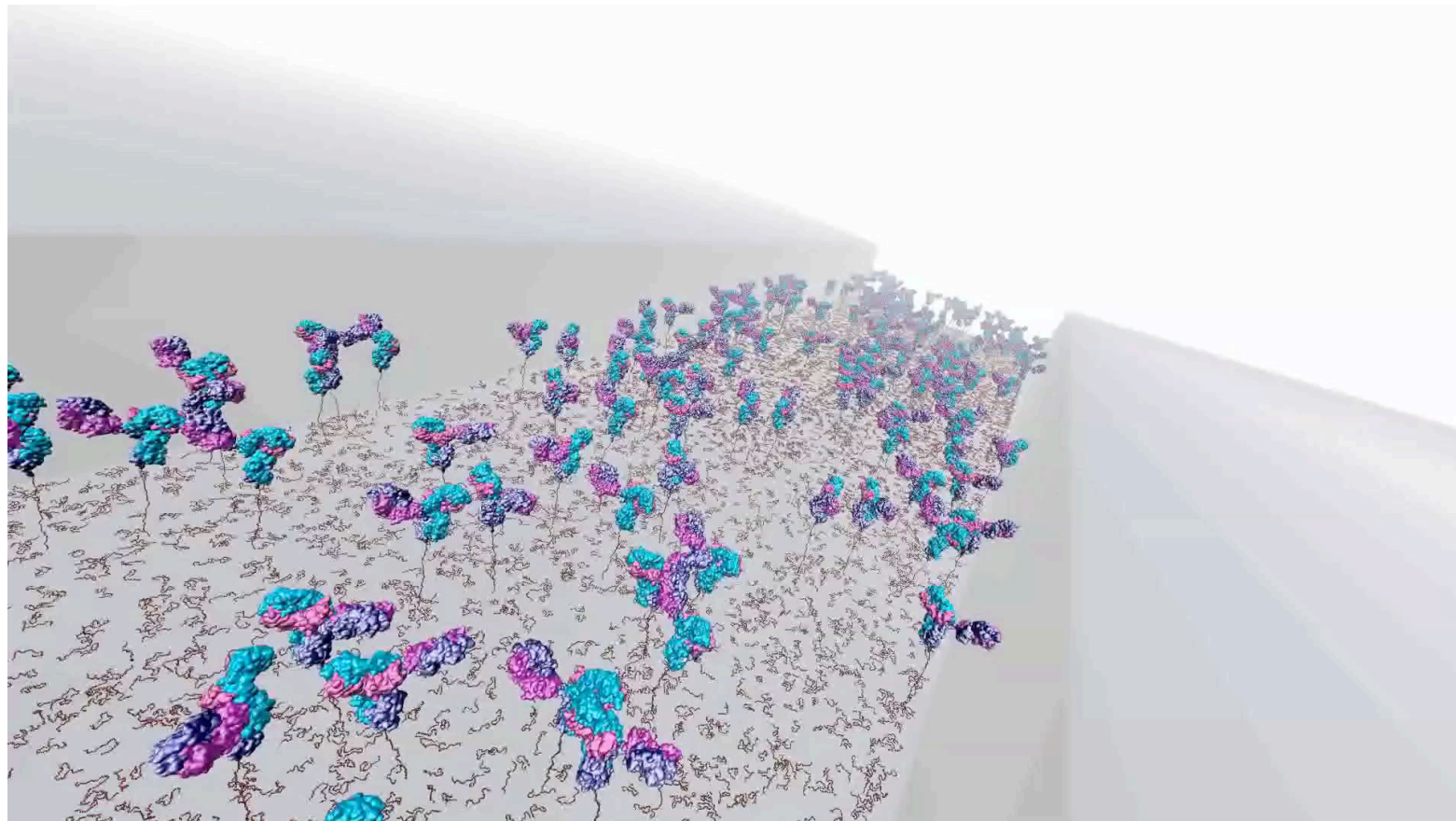
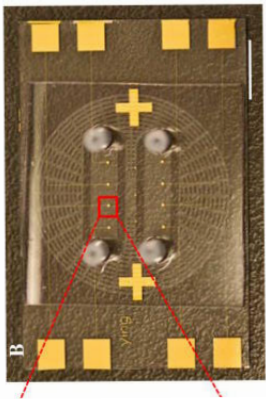
- ◆ Mechanisms in Molecular Biology
- ◆ Molecular Basis of Disease
- ◆ Drug Design
- ◆ Nano-biotechnology



# Nano-biotechnology

## Microfluidic Sensing Devices

Functionalized nanosurface with antibodies



**HIV subtype  
identification**

*Lab Chip 2012*

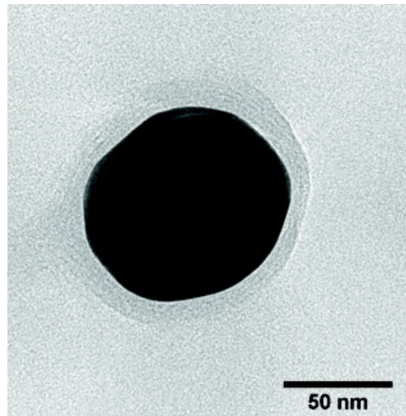
Created by **nanoBIO Node** tools

# Nano-biotechnology

## Gold Nanoparticles as Delivery Vehicles

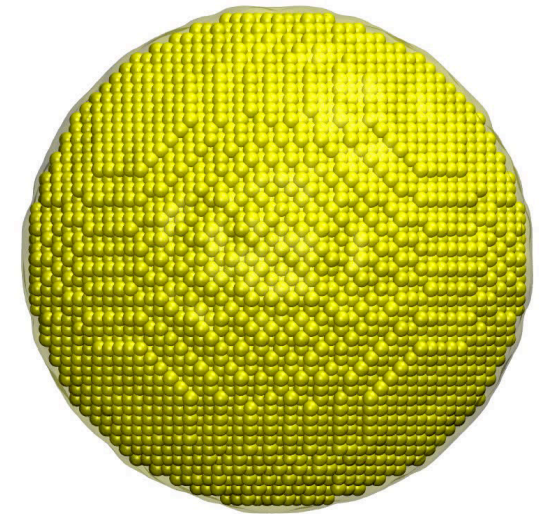
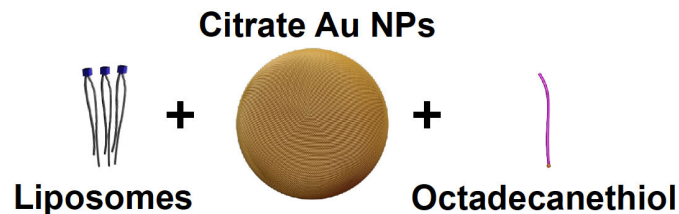
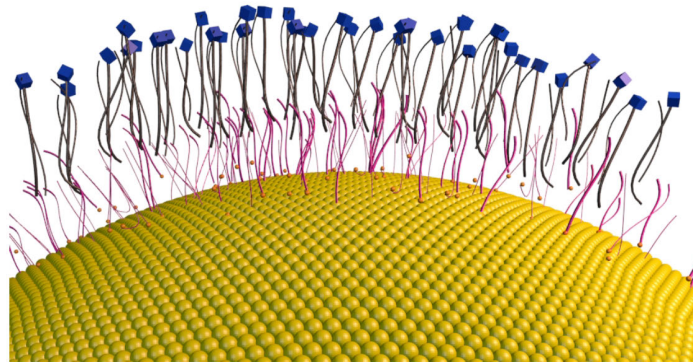
Schematic model with  
no prediction power

Transmission  
Electron Micrograph



Yang, J. A.; Murphy, C. J.  
Langmuir 2012, 28, 5404–  
5416

Cartoon representation of lipid Au NPs



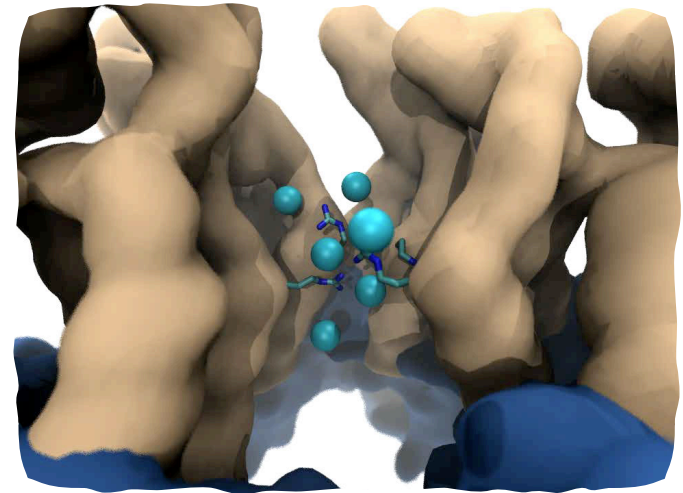
**Experiment:**  
Murphy Lab

**Modeling/Simulation:**  
Tajkhorshid Lab

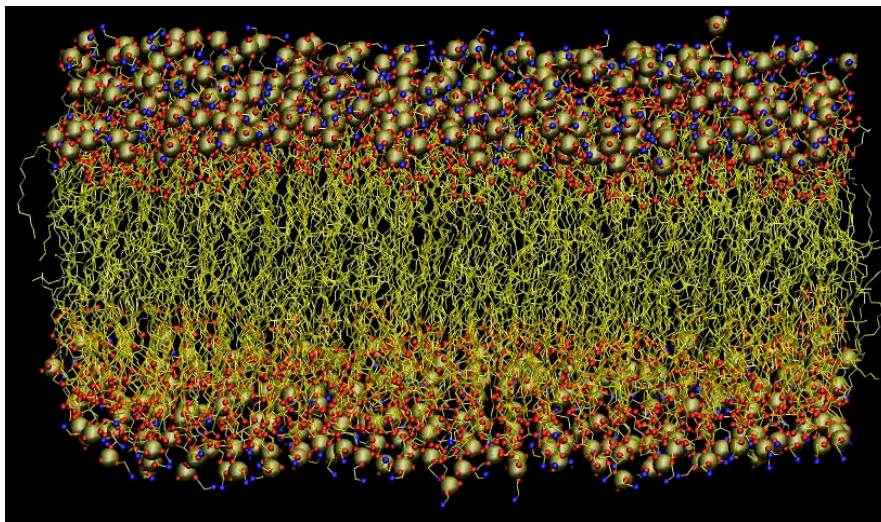
# Applications of Computational Methodologies to Structural Biology

Simulation of the dynamics of the molecular system (MD)

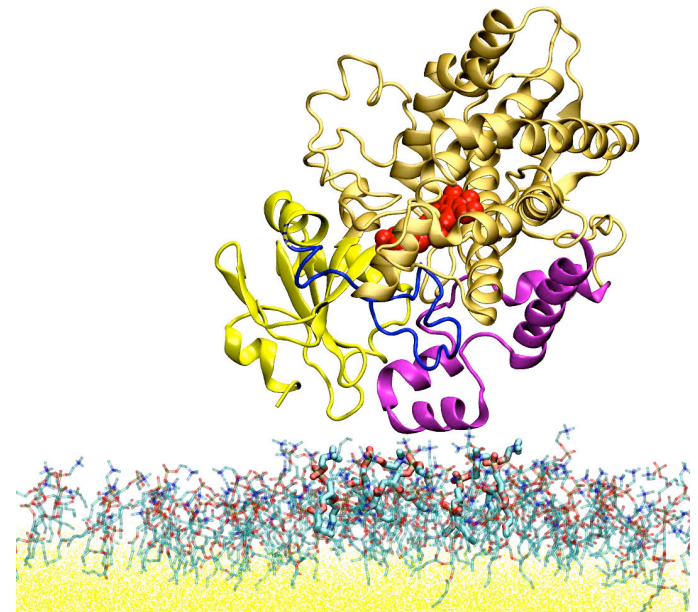
- Calculating ensemble-averaged properties of microscopic systems to compare to macroscopic measurements
- Providing a molecular basis for function
- Describing the molecular/structural changes underlying function
- ...



Hydration at the interface of viral shell proteins

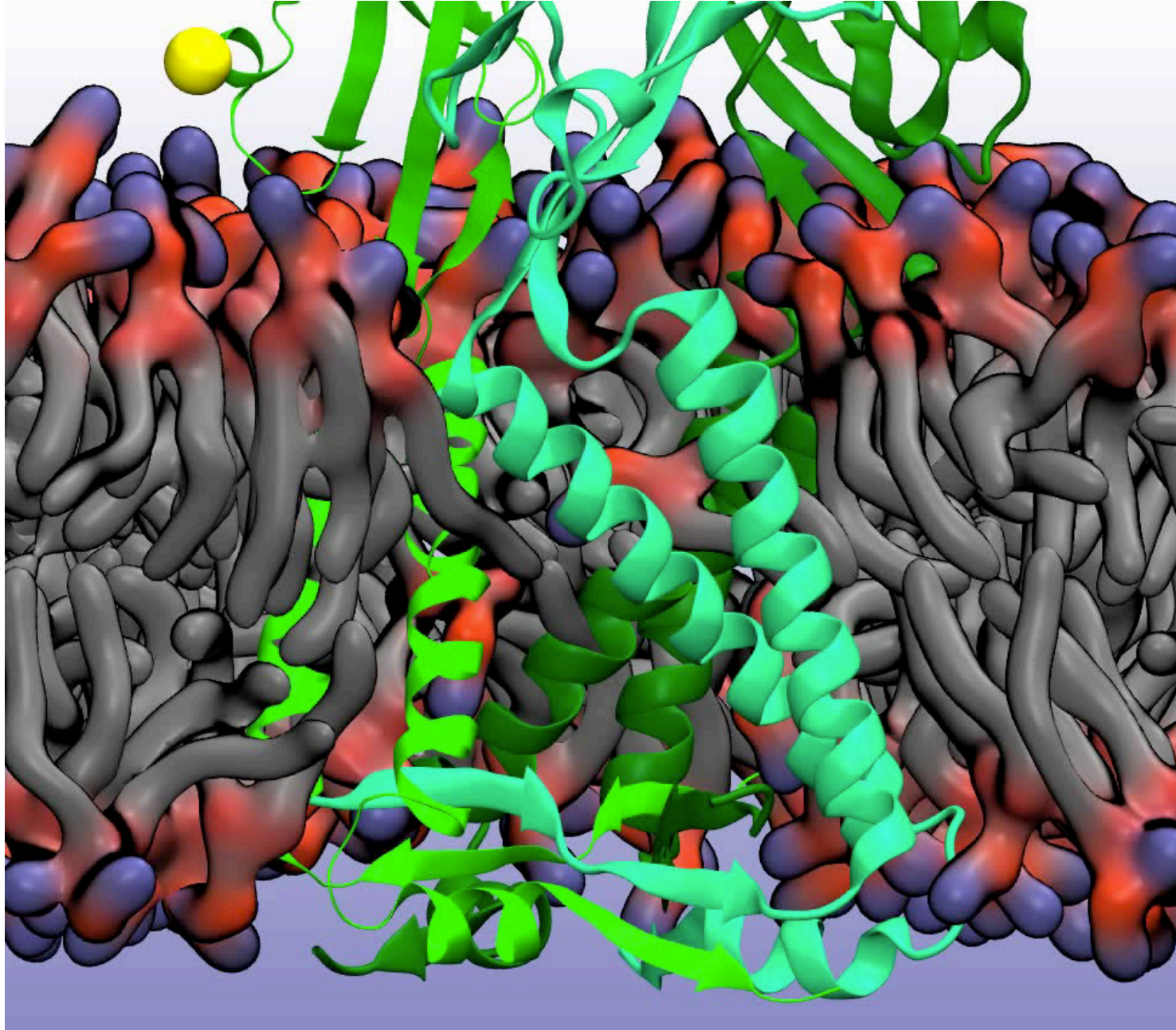


Thermal fluctuations of a phospholipid bilayer

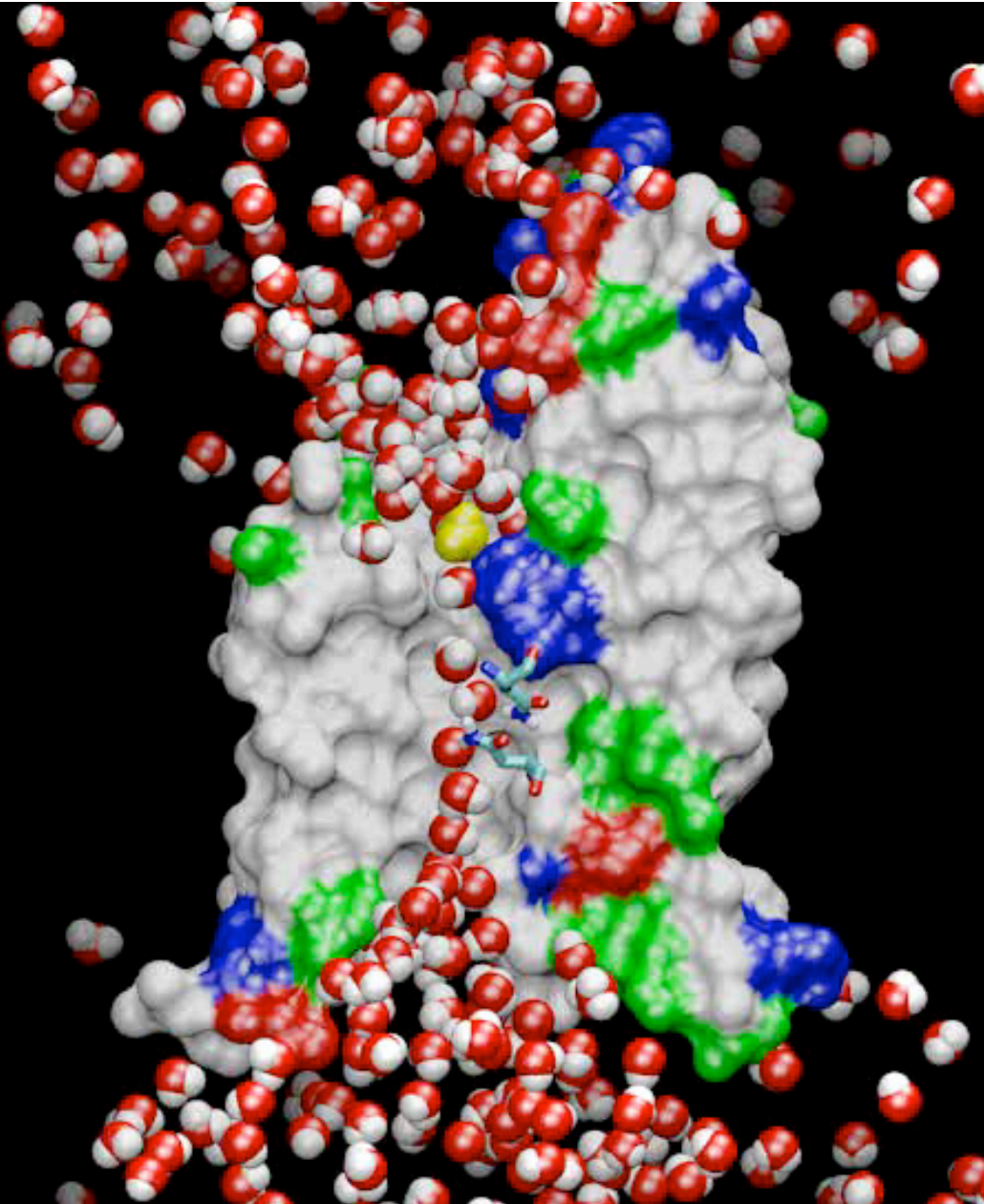


Membrane binding of a coagulation protein

# Lipid Protein Interaction



# Molecular Dynamics Simulations



Solving the Newtonian equations of motion for all particles at every time step

Major limitations:

- Time scale / sampling
- Force field approximations

Major advantage:

- Unparalleled spatial and temporal resolutions, simultaneously

**SPEED  
LIMIT**

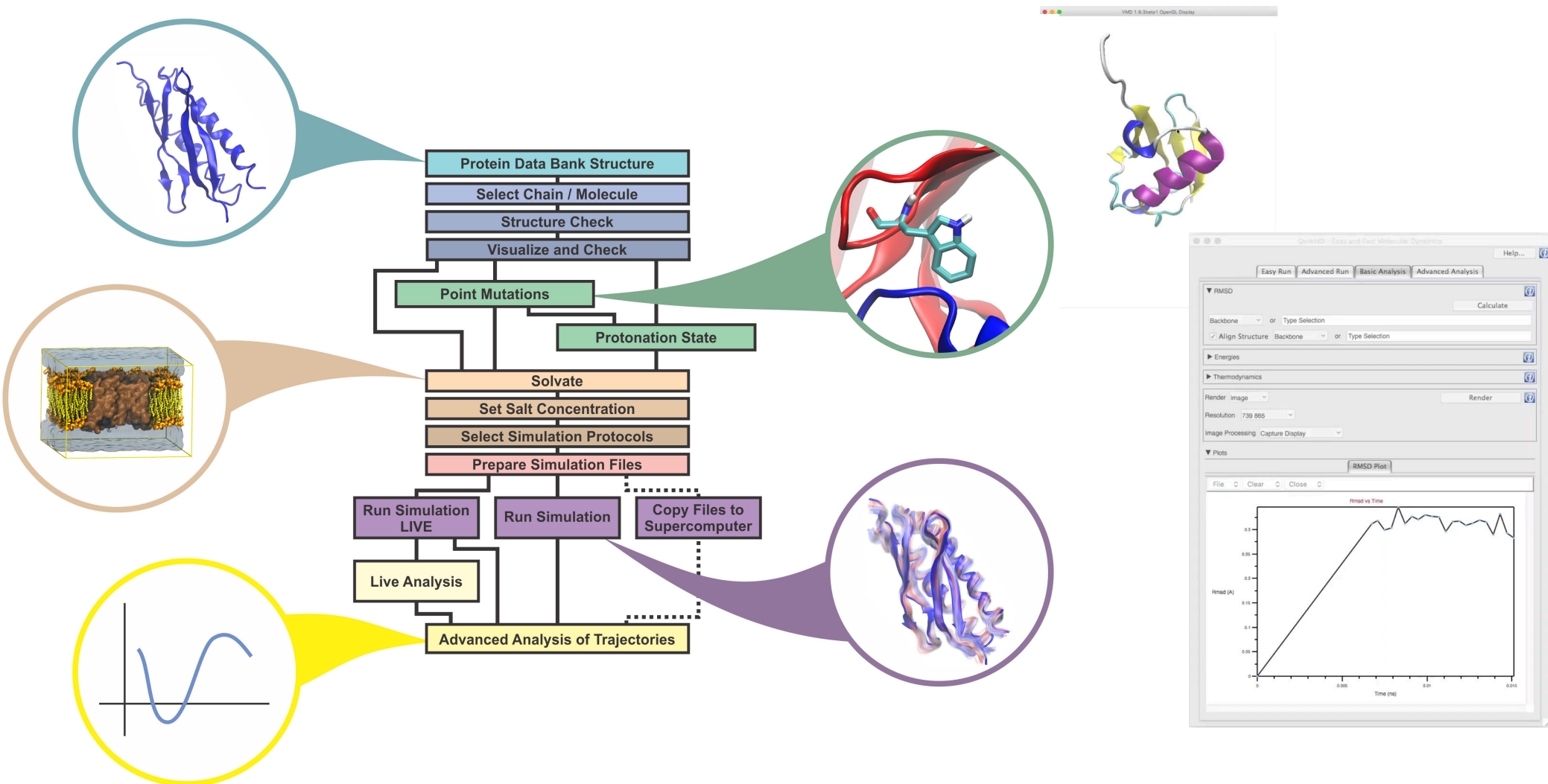
**1 fs**

# Steps in a Typical MD Simulation

- 1. Prepare molecule
  - Read in pdb and psf file
- 2. Minimization
  - Reconcile observed structure with force field used ( $T = 0$ )
- 3. Heating
  - Raise temperature of the system
- 4. Equilibration
  - Ensure system is stable
- 5. Dynamics
  - Simulate under desired conditions (NVE, NpT, etc)
  - Collect your data
- 6. Analysis
  - Evaluate observables (macroscopic level properties)
  - Or relate to single molecule experiments



# QwikMD- Gateway to Easy Simulation



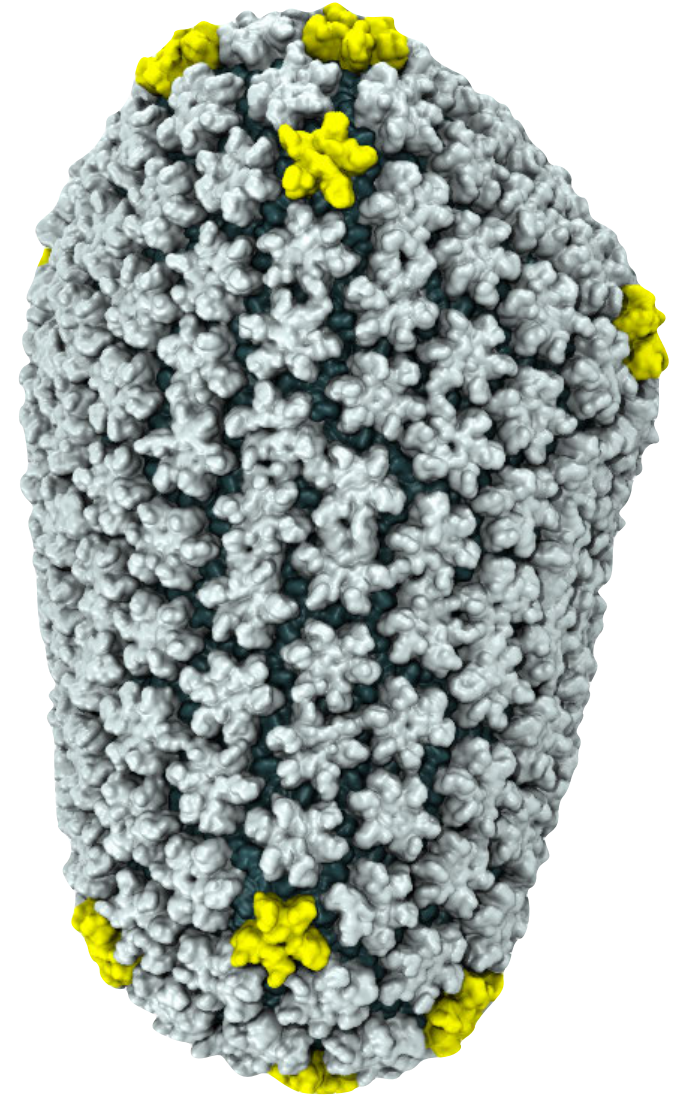
Ribeiro, J. V., ..., Schulten, K.. QwikMD — Integrative Molecular Dynamics Toolkit for Novices and Experts. *Sci. Rep.* 6, 26536; doi: 10.1038/srep26536 (2016)

# Applications of Computational Methodologies to Cell-Scale Structural Biology

## Using computational methods as “structure-building” tools

All experimental Structural biological approaches heavily rely on computational methods to analyze their data

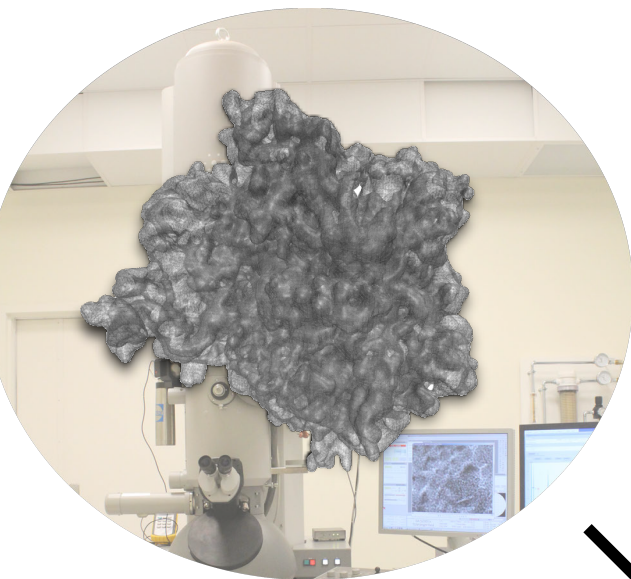
- NMR
- X-ray
- Electron Microscopy
- ...



Structural model of HIV virus

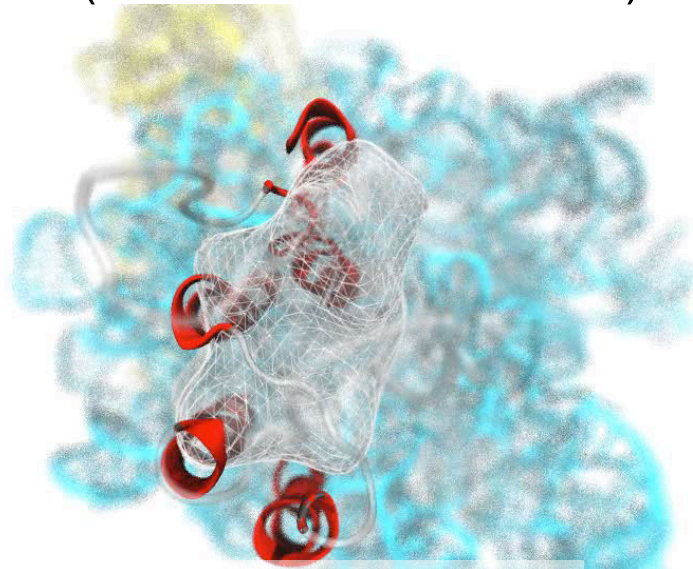
# Molecular Dynamics Flexible Fitting (MDFF)

Electron  
Microscope



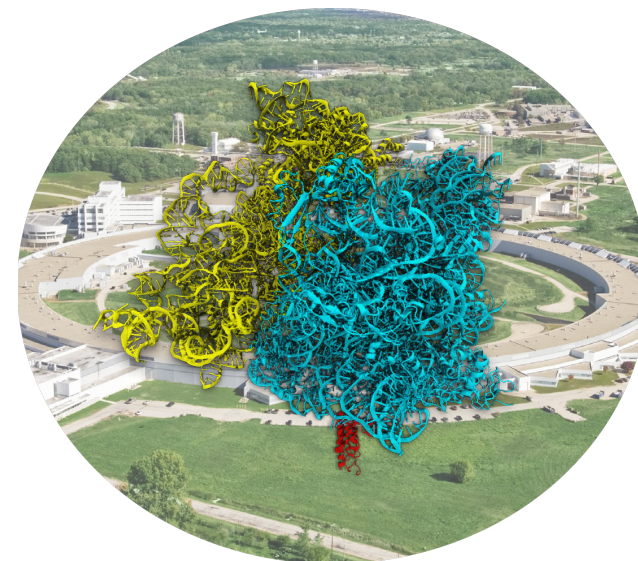
cryo-EM density  
map

(Ribosome-bound YidC)

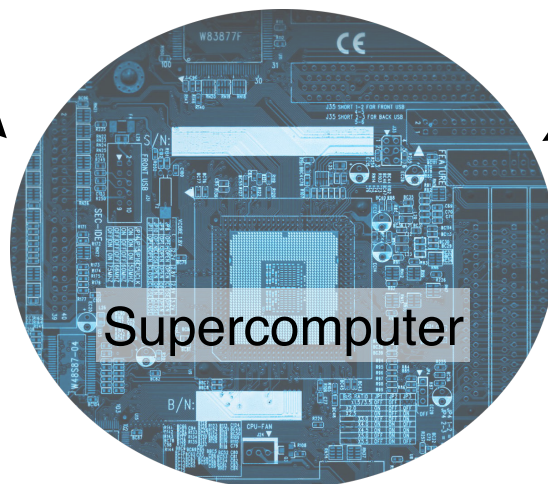


Match through MD

APS  
Synchrotron



crystallographic  
structure



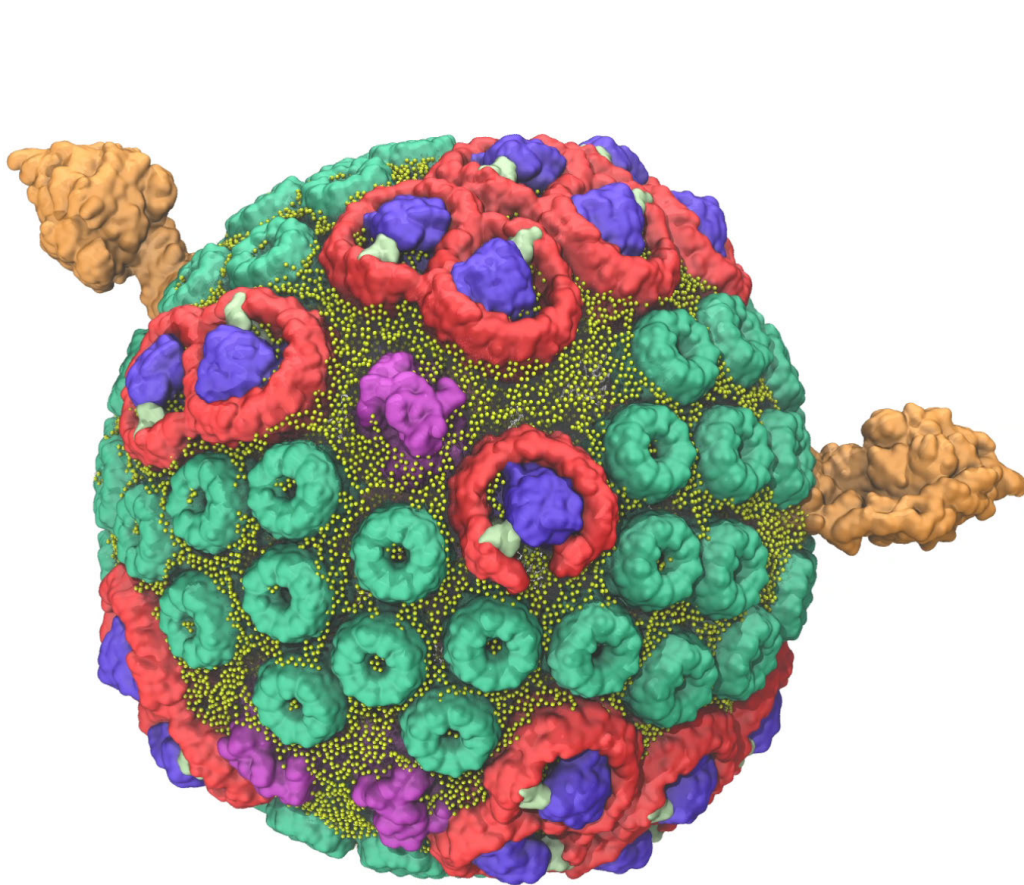
Supercomputer

[1] Trabuco et al. *Structure* (2008) 16:673-683.

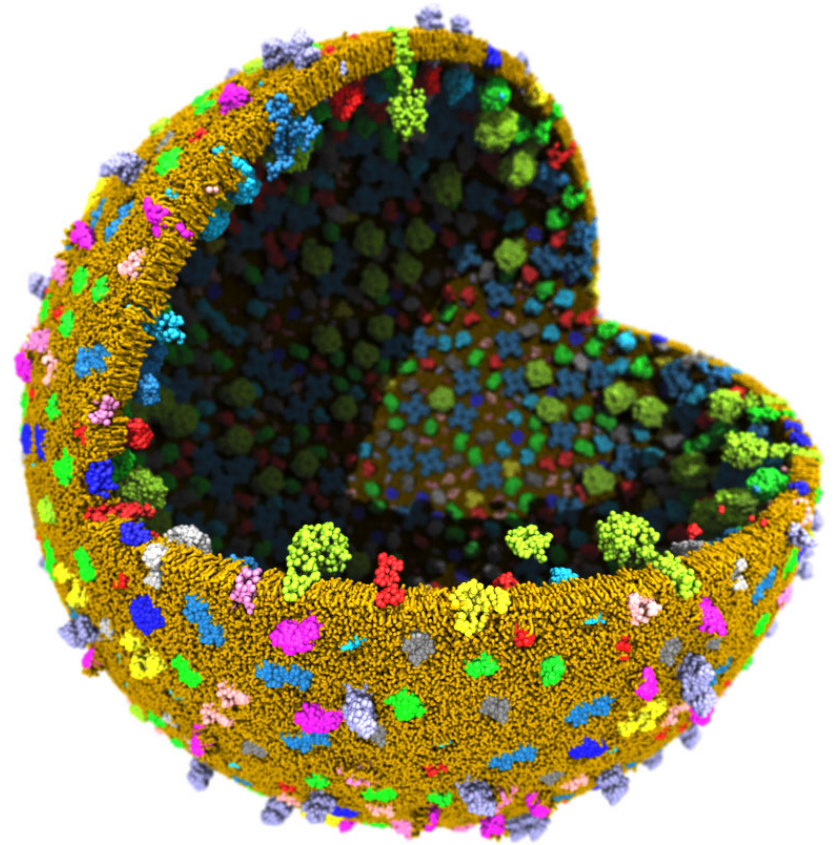
[2] Trabuco et al. *Methods* (2009) 49:174-180.

# Applications of Computational Methodologies to Cell-Scale Structural Biology

Using simulations as a “structure-building” tool



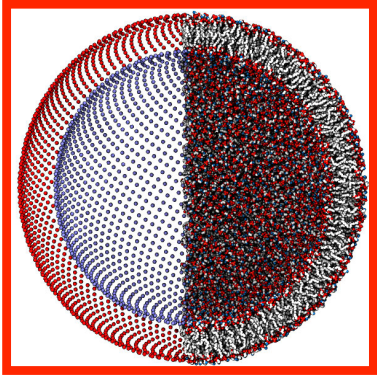
The most detailed model of a chromatophore



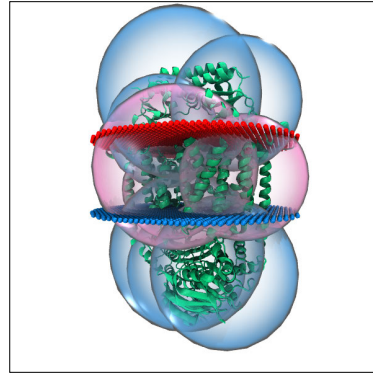
Computational model of a minimal cell envelope

# Automated Protein Embedding into Complex Membrane Structures

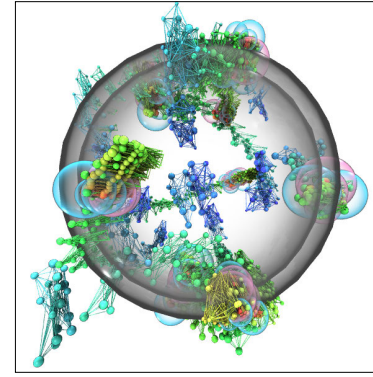
Vesicle Construction



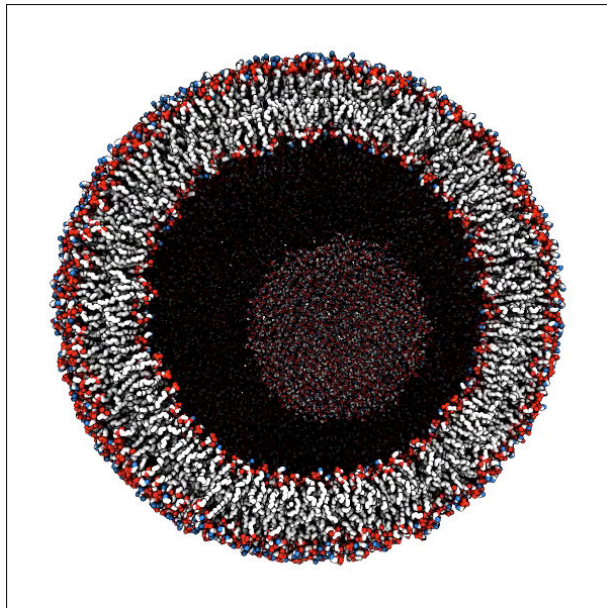
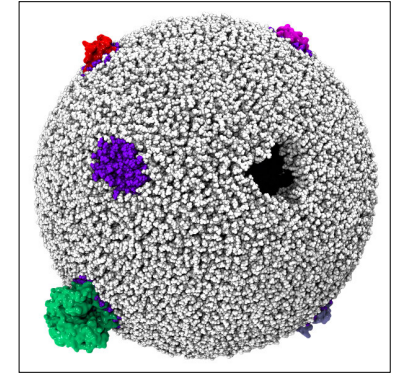
Coarse Grain Protein



CG Protein Placement



Combine Lipid + Protein



## Distribution of proteins across the membrane surface (dense environment)

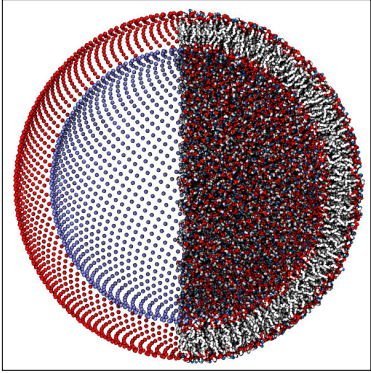
- Ability to handle a variety of protein geometries
- Proper orientation of proteins in relation to the membrane surface
- Generalizable and automated method for membranes of arbitrary shape

## Embedding proteins into the membrane

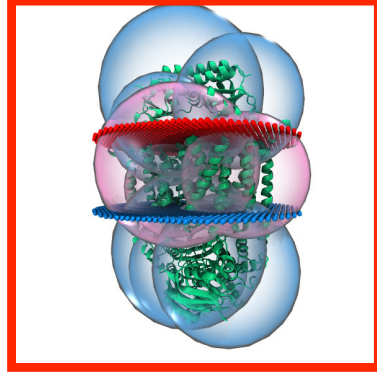
- Account for surface area occupied by proteins in inner and outer leaflets
- Proper lipid packing around embedded proteins

# Automated Protein Embedding into Complex Membrane Structures

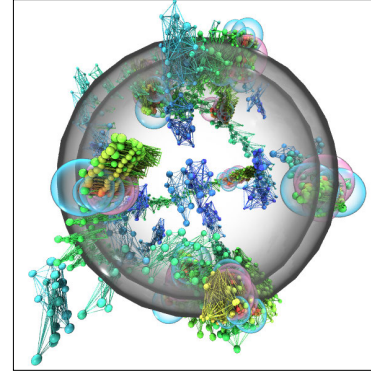
Vesicle Construction



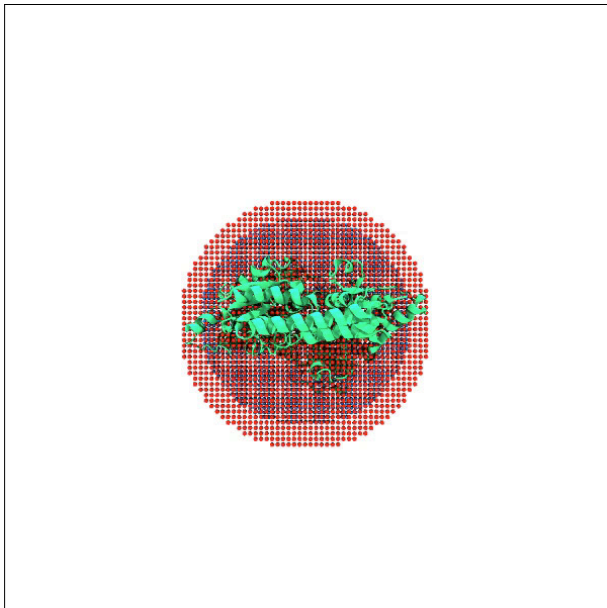
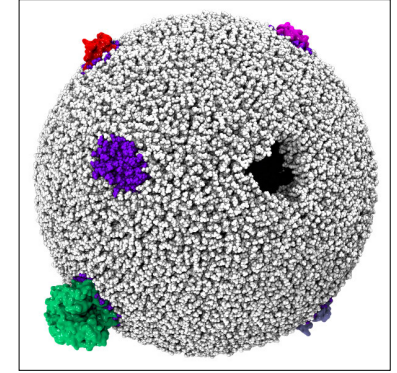
Coarse Grain Protein



CG Protein Placement



Combine Lipid + Protein



## Distribution of proteins across the membrane surface (dense environment)

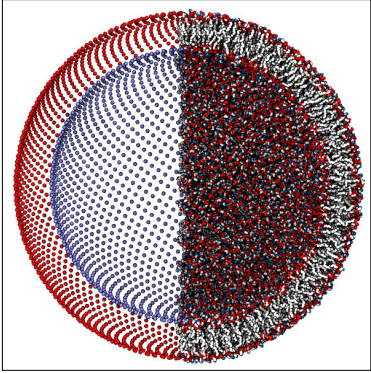
- Ability to handle a variety of protein geometries
- Proper orientation of proteins in relation to the membrane surface
- Generalizable and automated method for membranes of arbitrary shape

## Embedding proteins into the membrane

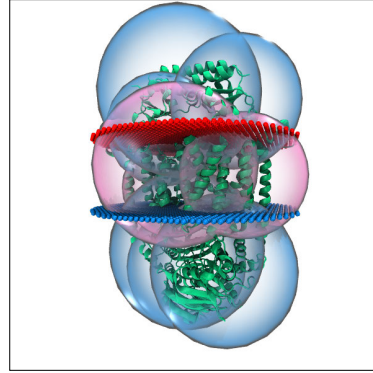
- Account for surface area occupied by proteins in inner and outer leaflets
- Proper lipid packing around embedded proteins

# Automated Protein Embedding into Complex Membrane Structures

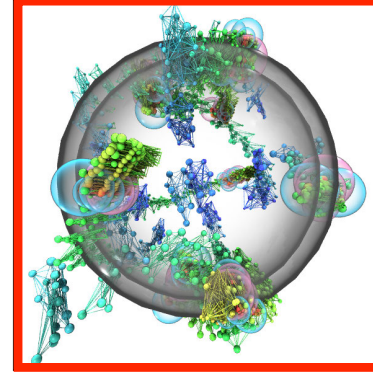
Vesicle Construction



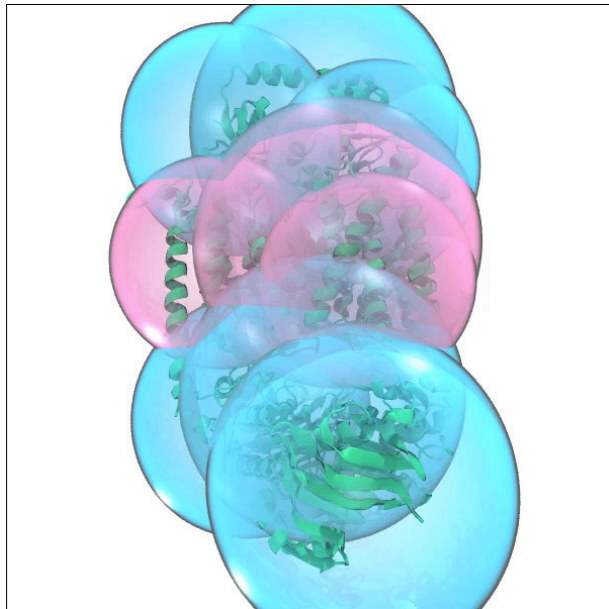
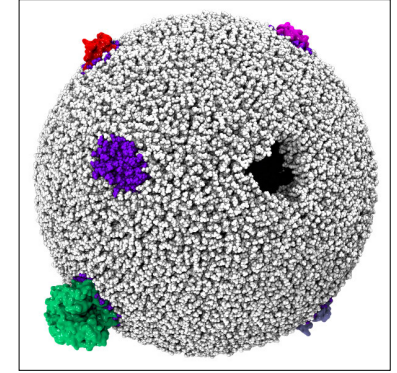
Coarse Grain Protein



CG Protein Placement



Combine Lipid + Protein



## Distribution of proteins across the membrane surface (dense environment)

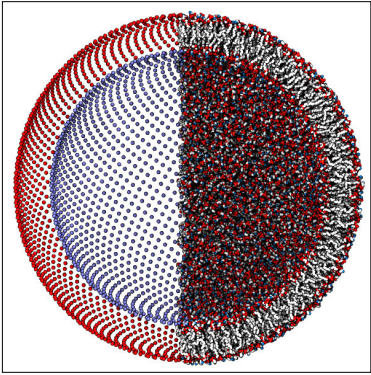
- Ability to handle a variety of protein geometries
- Proper orientation of proteins in relation to the membrane surface
- Generalizable and automated method for membranes of arbitrary shape

## Embedding proteins into the membrane

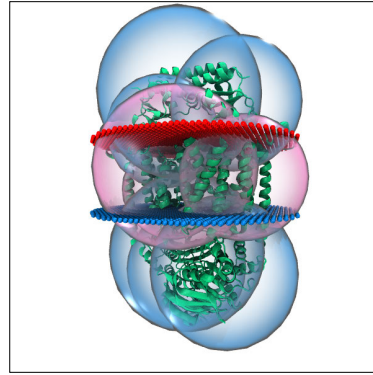
- Account for surface area occupied by proteins in inner and outer leaflets
- Proper lipid packing around embedded proteins

# Automated Protein Embedding into Complex Membrane Structures

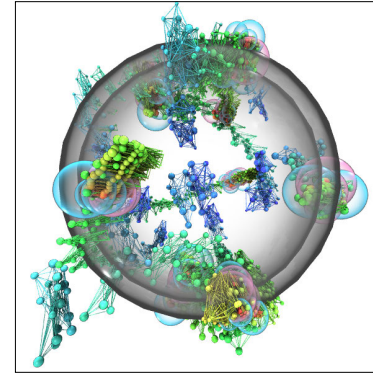
Vesicle Construction



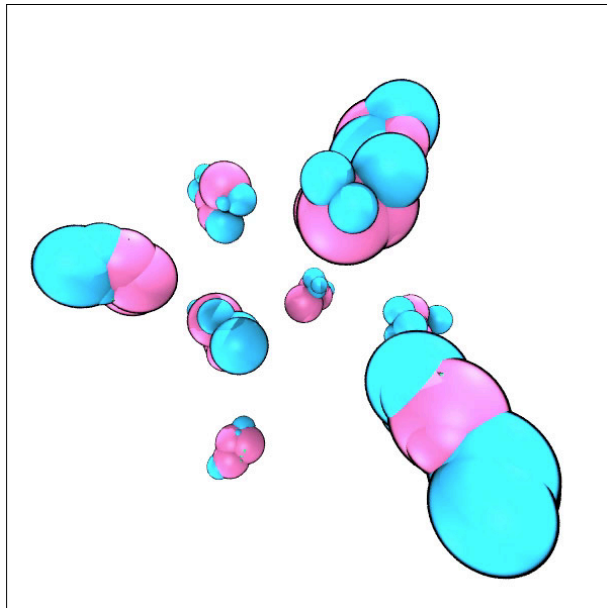
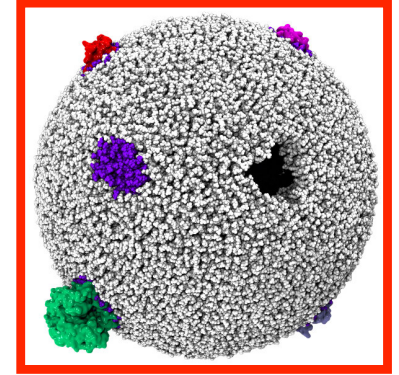
Coarse Grain Protein



CG Protein Placement



Combine Lipid + Protein



## Distribution of proteins across the membrane surface (dense environment)

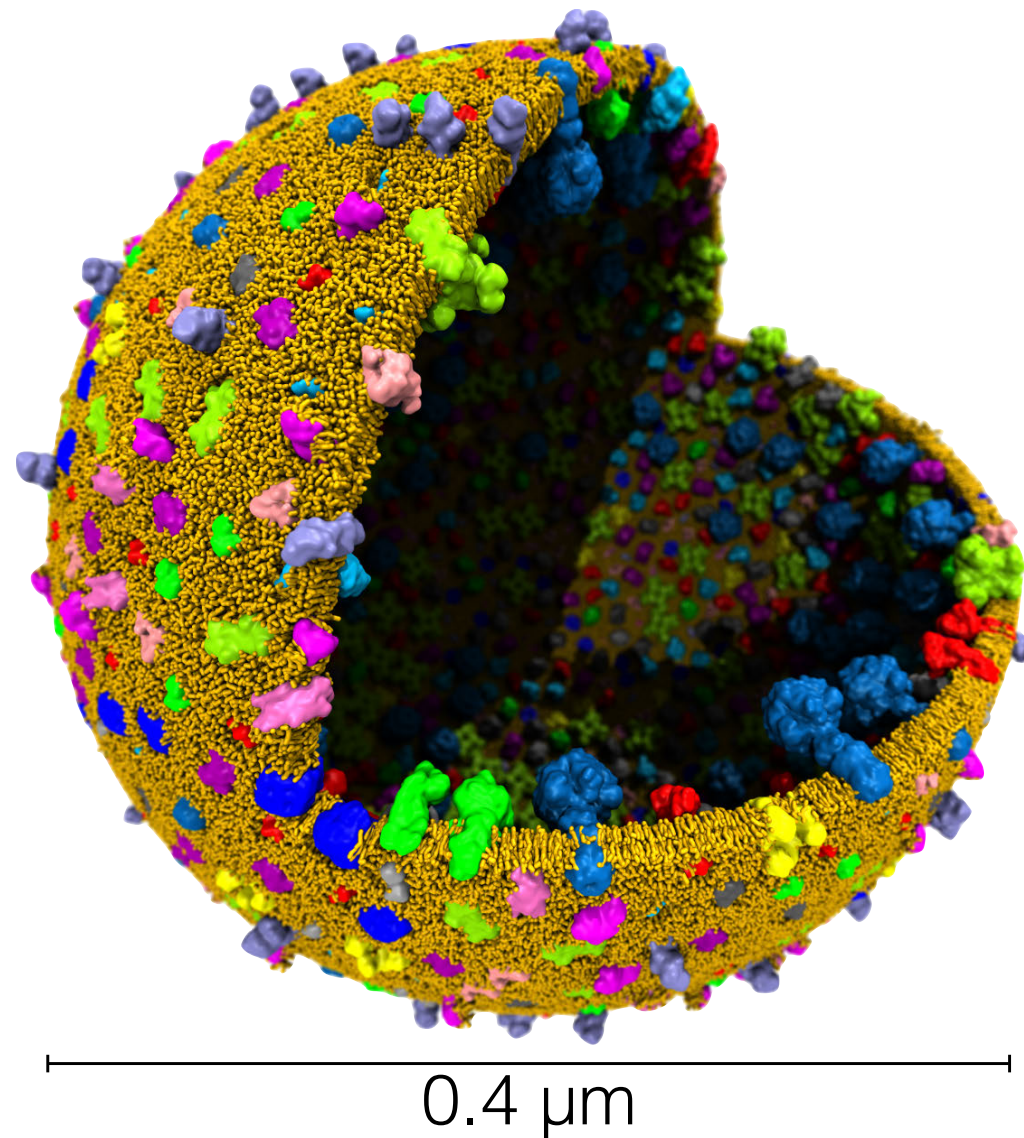
- Ability to handle a variety of protein geometries
- Proper orientation of proteins in relation to the membrane surface
- Generalizable and automated method for membranes of arbitrary shape

## Embedding proteins into the membrane

- Account for surface area occupied by proteins in inner and outer leaflets
- Proper lipid packing around embedded proteins



**113 million** Martini particles  
representing **1 billion** atoms



<u>Protein Components</u>	<u>Copy #</u>
● Aquaporin Z	97
● Copper Transporter (CopA)	166
● F1 ATPase	63
● Lipid Flipase (MsbA)	29
● Molybdenum transporter (ModBC)	130
● Translocon (SecY)	103
● Methionine transporter (MetNI)	136
● Membrane chaperon (YidC)	126
● Energy coupling factor (ECF)	117
● Potassium transporter (KtrAB)	148
● Glutamate transporter (Glt <sub>TK</sub> )	41
● Cytidine-Diphosphate diacylglycerol (Cds)	50
● Membrane-bound protease (PCAT)	57
● Folate transporter (FolT)	134
	<u>1,397</u>

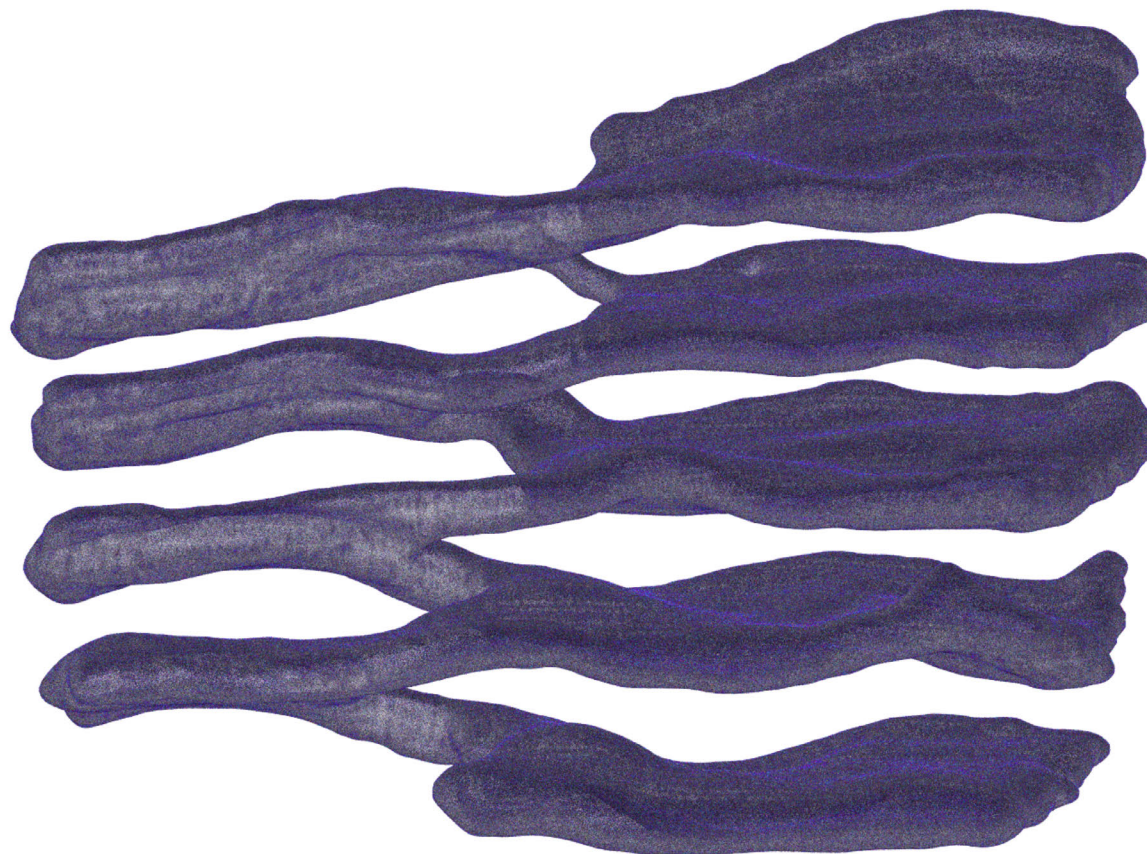
3.7 M lipids (DPPC), 2.4 M Na<sup>+</sup> & Cl<sup>-</sup> ions,  
104 M water particles (4 H<sub>2</sub>O / particle)

# Applications of Computational Methodologies to Cell-Scale Structural Biology

Guided Construction of Membranes from Experimental Data

**Ex**perimentally-Derived **M**embrane of **A**rbitrary **S**hape Builder

Terasaki Ramp  
~4 Billion Atoms



~1.59 $\mu$ m

— Outer Leaflet

— Inner Leaflet

— Cholesterol

● POPC

● POPE

● POPI

● POPS

● Sphingomyelin

● Cardiolipin

Terasaki et al., *Cell*, **2013**.

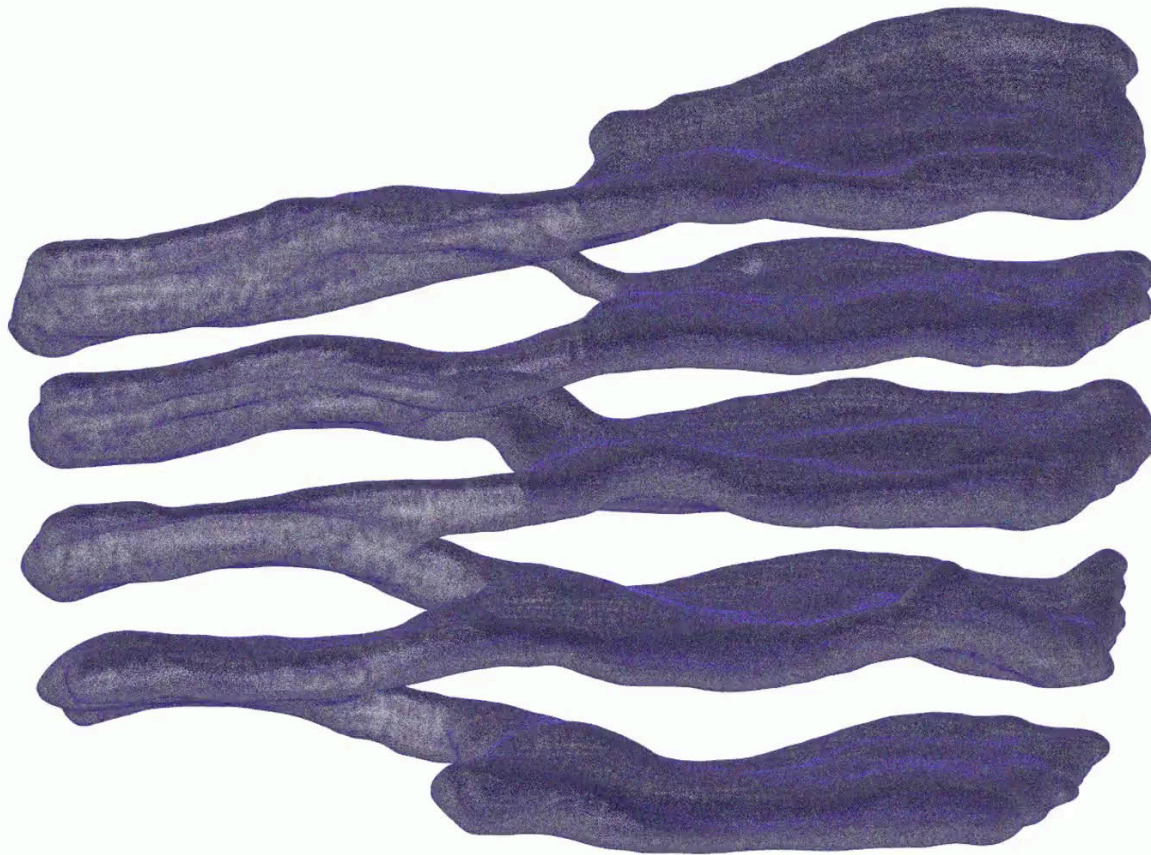
Keenan and Huang, *J. Dairy Sci.*, **1972**.

# Applications of Computational Methodologies to Cell-Scale Structural Biology

## Guided Construction of Membranes from Experimental Data

### Experimentally-Derived Membrane of Arbitrary Shape Builder

Terasaki Ramp  
~4 Billion Atoms



— Outer Leaflet

— Inner Leaflet

— Cholesterol

● POPC

● POPE

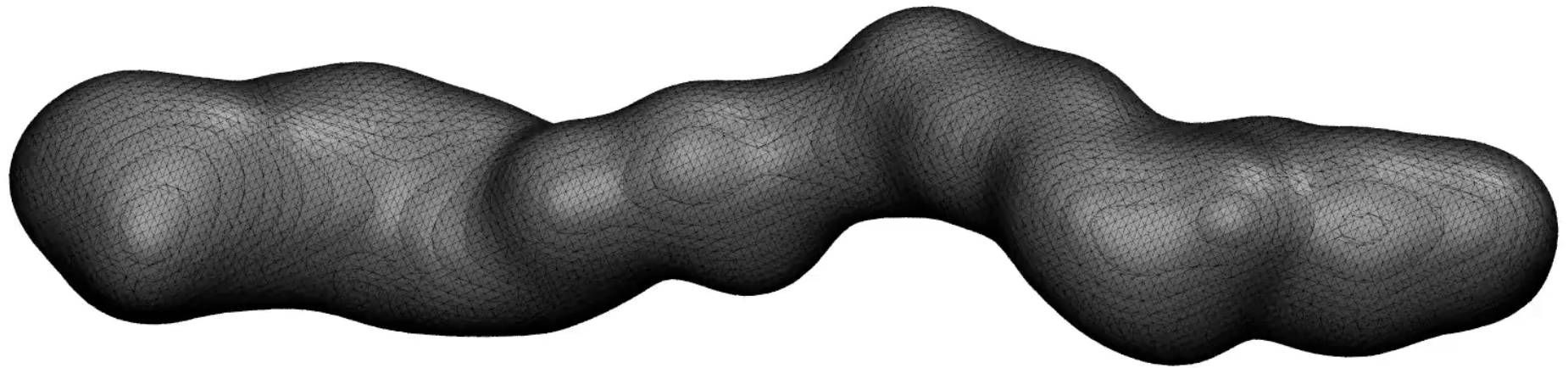
● POPI

● POPS

● Sphingomyelin

● Cardiolipin

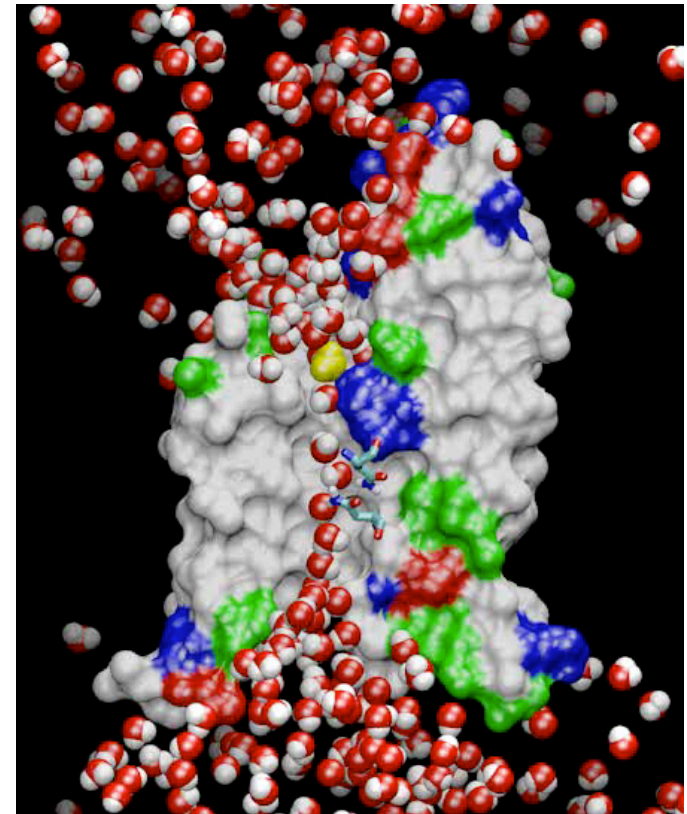
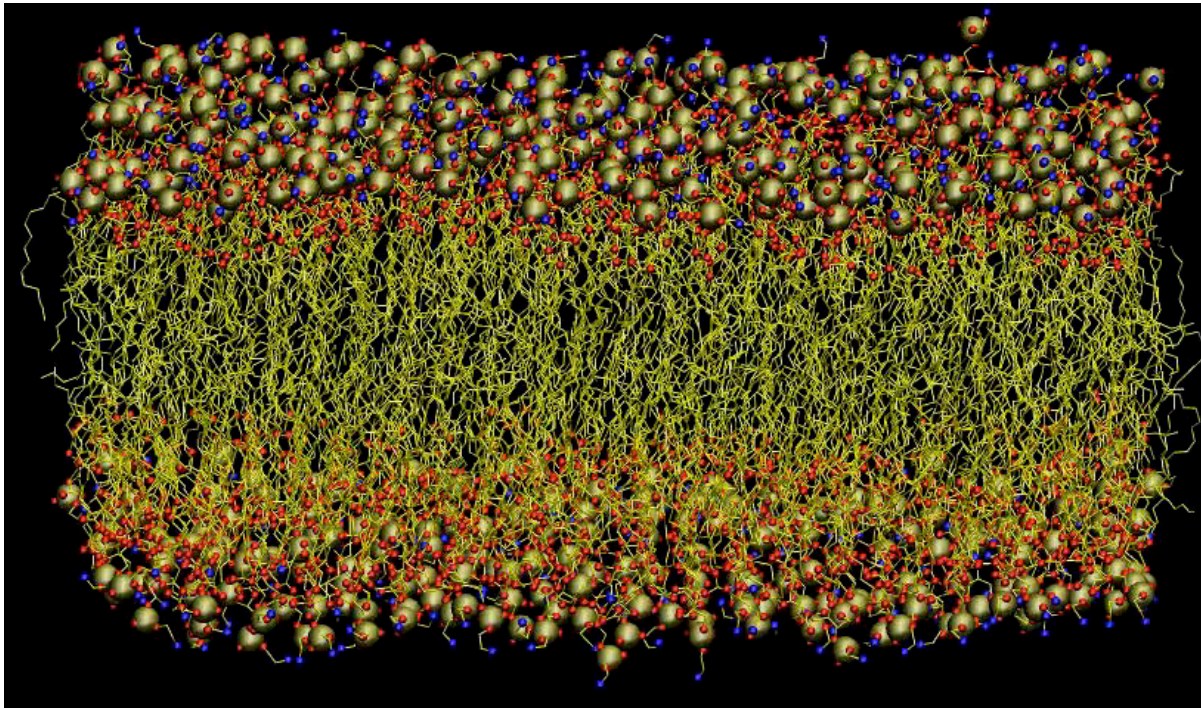
Experimentally-Derived **M**embrane of **A**rbitrary **S**hape Builder  
**xMAS Builder**



Obtain 3D mesh from an  
experimental technique

# Molecular Dynamics Simulation

- Generating a thermodynamic ensemble (Sampling / Statistic)
- Taking into account fluctuations/dynamics in interpretation of experimental observables
- Describing molecular processes + free energy
- Help with molecular modeling



# Classical Molecular Dynamics

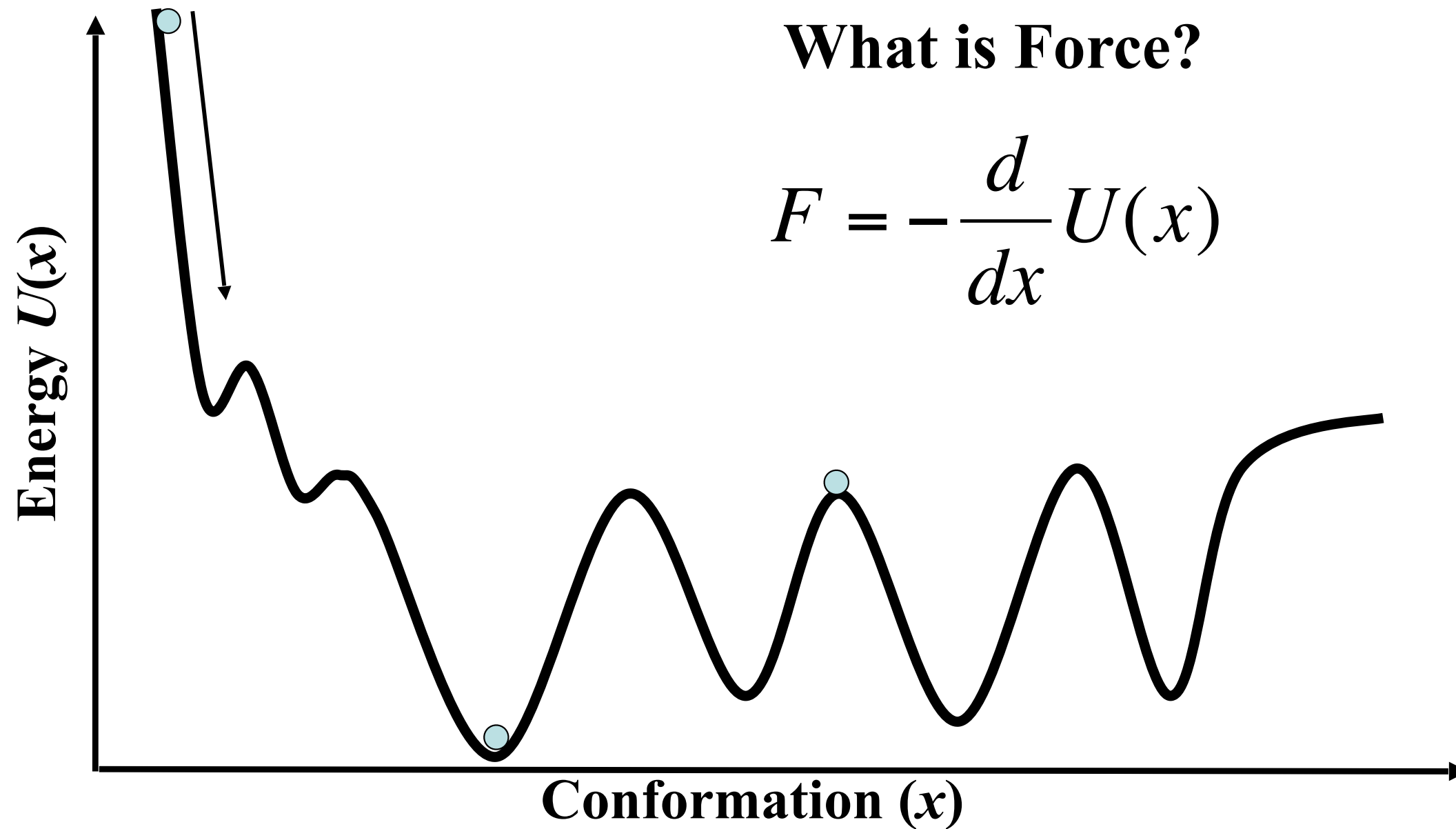
$$\mathbf{r}(t + \delta t) = \mathbf{r}(t) + \mathbf{v}(t)\delta t$$

$$\mathbf{v}(t + \delta t) = \mathbf{v}(t) + \mathbf{a}(t)\delta t$$

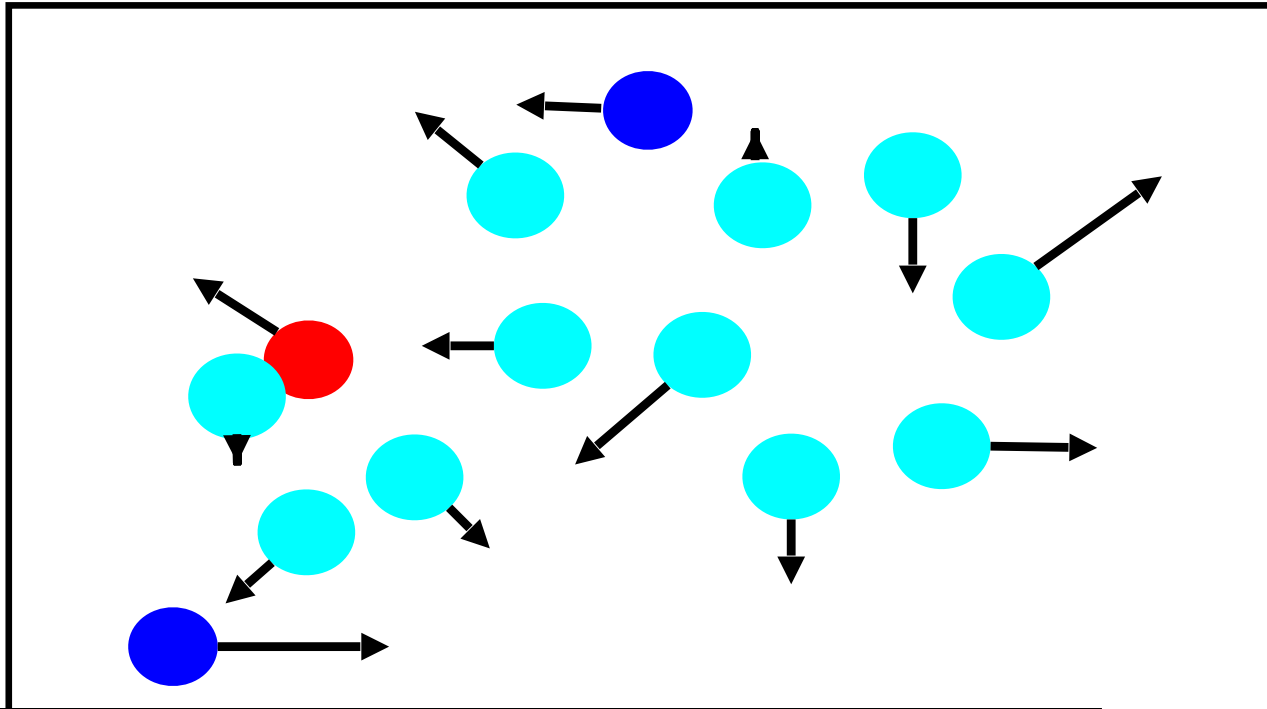
$$\mathbf{a}(t) = \mathbf{F}(t) / m$$

$$\mathbf{F} = -\frac{d}{dr}U(\mathbf{r})$$

# Potential Energy (hyper)Surface



# Classical Molecular Dynamics

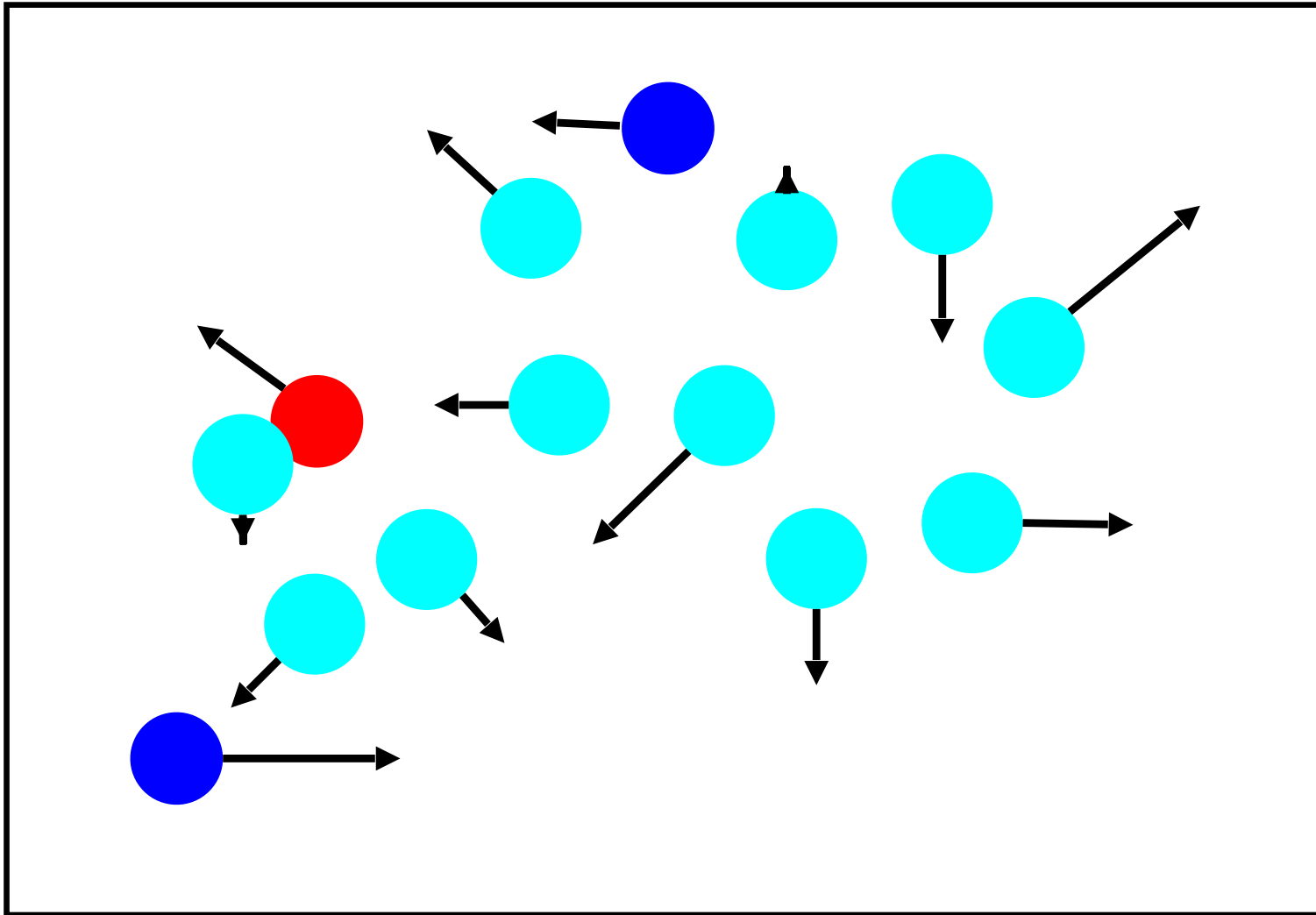


$$U(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}} + \epsilon_{ij} \left[ \left( \frac{R_{\min,ij}}{r_{ij}} \right)^{12} - 2 \left( \frac{R_{\min,ij}}{r_{ij}} \right)^6 \right]$$

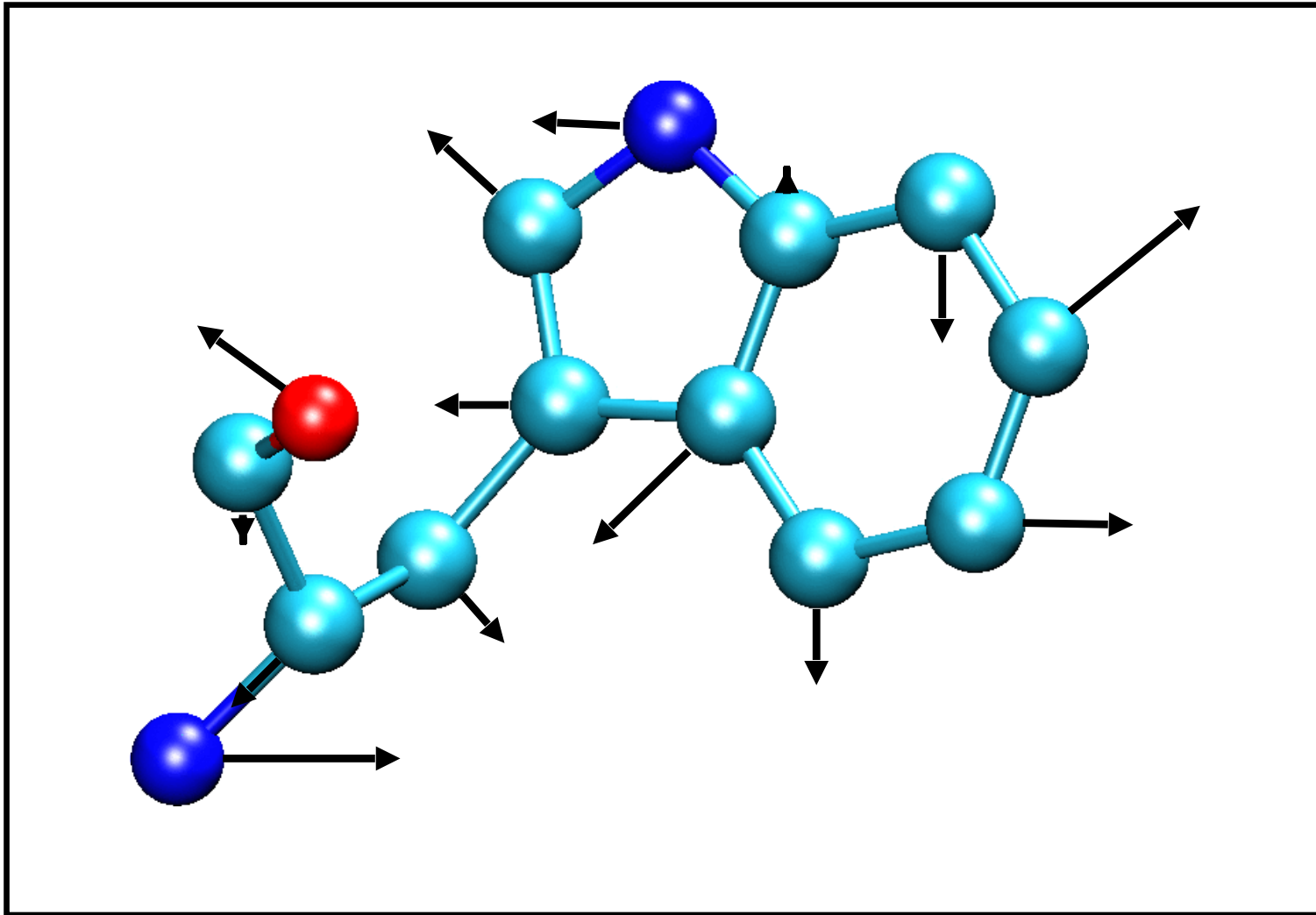
$$\mathbf{F}(\mathbf{r}) = \left( -\frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}^2} - 12 \frac{\epsilon_{ij}}{|r_{ij}|} \left[ \left( \frac{R_{\min,ij}}{r_{ij}} \right)^{12} - \left( \frac{R_{\min,ij}}{r_{ij}} \right)^6 \right] \right) \hat{\mathbf{r}}_{ij}$$



# Classical Molecular Dynamics



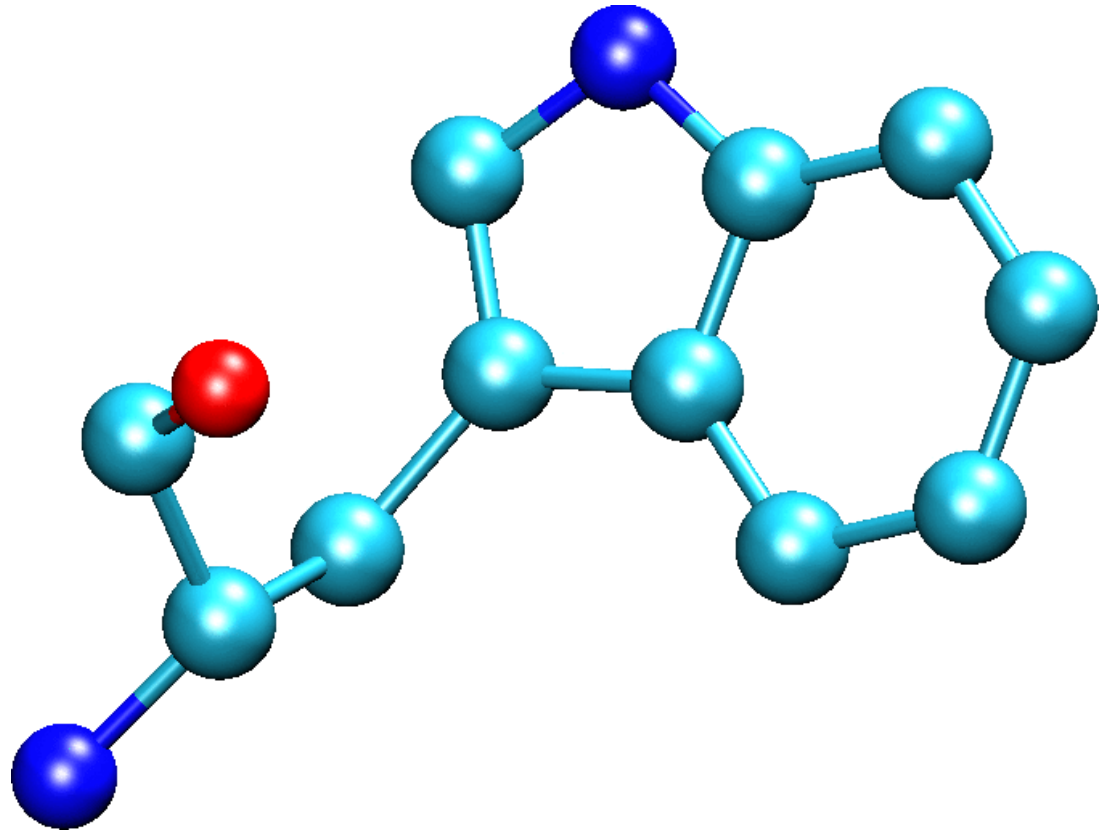
# Classical Molecular Dynamics



Bond definitions, atom types, atom names, parameters, ....

# What is a Force Field?

In molecular dynamics a molecule is described as a series of charged points (atoms) linked by springs (bonds).



To describe the time evolution of bond lengths, bond angles and torsions, also the non-bonding van der Waals and electrostatic interactions between atoms, one uses a **force field**. The **force field** is a collection of equations and associated constants designed to reproduce molecular geometry and selected properties of tested structures.

# Energy Functions

$$\begin{aligned}
 U(\vec{R}) = & \underbrace{\sum_{\text{bonds}} k_i^{\text{bond}} (r_i - r_0)^2}_{U_{\text{bond}}} + \underbrace{\sum_{\text{angles}} k_i^{\text{angle}} (\theta_i - \theta_0)^2}_{U_{\text{angle}}} + \\
 & \underbrace{\sum_{\text{dihedrals}} k_i^{\text{dihe}} [1 + \cos(n_i \phi_i + \delta_i)]}_{U_{\text{dihedral}}} + \\
 & \underbrace{\sum_i \sum_{j \neq i} 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \sum_i \sum_{j \neq i} \frac{q_i q_j}{\epsilon r_{ij}}}_{U_{\text{nonbond}}}
 \end{aligned}$$

$U_{\text{bond}}$  = oscillations about the equilibrium bond length

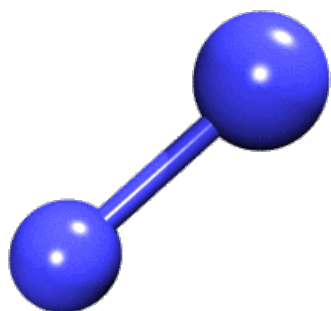
$U_{\text{angle}}$  = oscillations of 3 atoms about an equilibrium bond angle

$U_{\text{dihedral}}$  = torsional rotation of 4 atoms about a central bond

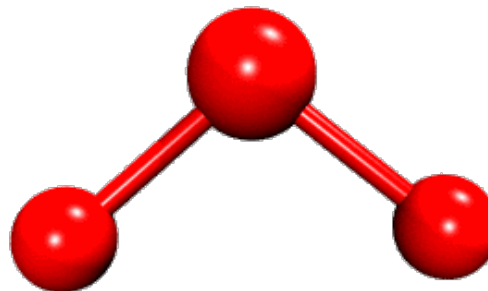
$U_{\text{nonbond}}$  = non-bonded energy terms (electrostatics and Lenard-Jones)

# Energy Terms Described in the CHARMM Force Field

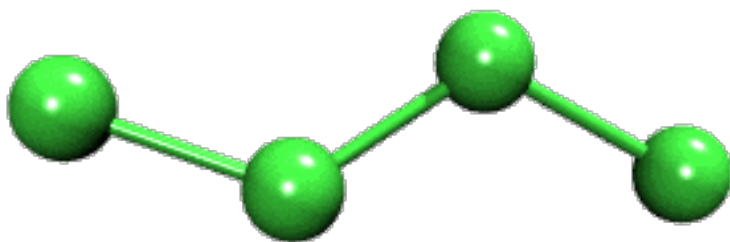
Bond



Angle



Dihedral



Improper



# Classical Dynamics

*F=ma at 300K*

Energy function:  $U(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = U(\vec{R})$

used to determine the force on each atom:

$$m_i \frac{d^2 \vec{r}_i}{dt^2} = \vec{F}_i = -\vec{\nabla} U(\vec{R})$$

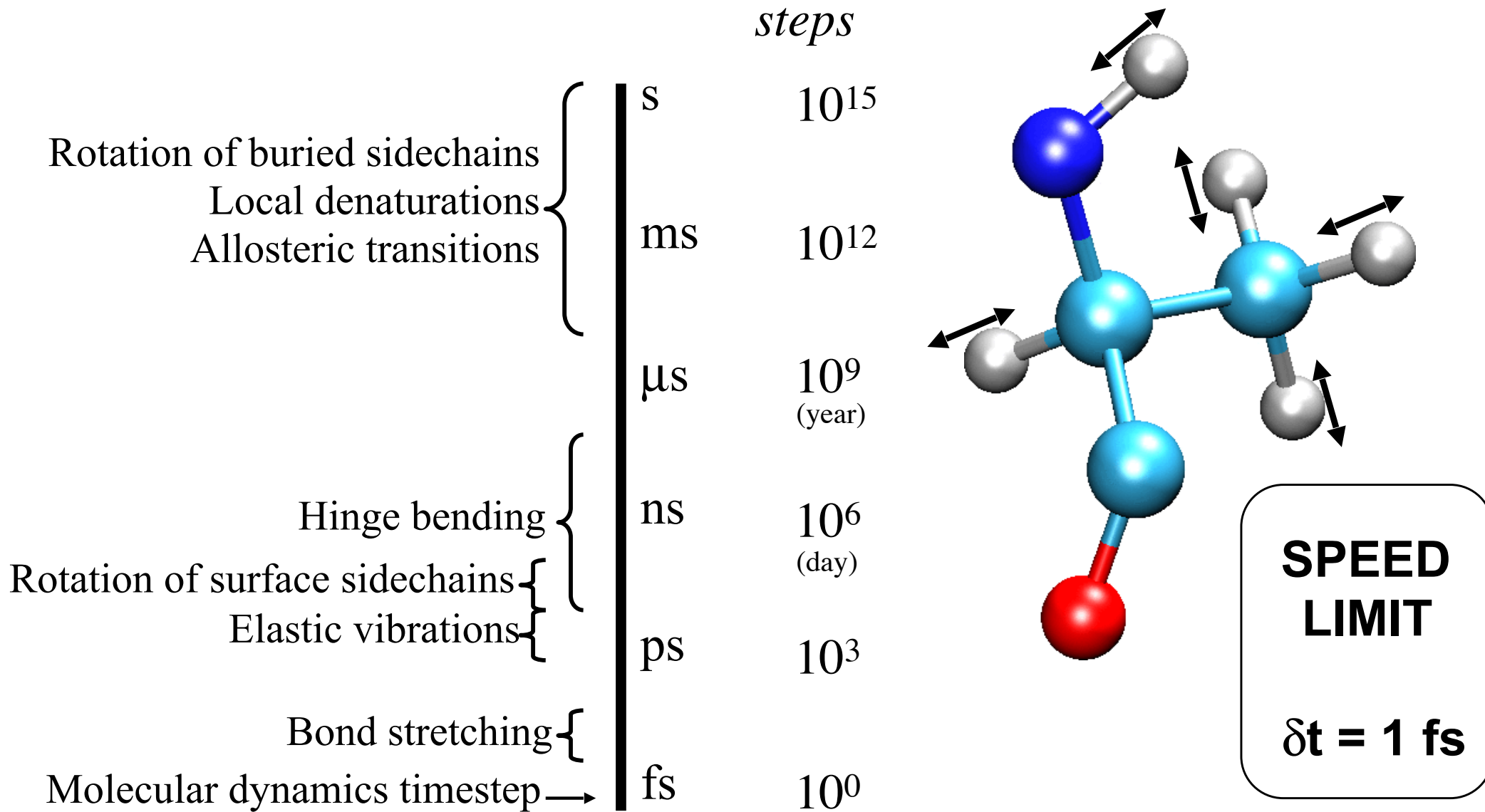
yields a set of 3N coupled 2<sup>nd</sup>-order differential equations that can be propagated forward (or backward) in time.

Initial coordinates obtained from crystal structure, velocities taken at random from Boltzmann distribution.

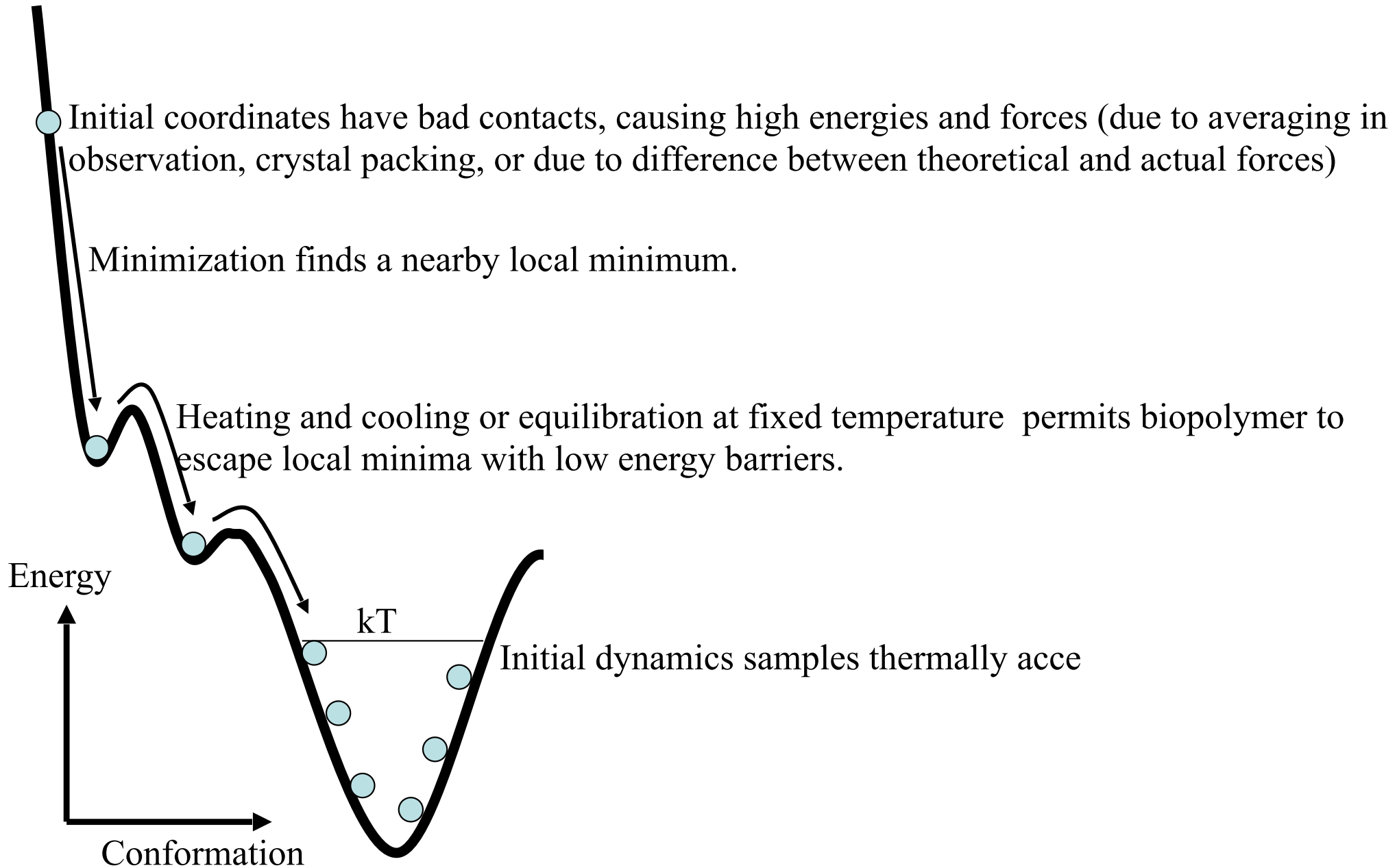
Langevin dynamics deals with each atom separately, balancing a small friction term with Gaussian noise to control temperature:

$$m \ddot{\vec{r}} = \vec{F}(\vec{r}) - \gamma m \dot{\vec{r}} + \vec{R}(t)$$

# The most serious bottleneck

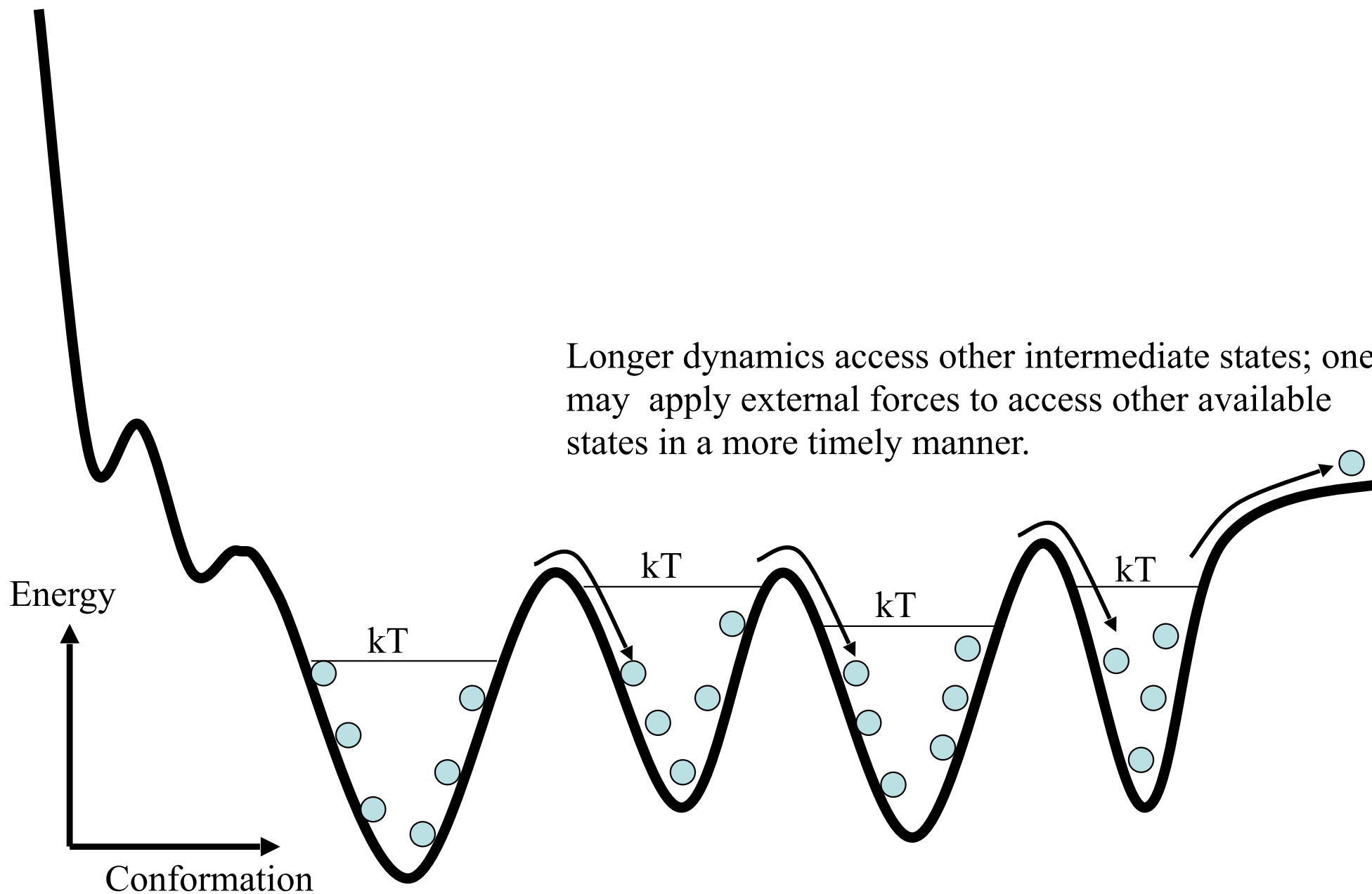


# Molecular Dynamics to Sample Energy Landscape

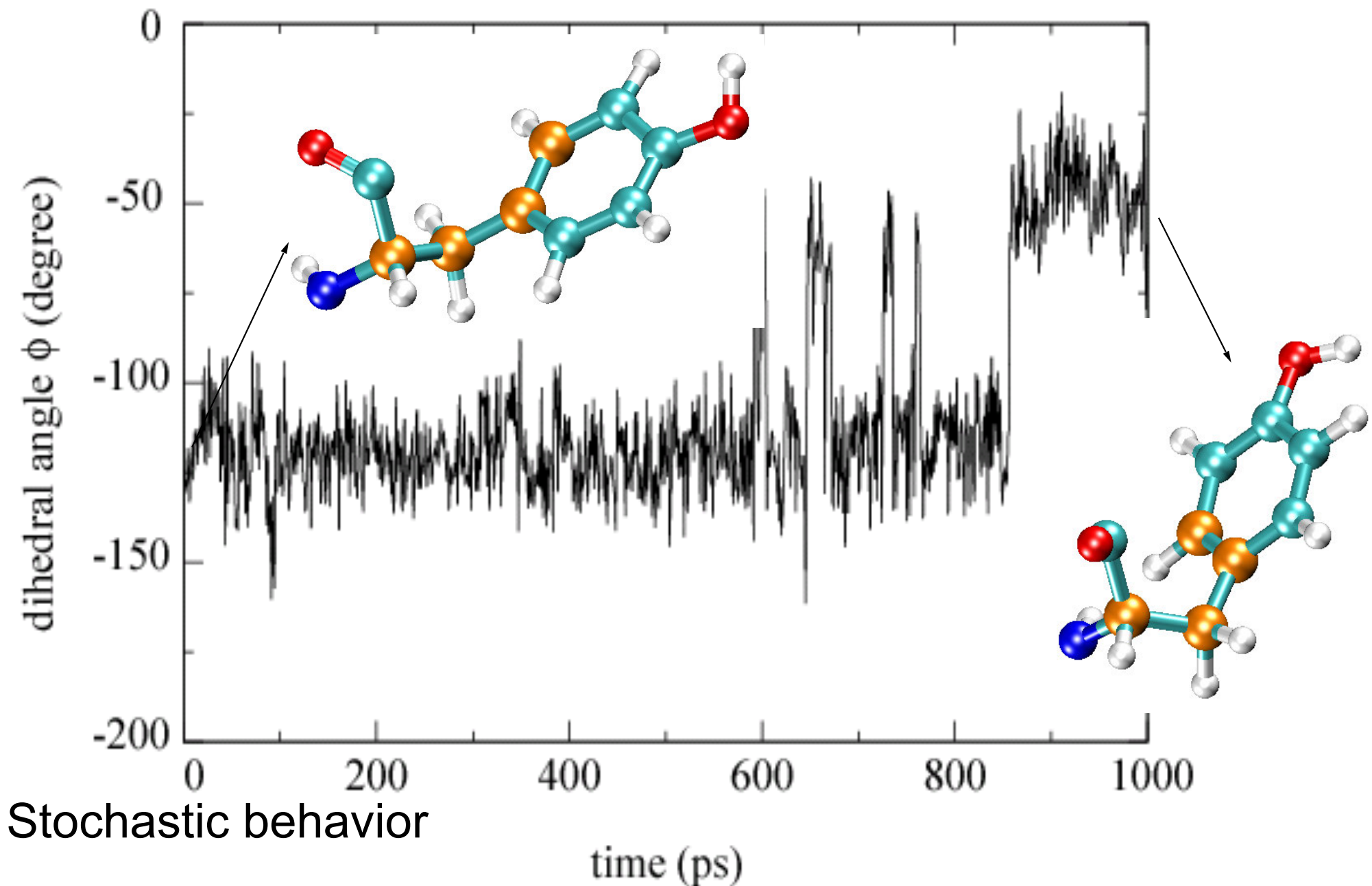




# Molecular Dynamics to Sample Energy Landscape



# Patience is required to observe Molecular Events



# Steps in a Typical MD Simulation

- 1. Prepare molecule
  - Read in pdb and psf file
- 2. Minimization
  - Reconcile observed structure with force field used ( $T = 0$ )
- 3. Heating
  - Raise temperature of the system
- 4. Equilibration
  - Ensure system is stable
- 5. Dynamics
  - Simulate under desired conditions (NVE, NpT, etc)
  - Collect your data
- 6. Analysis
  - Evaluate observables (macroscopic level properties)
  - Or relate to single molecule experiments

# Preparing Your System for MD Solvation

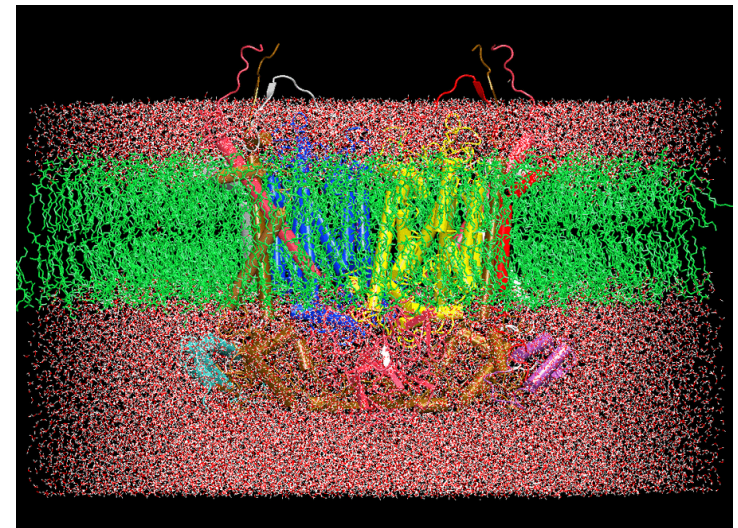
Biological activity is the result of interactions between molecules and occurs at the interfaces between molecules (protein-protein, protein-DNA, protein-solvent, DNA-solvent, etc).

Why model solvation?

- many biological processes occur in aqueous solution
- solvation effects play a crucial role in determining molecular conformation, electronic properties, binding energies, etc

How to model solvation?

- explicit treatment: solvent molecules are added to the molecular system
- implicit treatment: solvent is modeled as a continuum dielectric



# Classical Molecular Dynamics

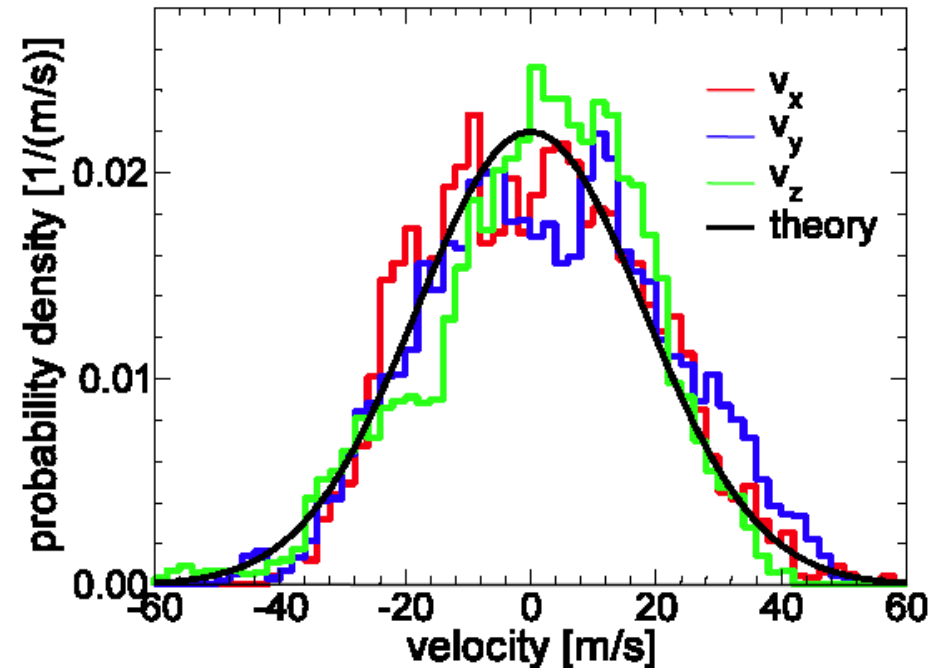
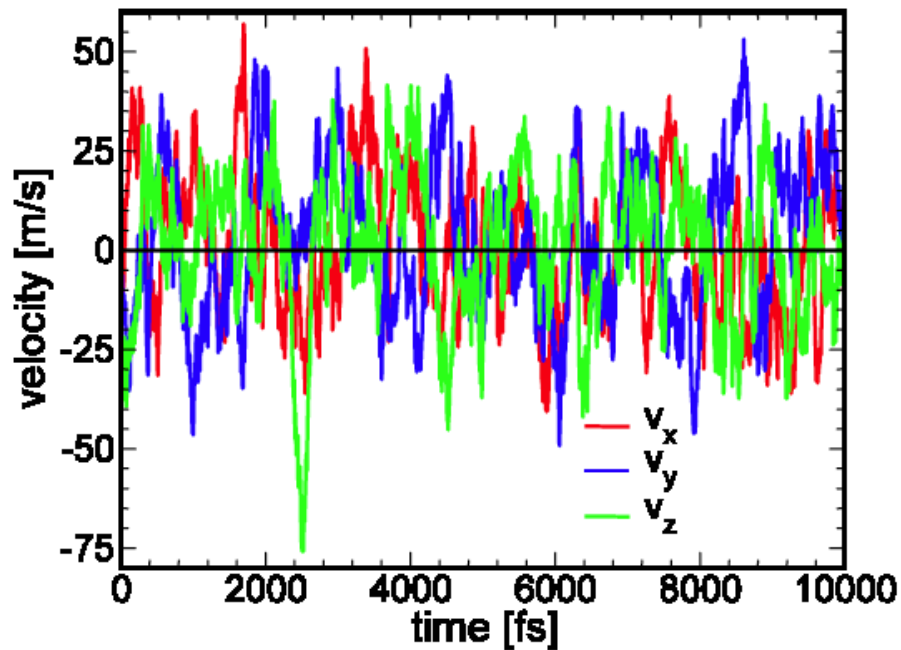
$$\mathbf{r}(t + \delta t) = \mathbf{r}(t) + \mathbf{v}(t)\delta t$$

$$\mathbf{v}(t + \delta t) = \mathbf{v}(t) + \mathbf{a}(t)\delta t$$

$$\mathbf{a}(t) = \mathbf{F}(t) / m$$

$$\mathbf{F} = -\frac{d}{dr}U(\mathbf{r})$$

# Maxwell Distribution of Atomic Velocities



$$p(v_\sigma) = \sqrt{\frac{m}{2\pi k_B T}} \exp\left[-\frac{mv_\sigma^2}{2k_B T}\right]$$

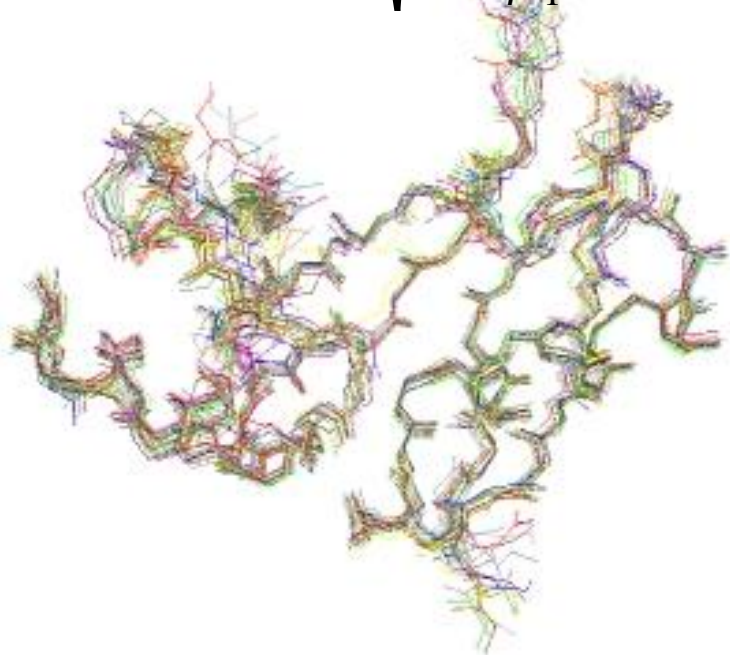
$$\sigma = x, y, z$$

# Equilibrium Properties of Proteins

## Ubiquitin

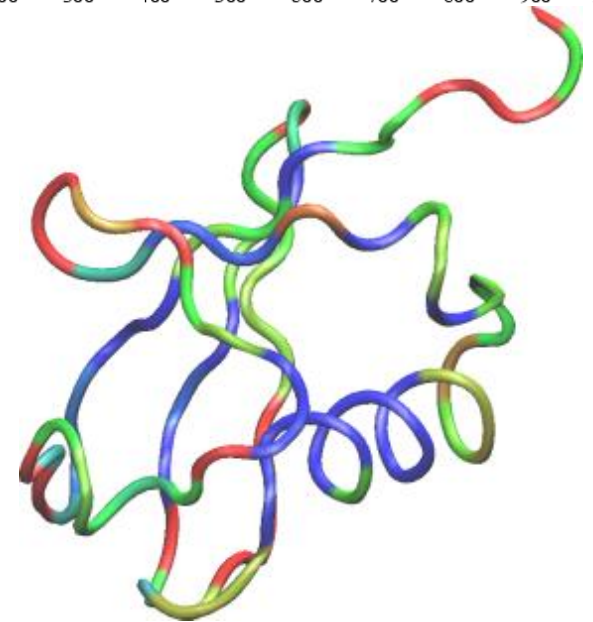
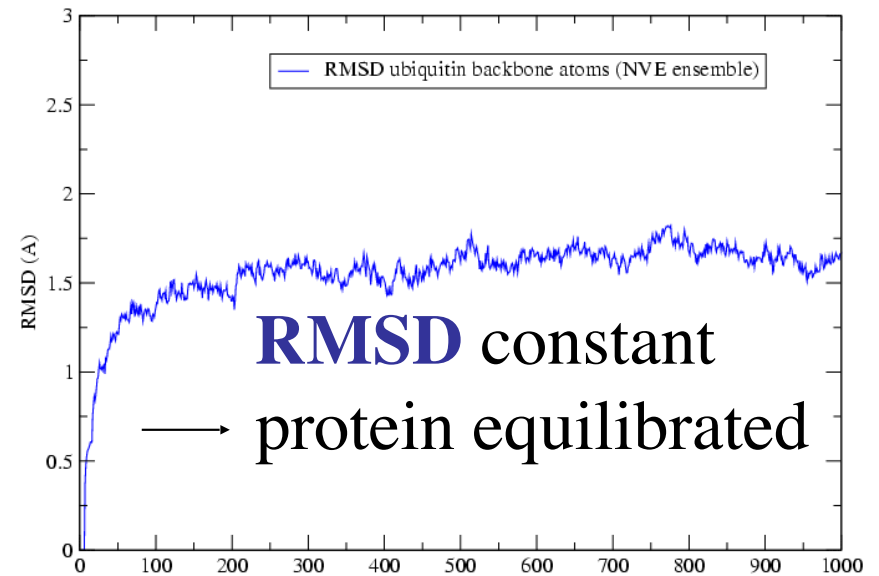
Root Mean Squared Deviation: measure for equilibration and protein flexibility

$$RMSD(t) = \sqrt{\frac{1}{N} \sum_{i=1}^N (R_i(t) - R_i(0))^2}$$



NMR structures  
aligned together to see flexibility

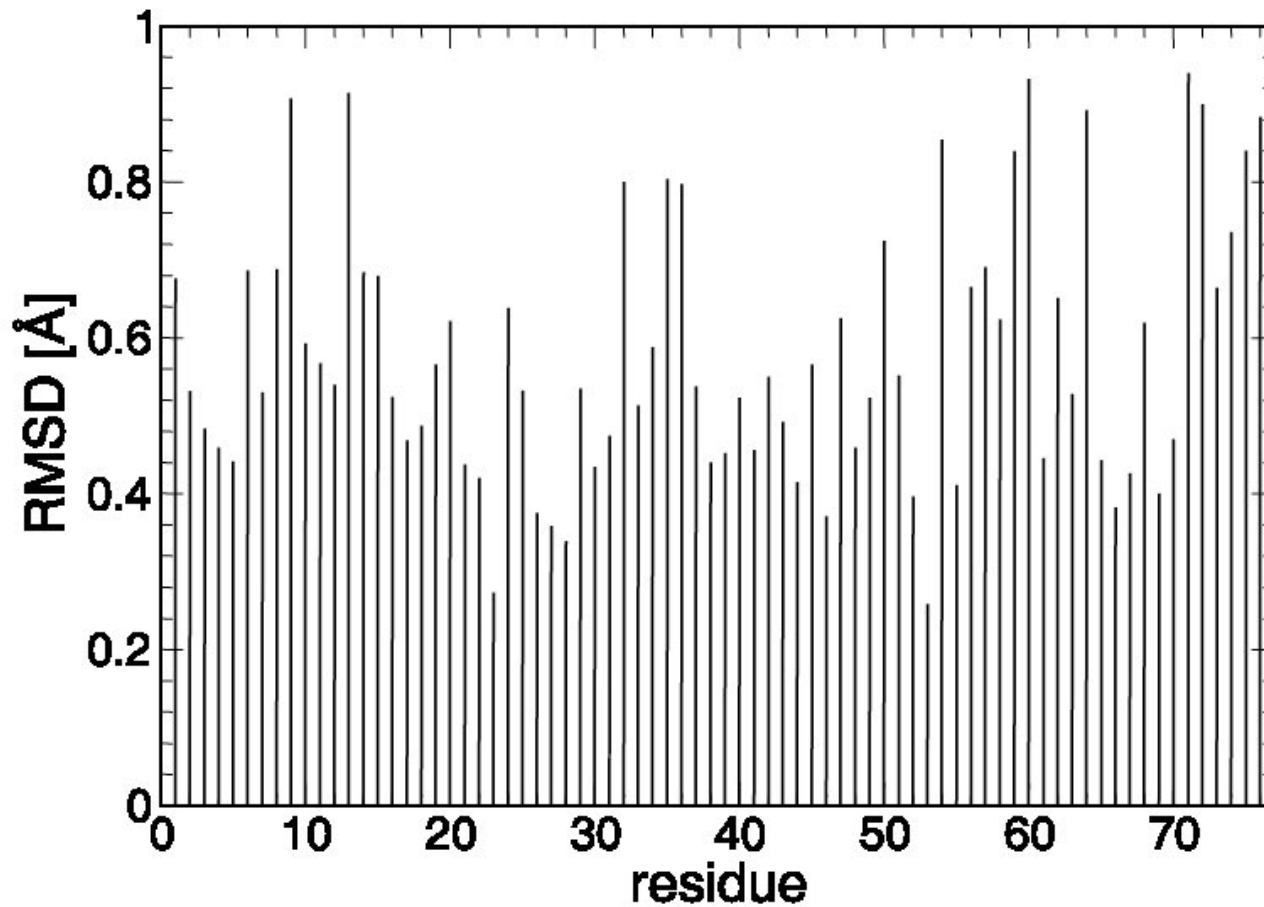
**Protein sequence  
exhibits  
characteristic  
permanent  
flexibility!**



MD simulation  
The color represents mobility of the protein  
through simulation (red = more flexible)

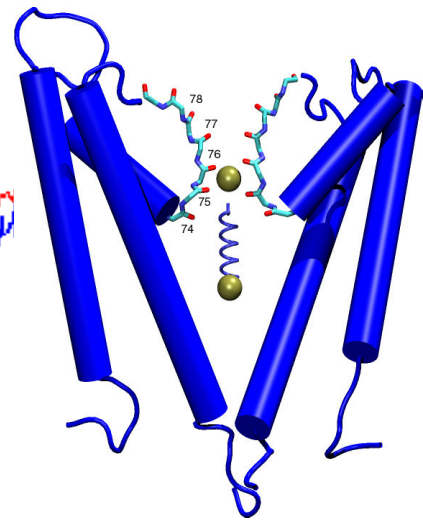
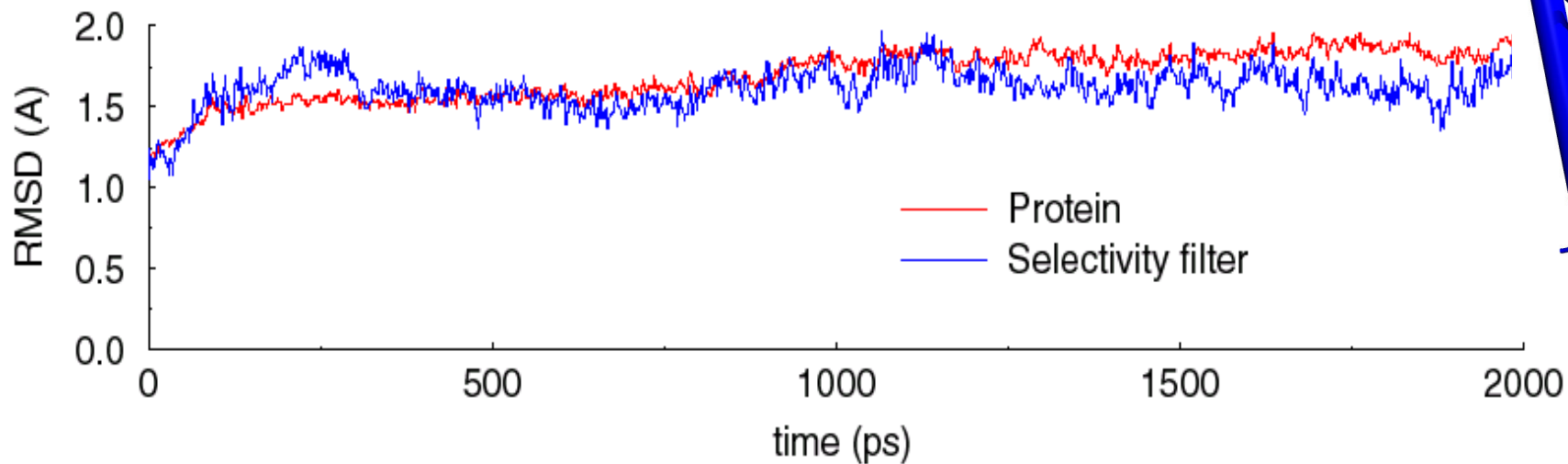
# Thermal Motion of Ubiquitin from MD

RMSD values per residue

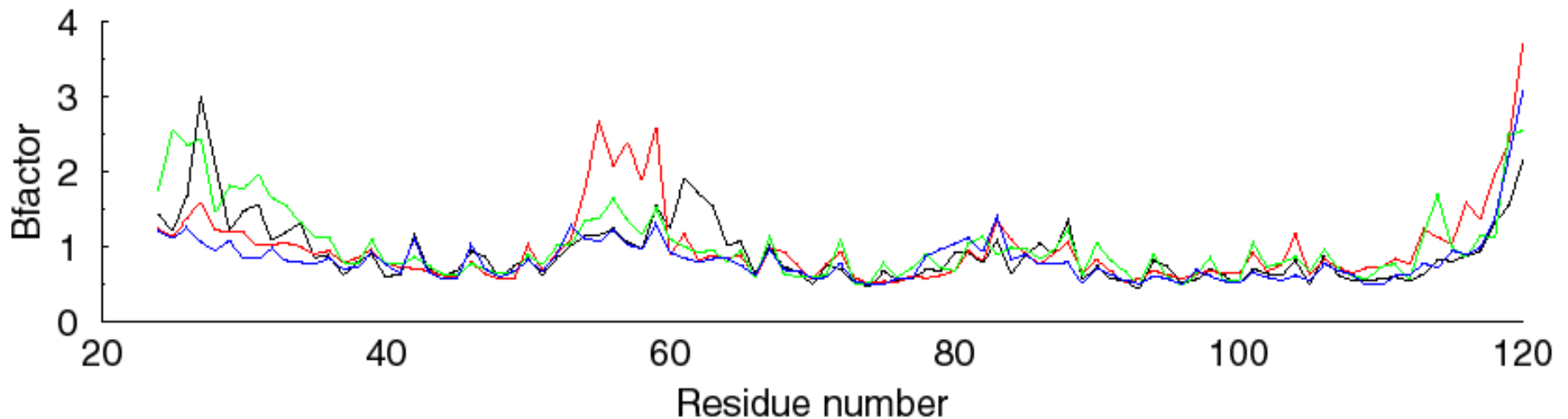




# MD Results



RMS deviations for the KcsA protein and its selectivity filter indicate that the protein is stable during the simulation with the selectivity filter the most stable part of the system.



Temperature factors for individual residues in the four monomers of the KcsA channel protein indicate that the most flexible parts of the protein are the N and C terminal ends, residues 52-60 and residues 84-90. Residues 74-80 in the selectivity filter have low temperature factors and are very stable during the simulation.

# Battling the Timescale

non-Equilibrium MD simulations

Reduced Representations

# Battling the Timescale - Case I

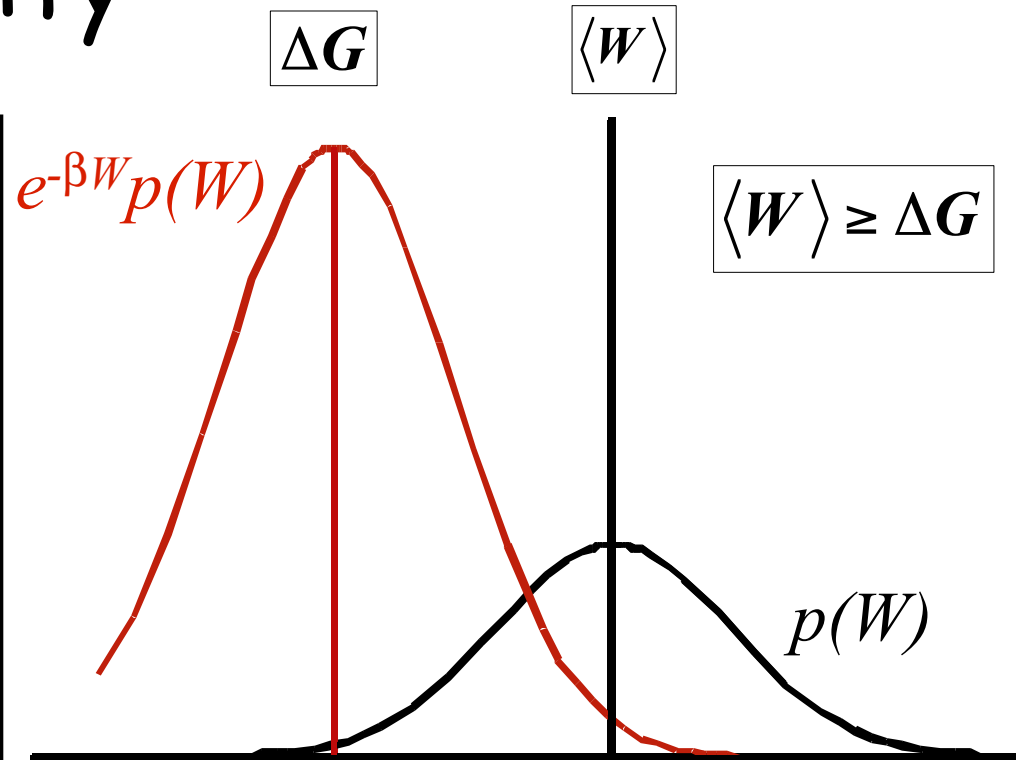
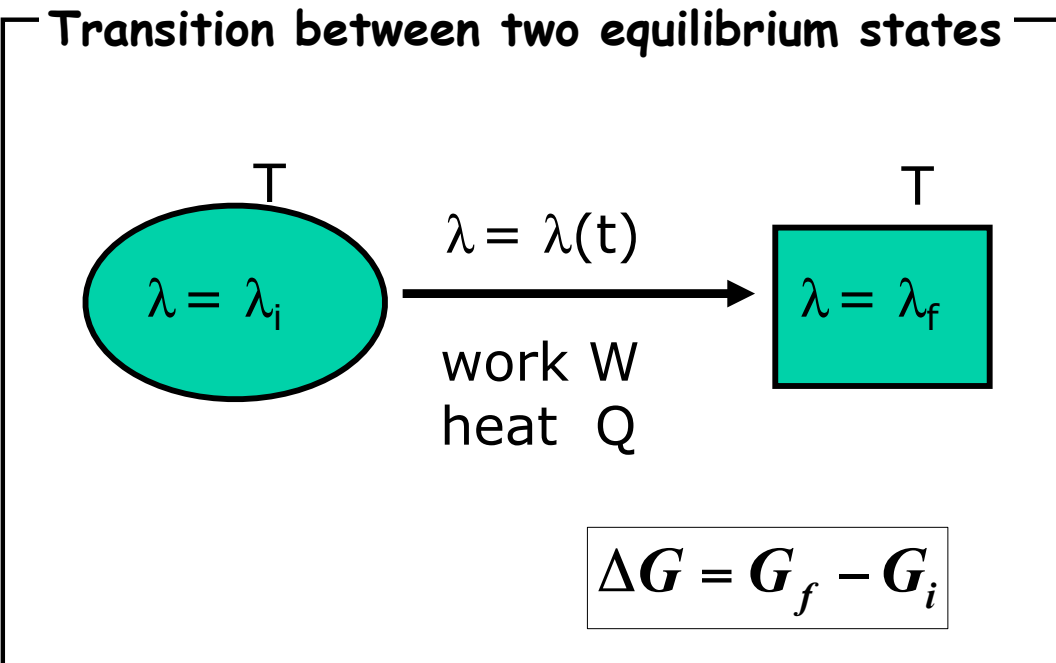
## Steered Molecular Dynamics is a non-equilibrium method by nature

- A wide variety of events that are inaccessible to conventional molecular dynamics simulations can be probed.
- The system will be driven, however, away from equilibrium, resulting in problems in describing the energy landscape associated with the event of interest.

Second law of thermodynamics

$$\longrightarrow W \geq \Delta G$$

# Jarzynski's Equality



C. Jarzynski, *Phys. Rev. Lett.*, **78**, 2690 (1997)

C. Jarzynski, *Phys. Rev. E*, **56**, 5018 (1997)

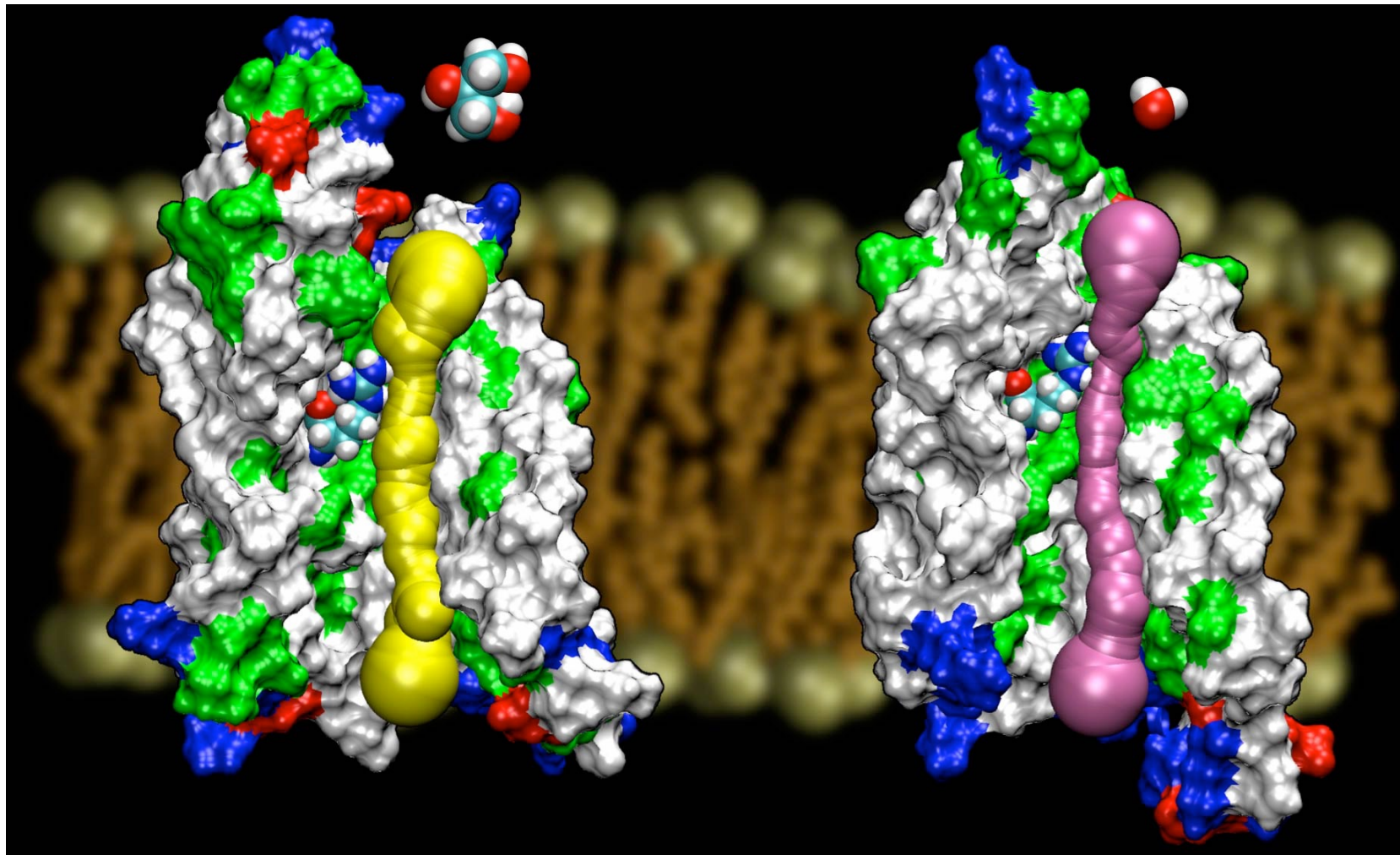
$$\langle e^{-\beta W} \rangle = e^{-\beta \Delta G}$$

$$\beta = \frac{1}{k_B T}$$

**In principle**, it is possible to obtain free energy surfaces from repeated **non-equilibrium** experiments.

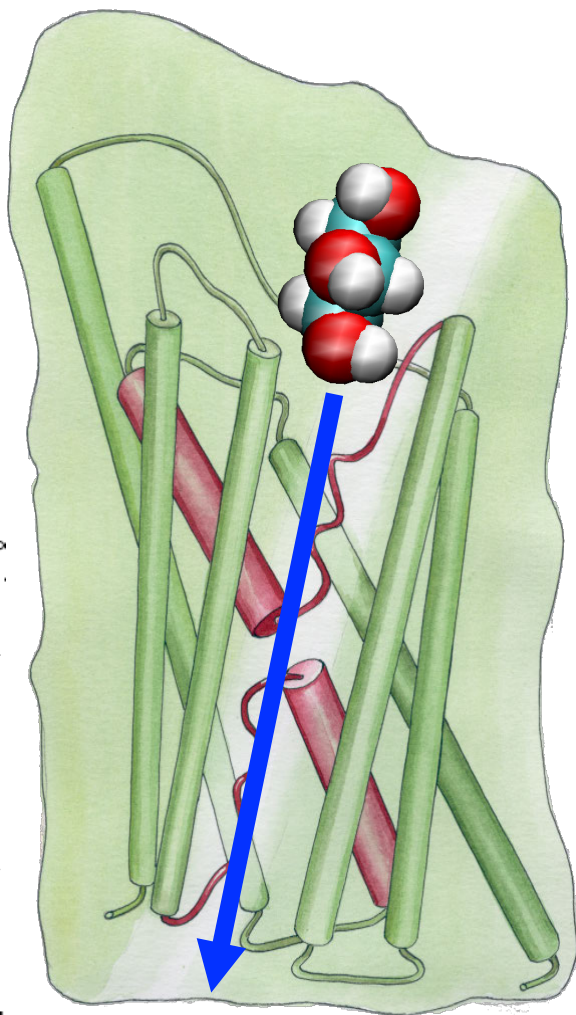
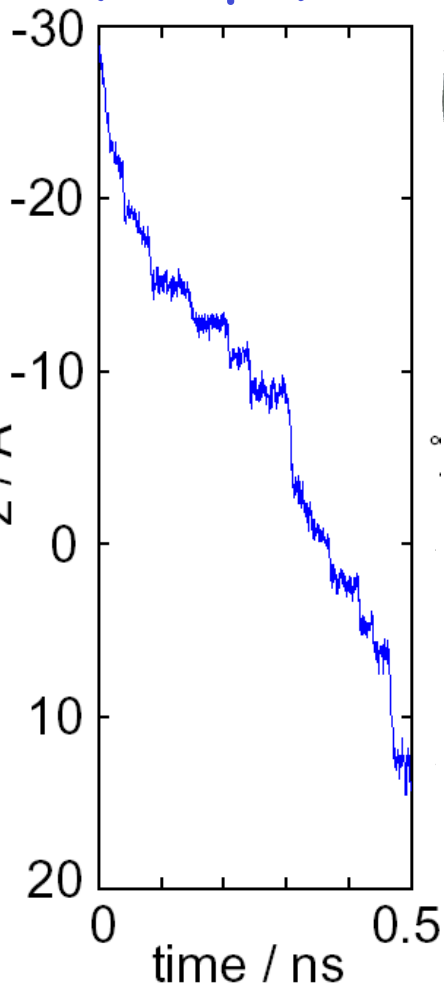
# AqpZ vs. GlpF

- Both from *E. coli*
- AqpZ is a pure water channel
- GlpF is a glycerol channel
- We have high resolution structures for both channels

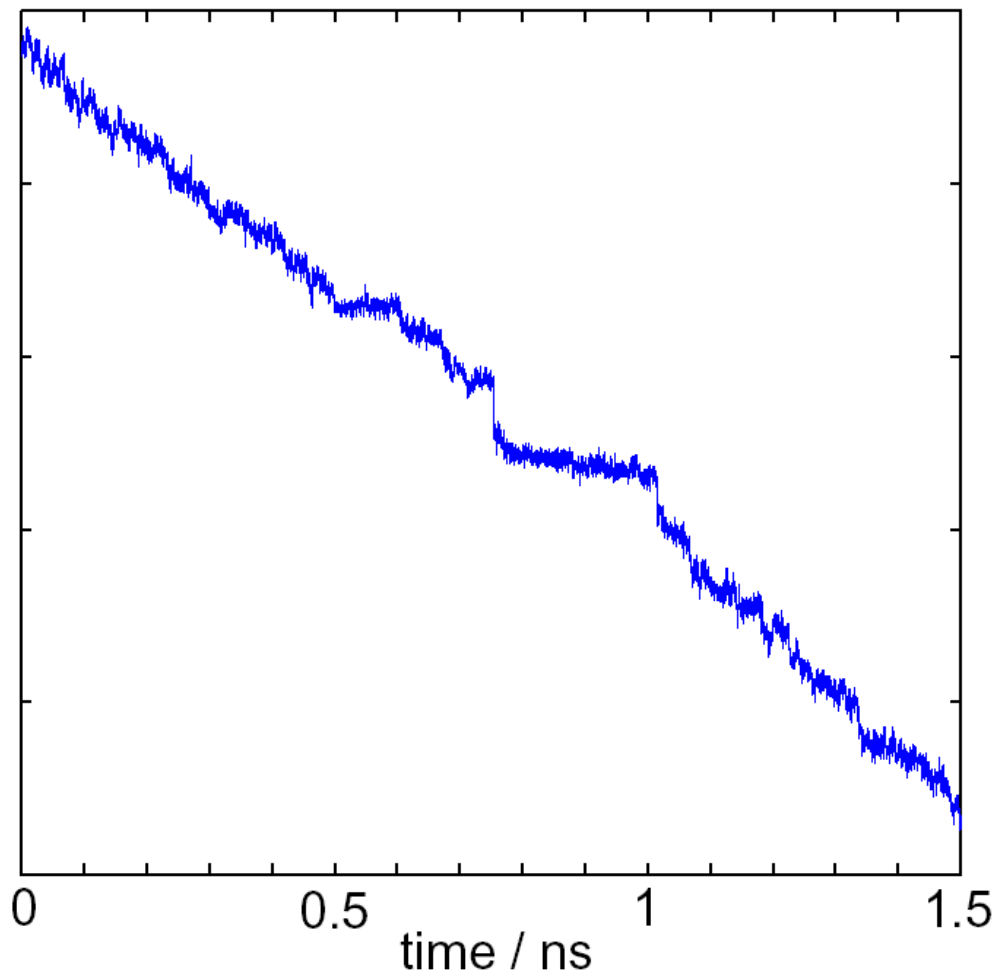


# Steered Molecular Dynamics

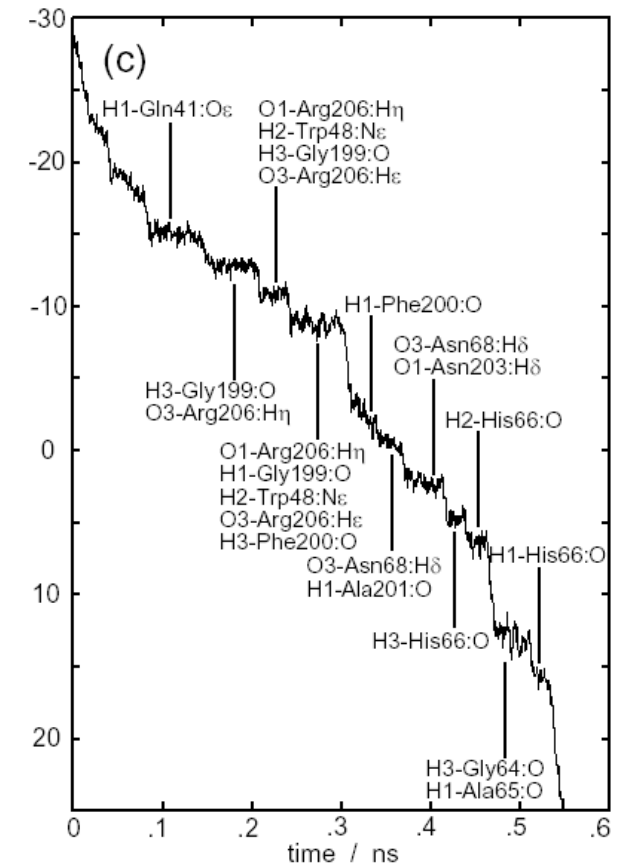
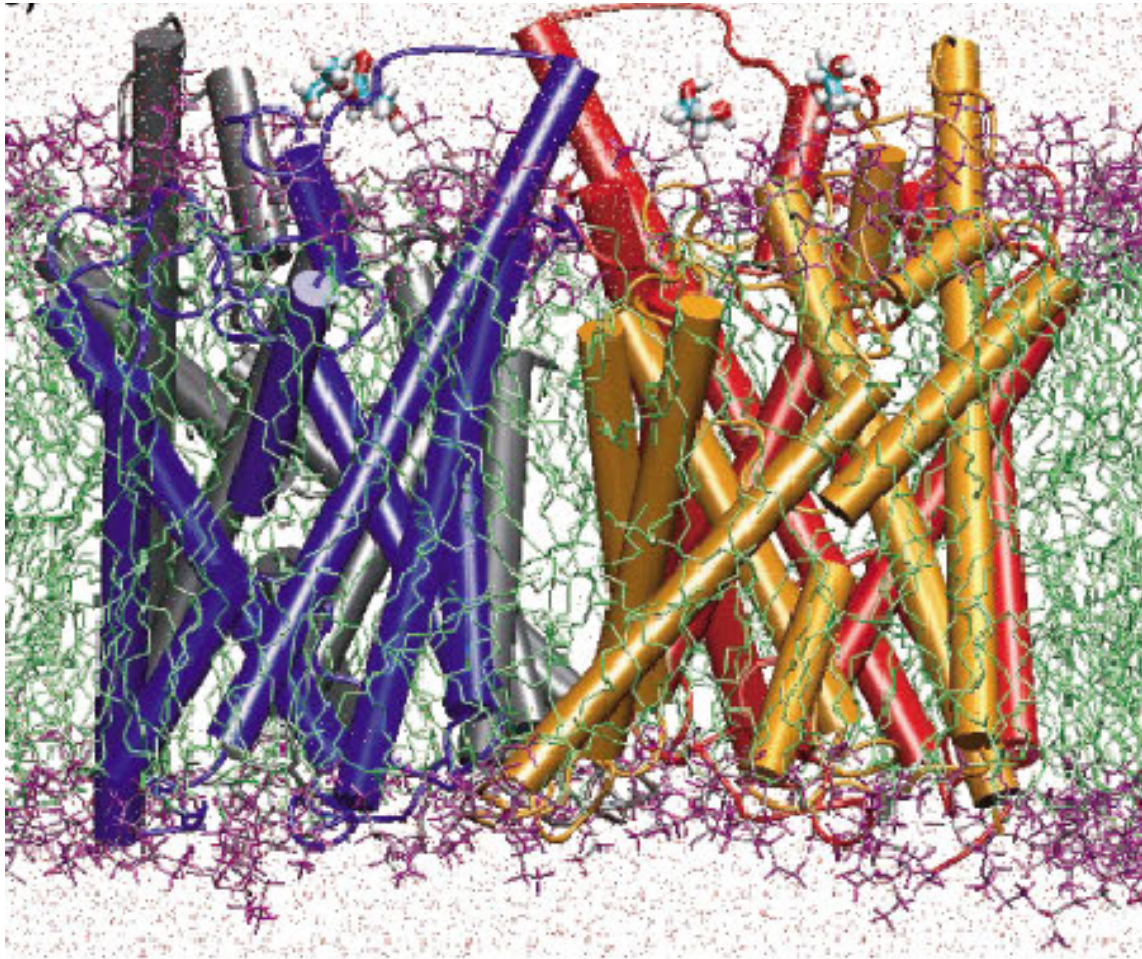
constant force  
(250 pN)



constant velocity  
(30 Å/ns)



# SMD Simulation of Glycerol Passage



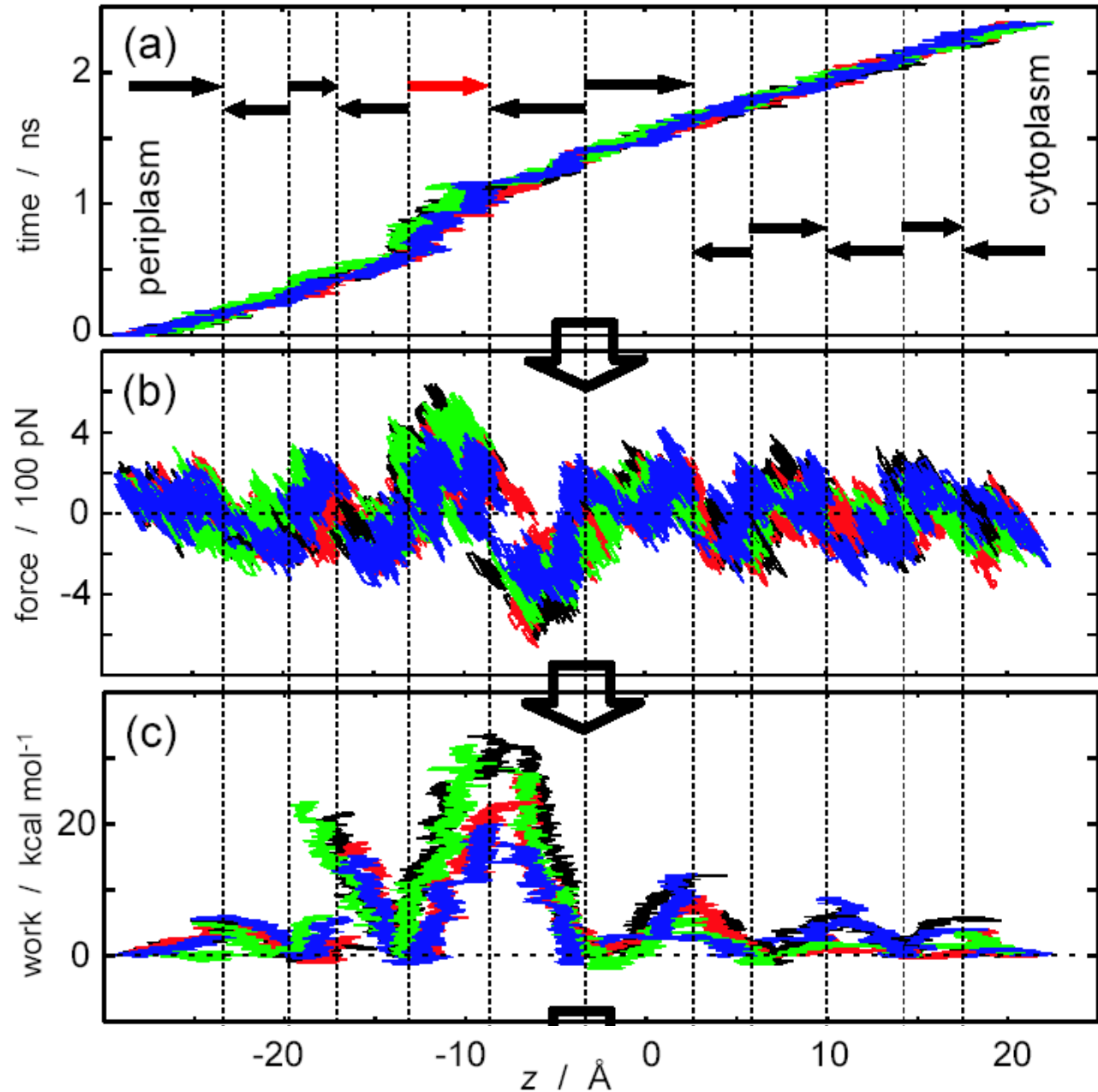
Trajectory of glycerol pulled by **constant force**

# Constructing the Potential of Mean Force

4 trajectories  
 $v = 0.03, 0.015$  Å/ps  
 $k = 150$  pN/Å

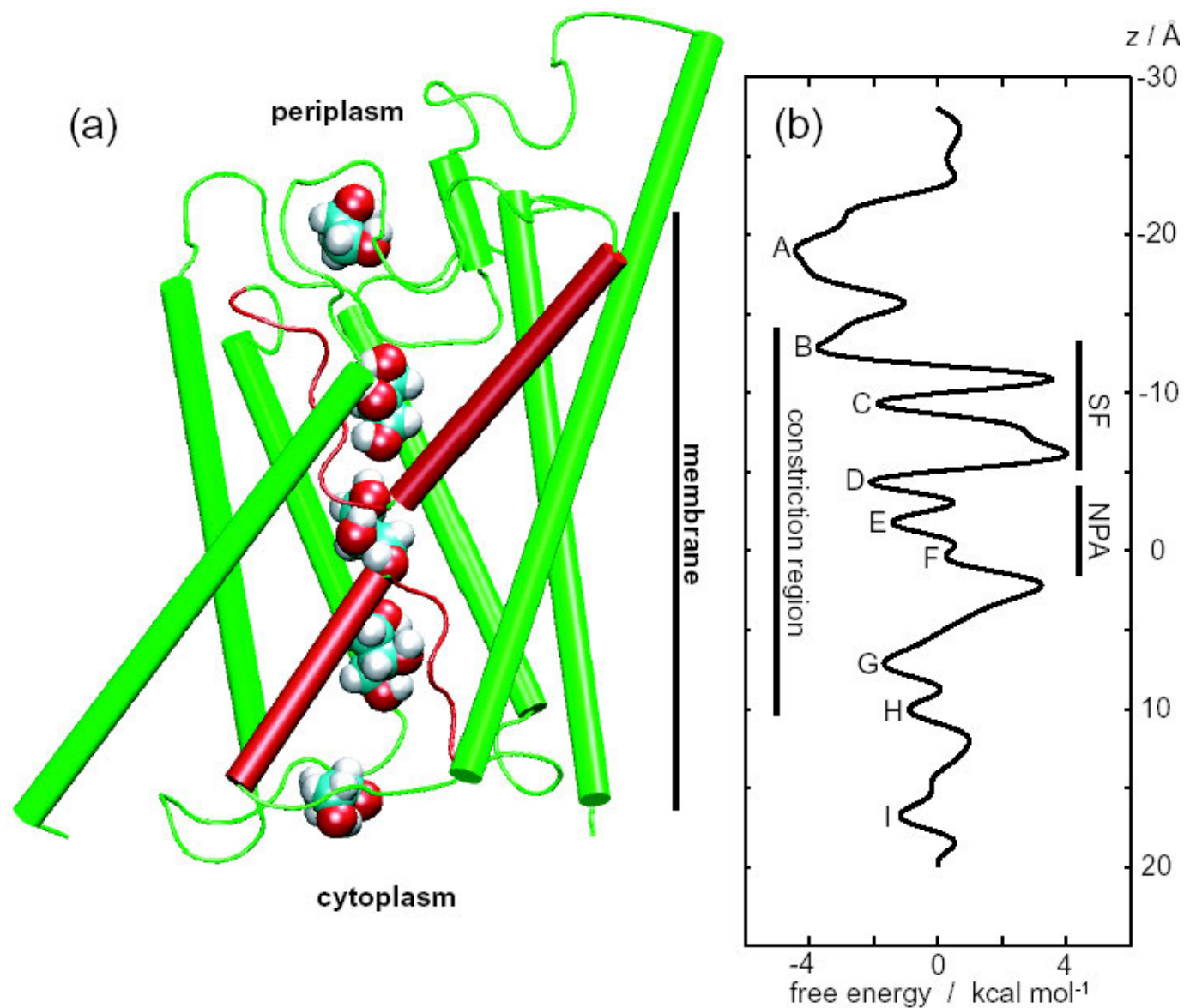
$$f(t) = -k[z(t) - z_0 - vt]$$

$$W(t) = \int_0^t dt' v f(t')$$



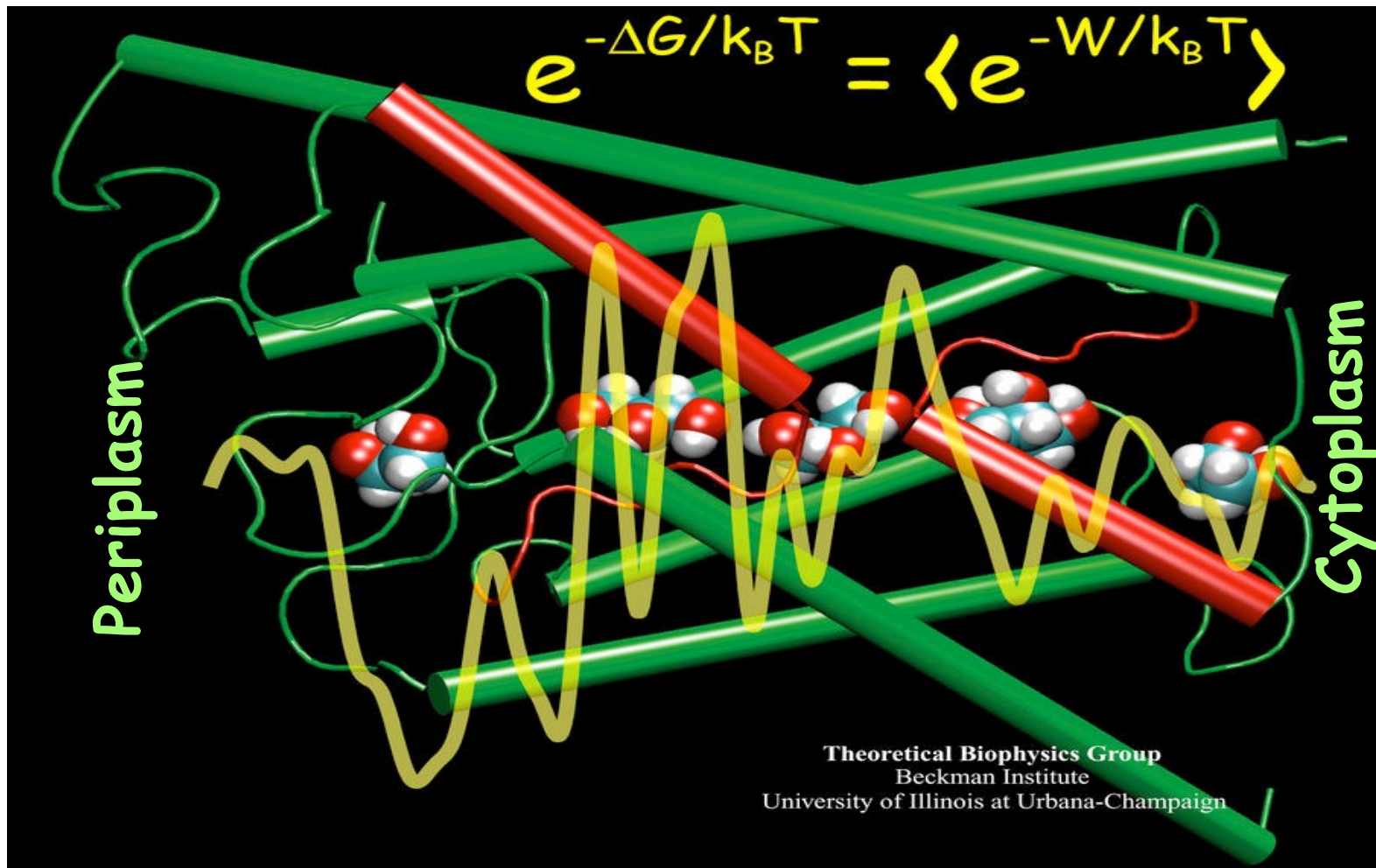


# Features of the Potential of Mean Force



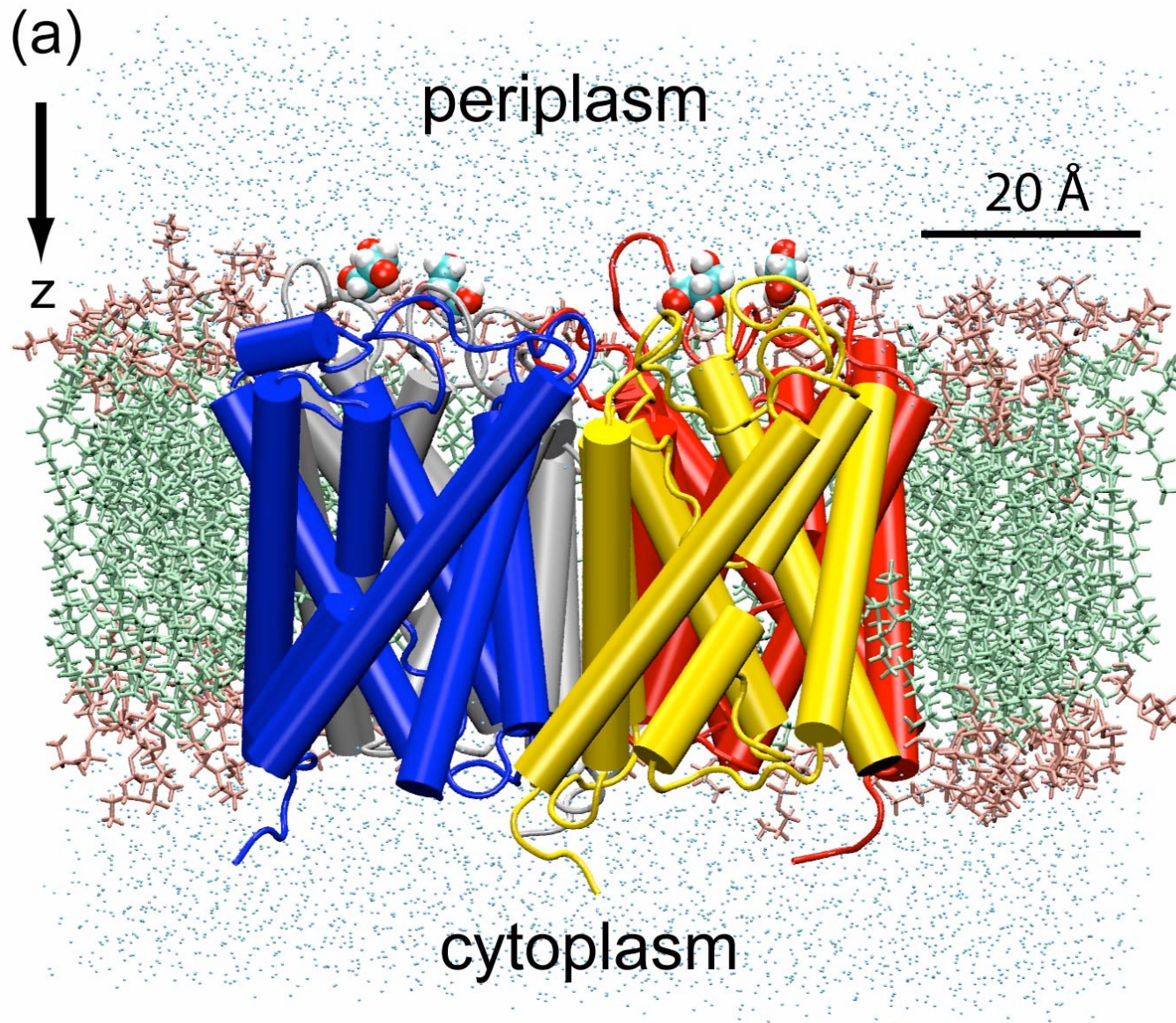
- Captures major features of the channel
- The largest barrier  $\approx 7.3$  kcal/mol; exp.:  $9.6 \pm 1.5$  kcal/mol

# Features of the Potential of Mean Force

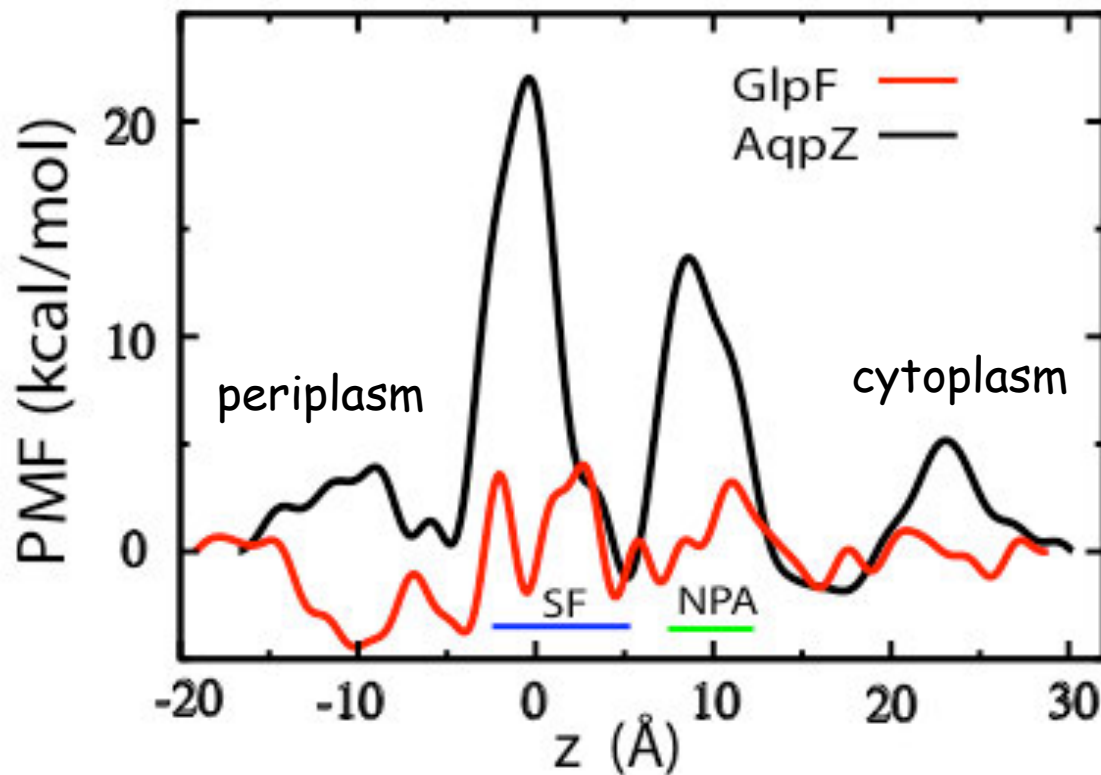


## Asymmetric Profile in the Vestibules

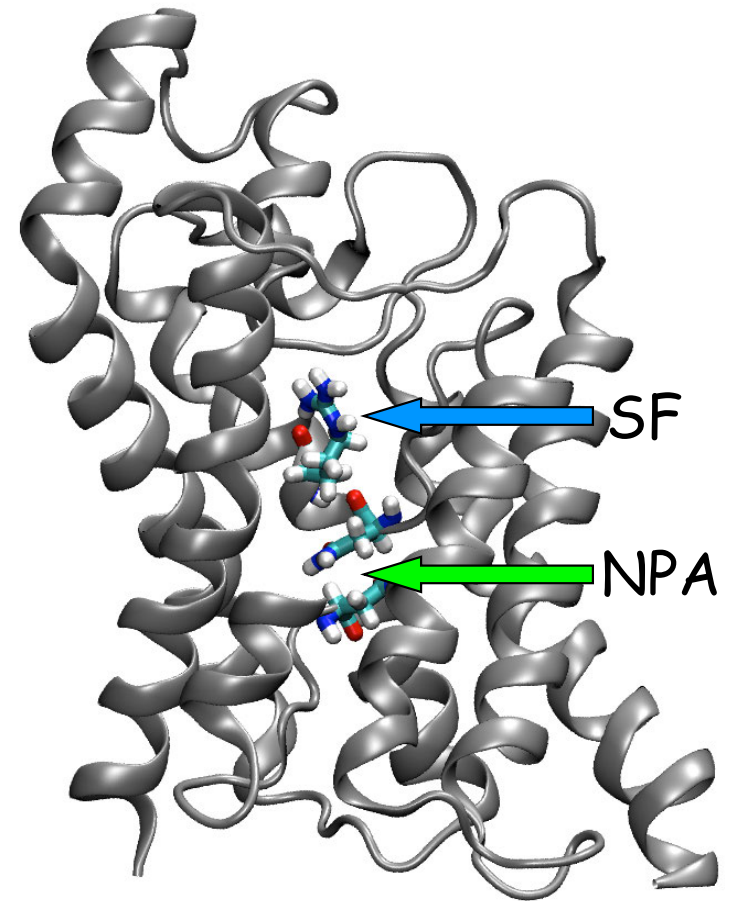
# Artificial induction of glycerol conduction through AqpZ



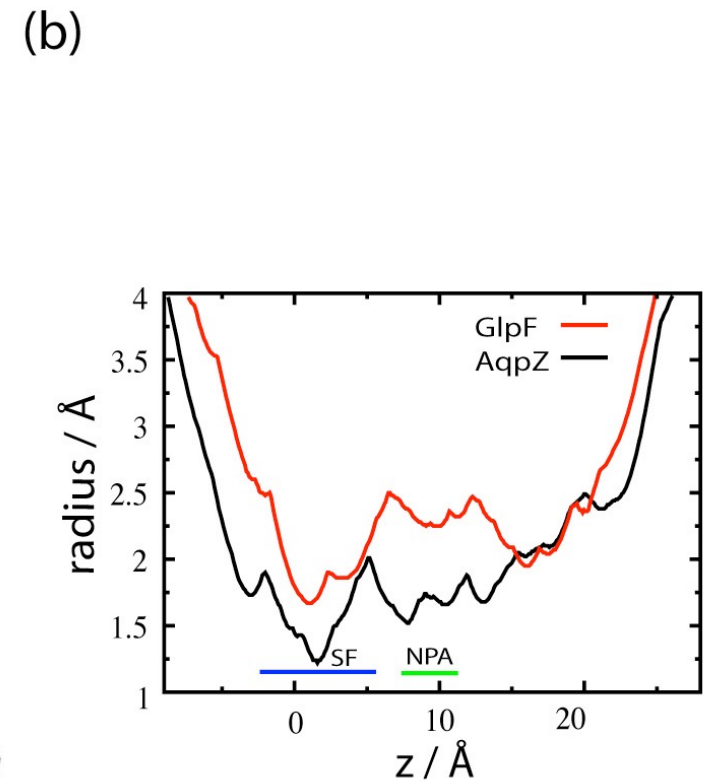
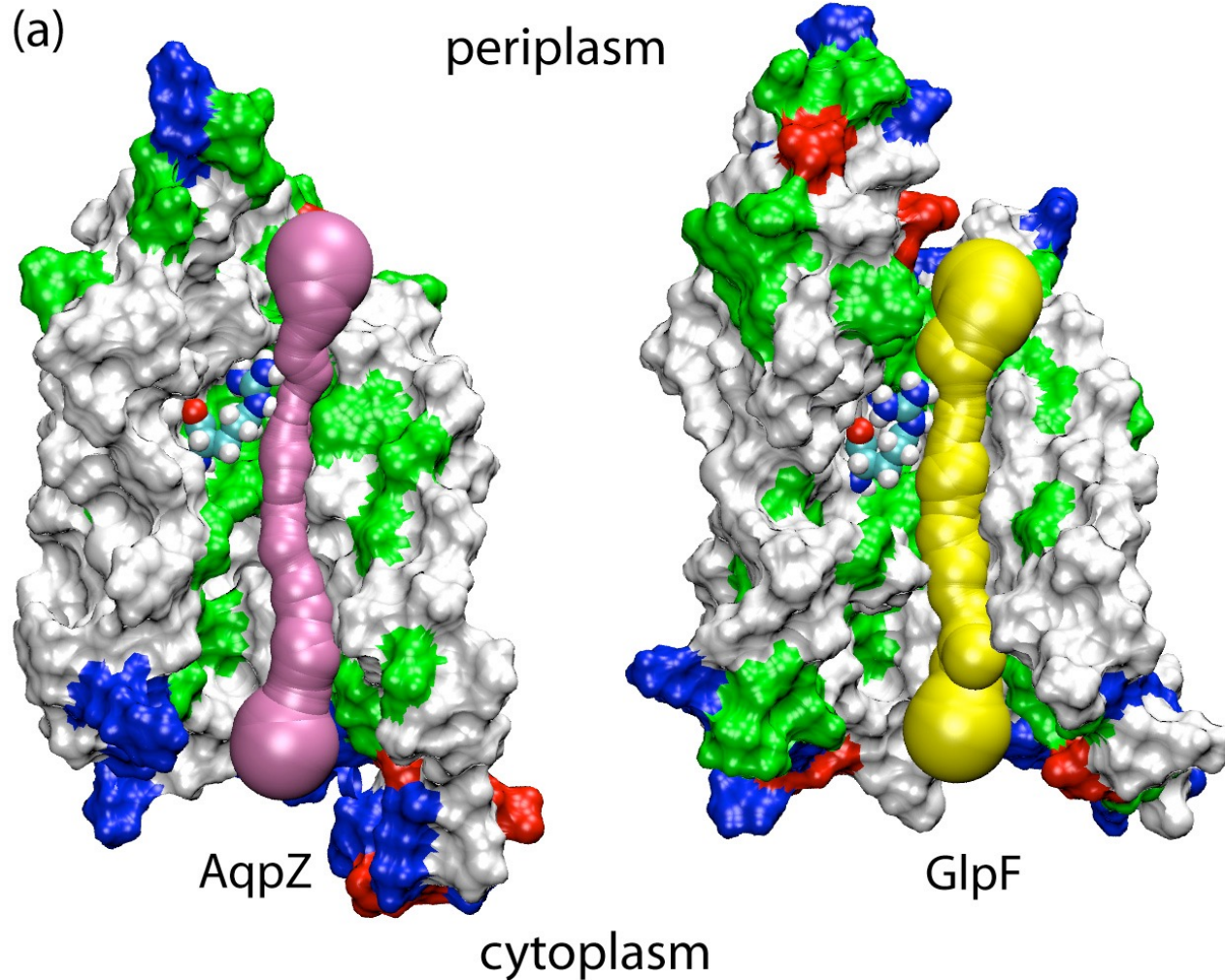
# Three fold higher barriers



AqpZ 22.8 kcal/mol  
GlpF 7.3 kcal/mol

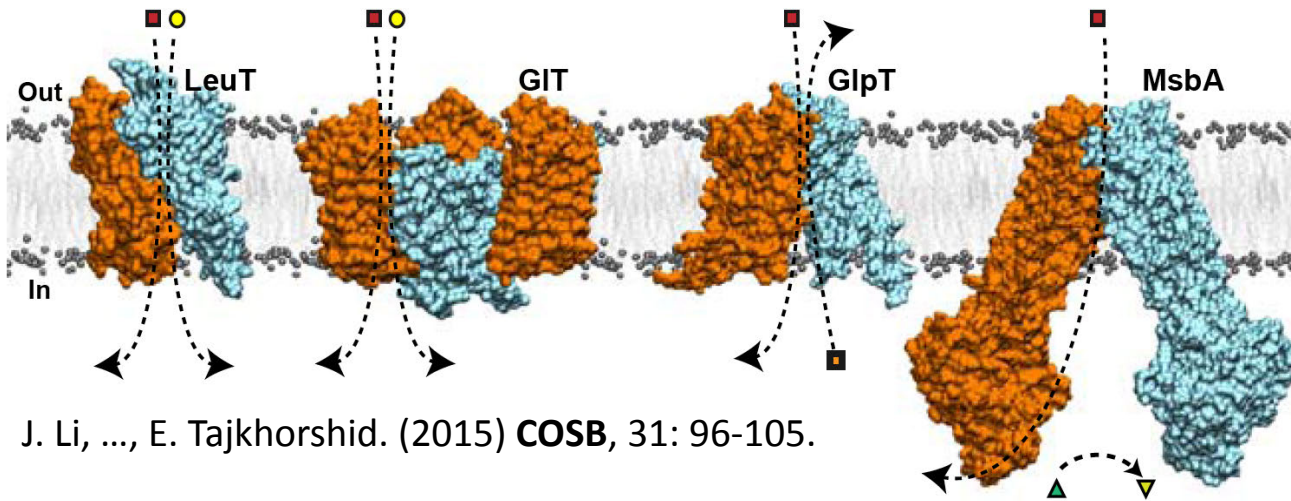


# Could it be simply the size?

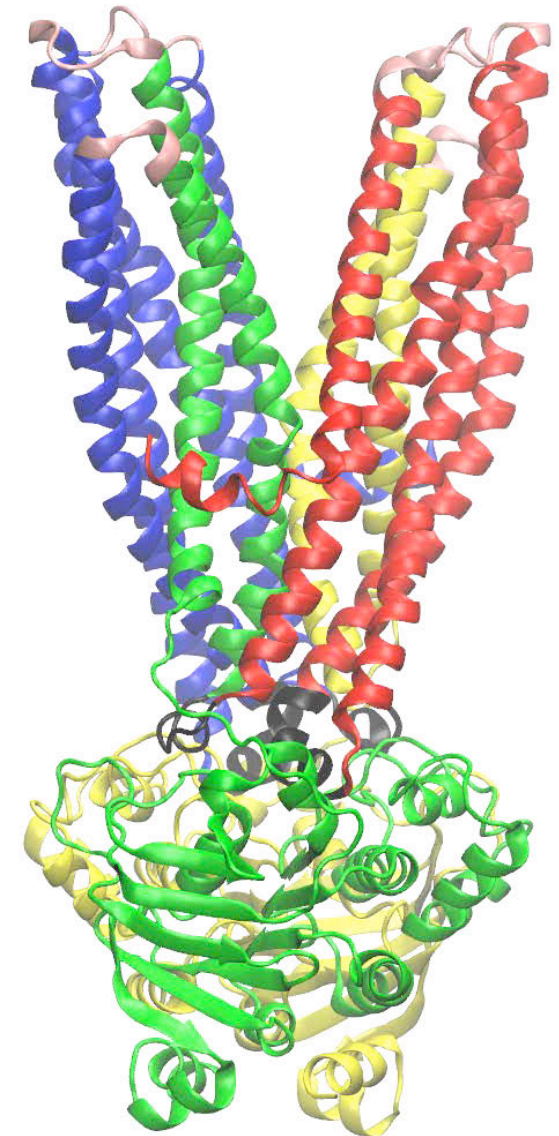


# Battling the Timescale - Case II

## Biased (nonequilibrium) simulations



J. Li, ..., E. Tajkhorshid. (2015) *COSB*, 31: 96-105.



### ◆ Neurotransmitter Uptake

» Norepinephrine, serotonin, dopamine, glutamate,...

### ◆ Gastrointestinal Tract

» Active absorption of nutrients  
» Secretion of ions

### ◆ Kidneys

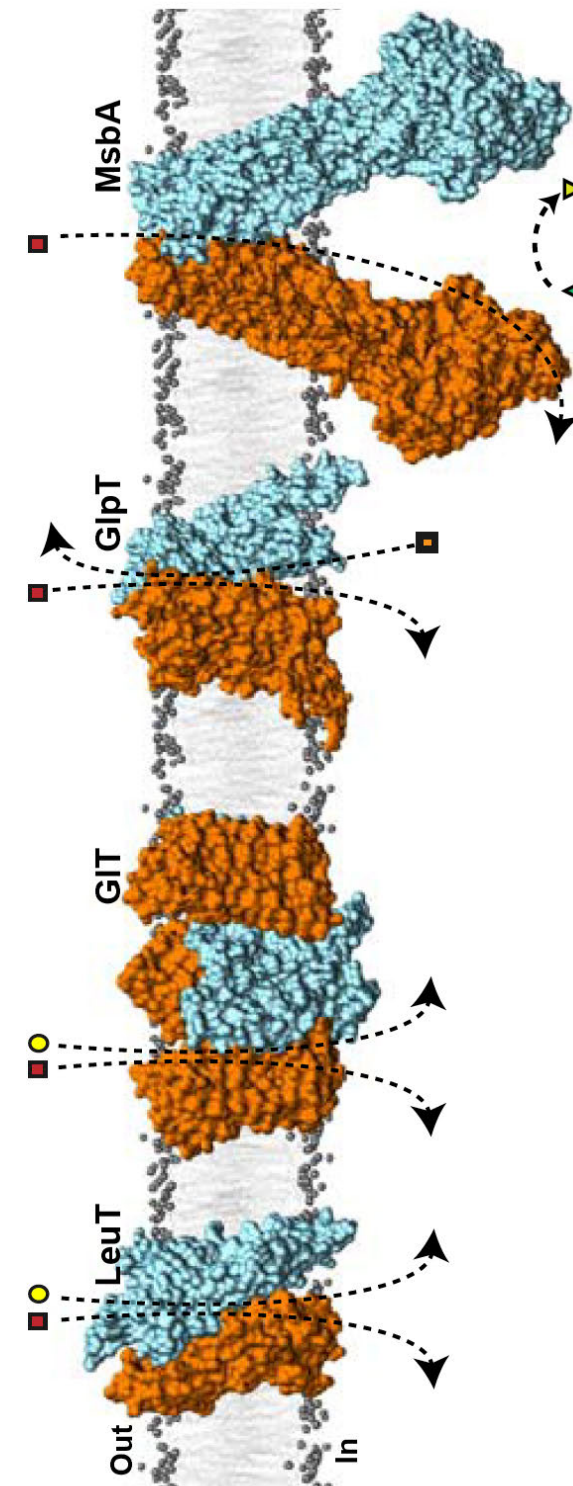
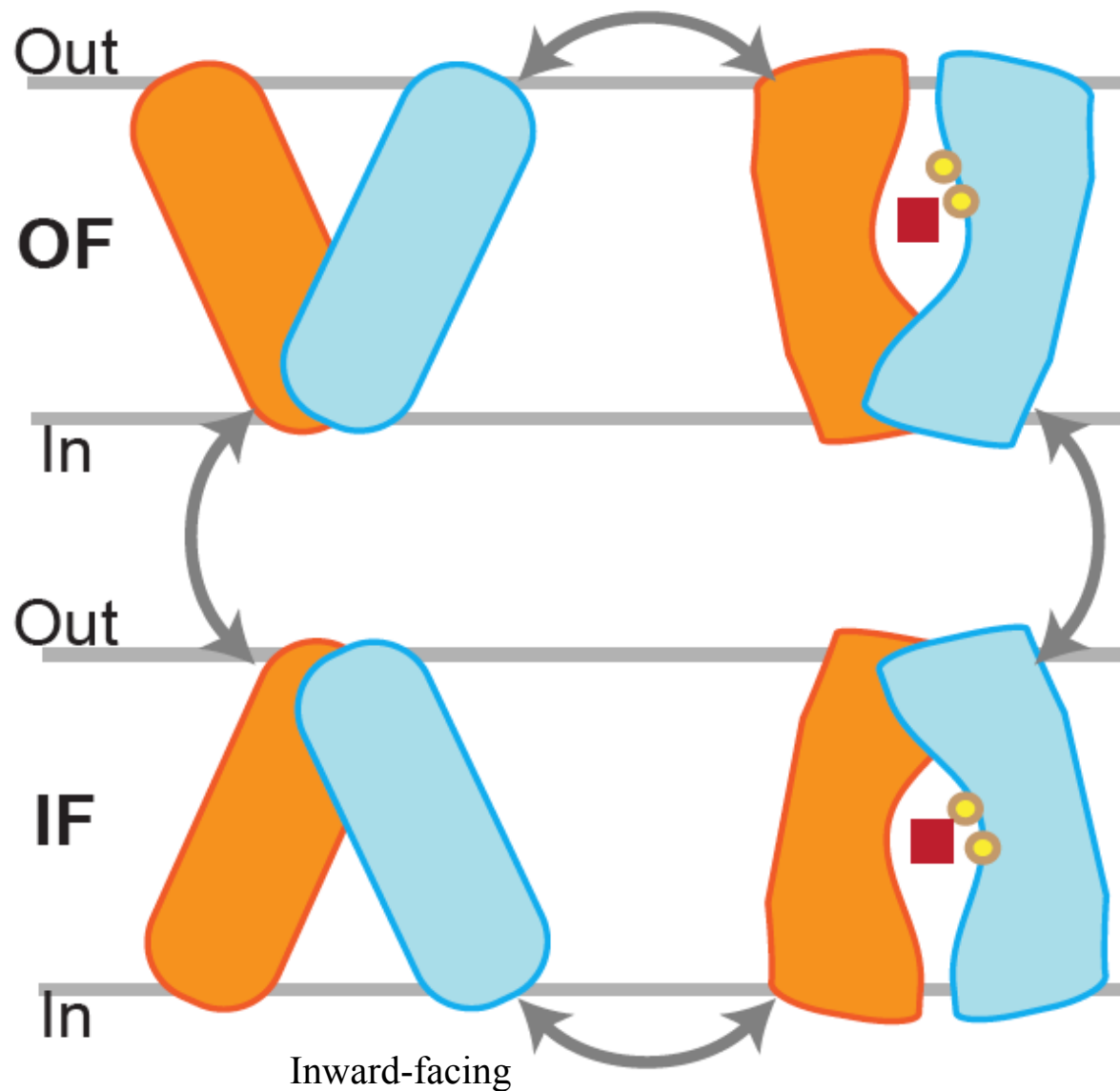
» Reabsorption  
» Secretion

### ◆ Pharmacokinetics of all drugs

» Absorption, distribution, elimination  
» Multi-drug resistance in cancer cells

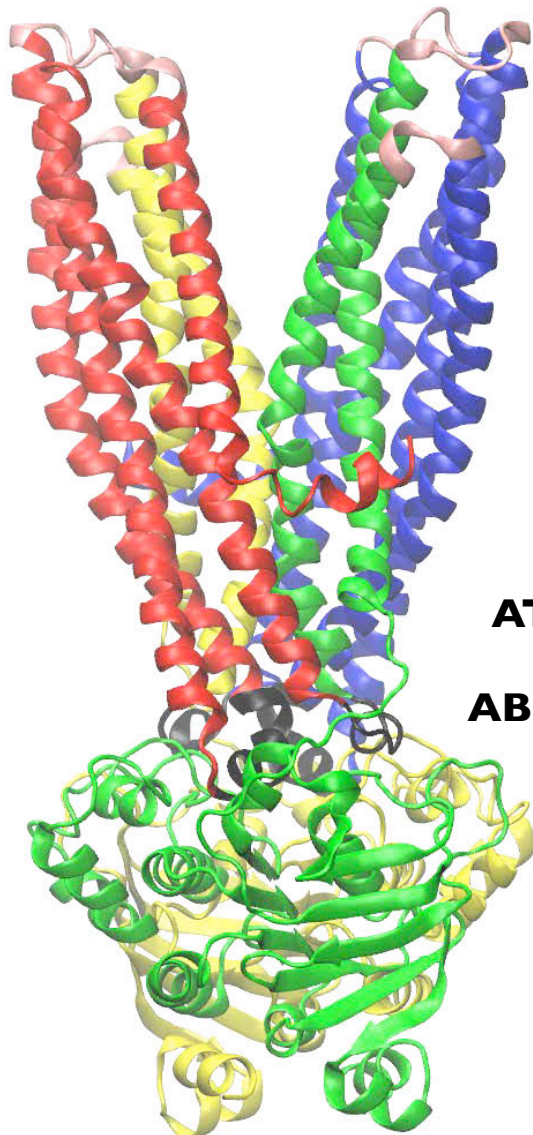
# Alternating Access Mechanism

Outward-facing

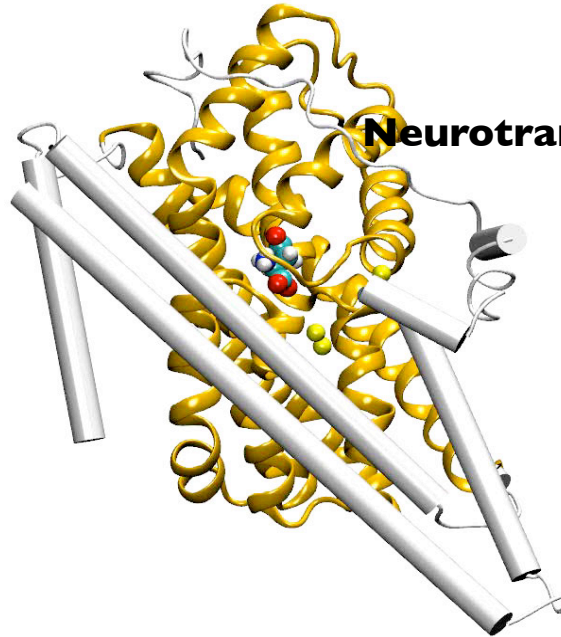


**COMPLEX**

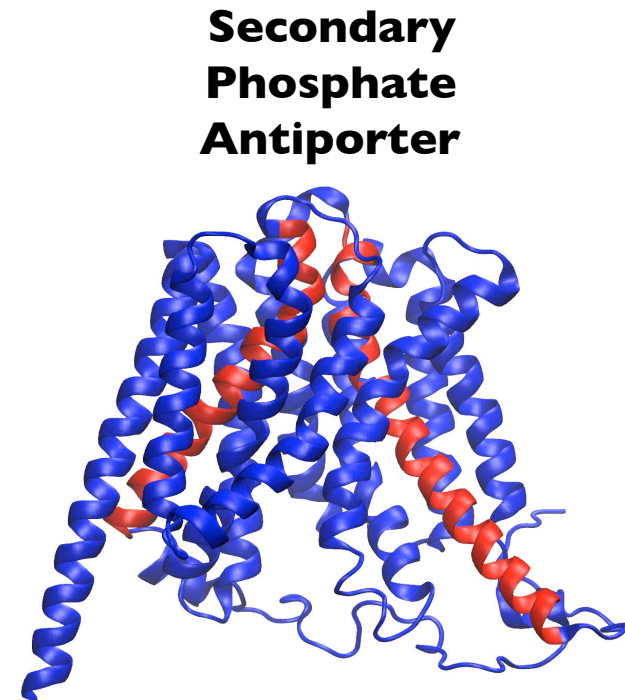
# Diverse Structural Transitions Involved



**ATP-Driven  
Primary  
ABC Exporter**



**Na-coupled  
Secondary  
Neurotransmitter Transporter**



**Secondary  
Phosphate  
Antiporter**

**NON-EQUILIBRIUM METHODS ARE REQUIRED.**



# Complex Processes Require Complex Treatments

## I.1 Defining Practical Collective Variables

Empirical search for practical collective variables for inducing the conformational changes involved in the transition.

## I.2 Optimizing the Biasing Protocols

Systematic search for a practical biasing protocol by using different combinations of collective variables.

## II. Optimizing the Transition Pathway

Use all of the conformations available to generate the most reliable transition pathway:  
1. Bayesian approach for combining the data  
2. Post-hoc string method (analysis tool)  
3. String method with swarms of trajectories

## III.1 Free Energy Calculations

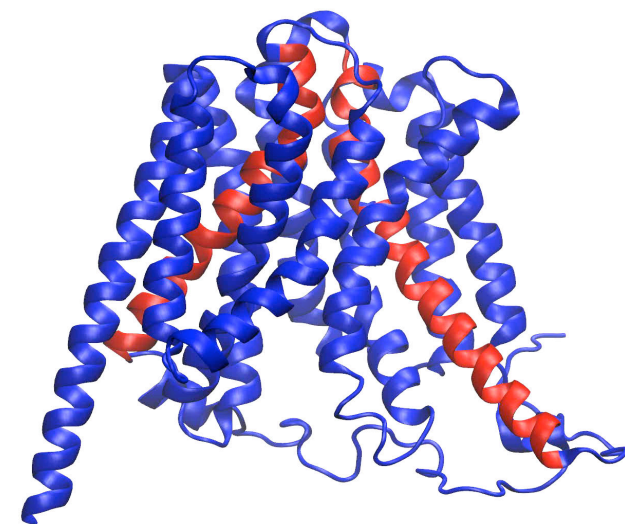
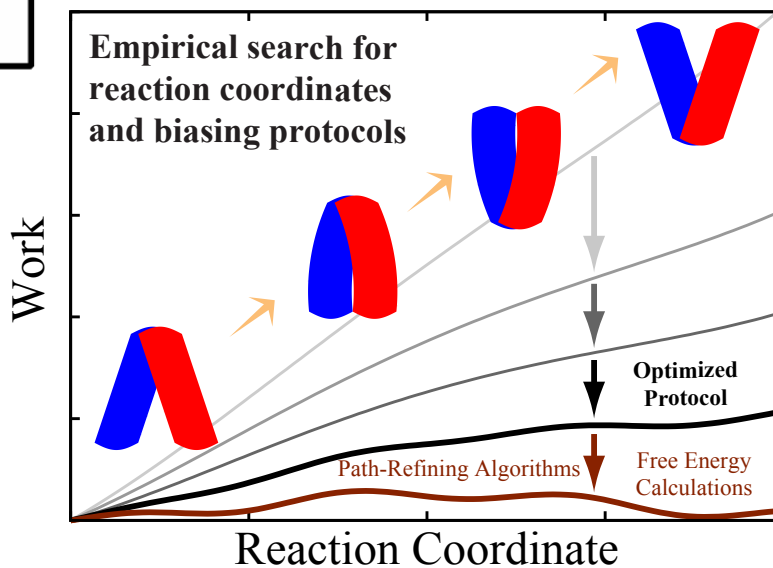
Using the most relevant collective variables (from I.1), biasing protocol (from I.2), and initial conformations (from I.2).

## III.2 Assessing the Sampling Efficiency

Detecting the poorly sampled, but potentially important regions, e.g., by using PCA.



**Mahmoud Moradi**

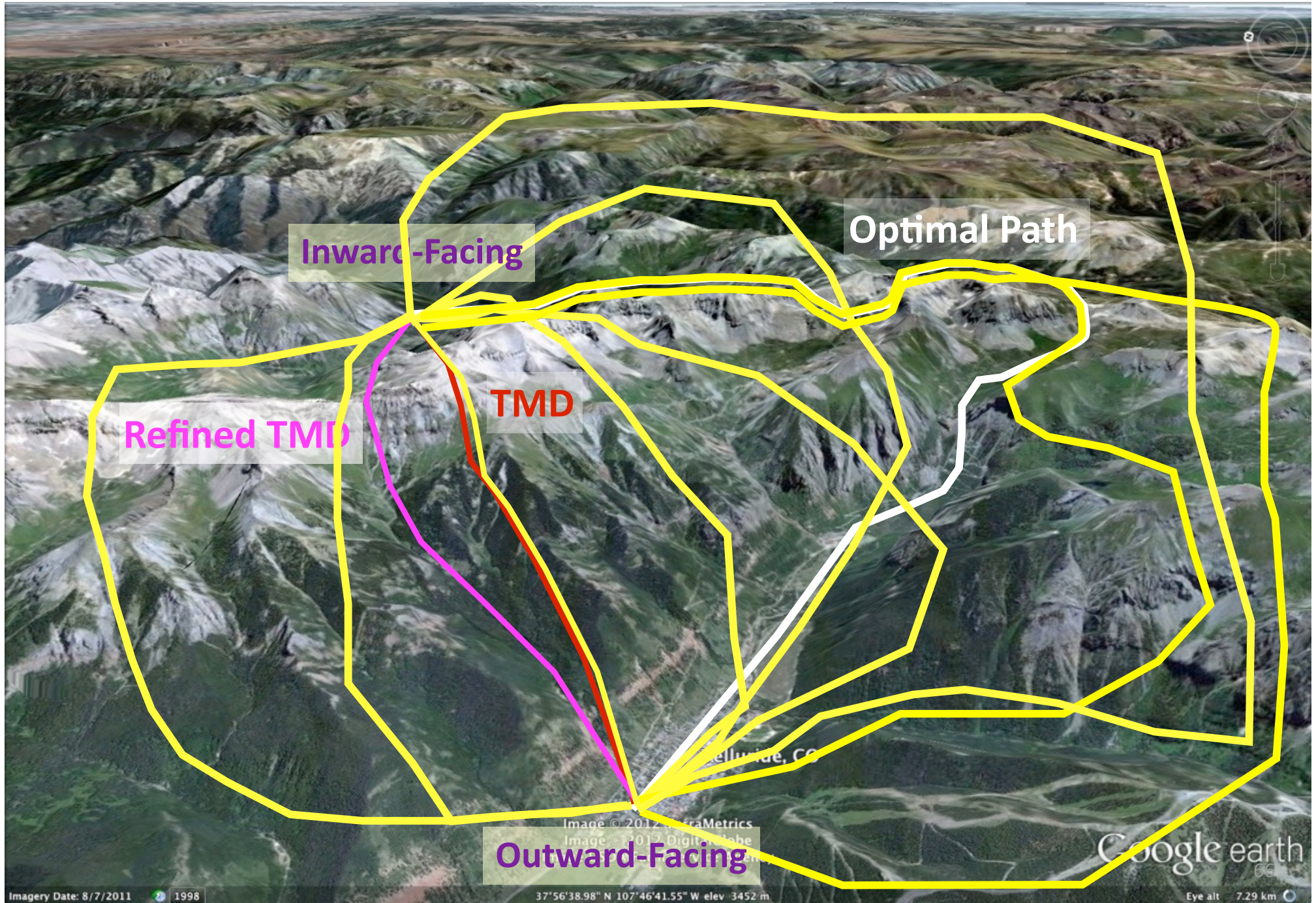


M. Moradi and ET (2013) *PNAS*, 110:18916–18921.

M. Moradi and ET (2014) *JCTC*, 10: 2866–2880.

M. Moradi, G. Enkavi, and ET (2015) *Nature Comm.*, 6:8393.

# Aggressive Search of the Space



# Non-equilibrium Driven Molecular Dynamics:

Applying a time-dependent external force to induce the transition

Along various pathways/mechanisms (collective variables)

Harmonic constant      Initial state

$$U_{dr}(\mathbf{x}, t) = \frac{1}{2}k \left( \xi(\mathbf{x}) - \xi_A + (\xi_B - \xi_A) \frac{t}{T} \right)^2$$

Biassing potential      Final state      Total simulation time

**Collective variables:  
RMSD, distance,  
R<sub>g</sub>, angle, ...  
orientation quaternion**

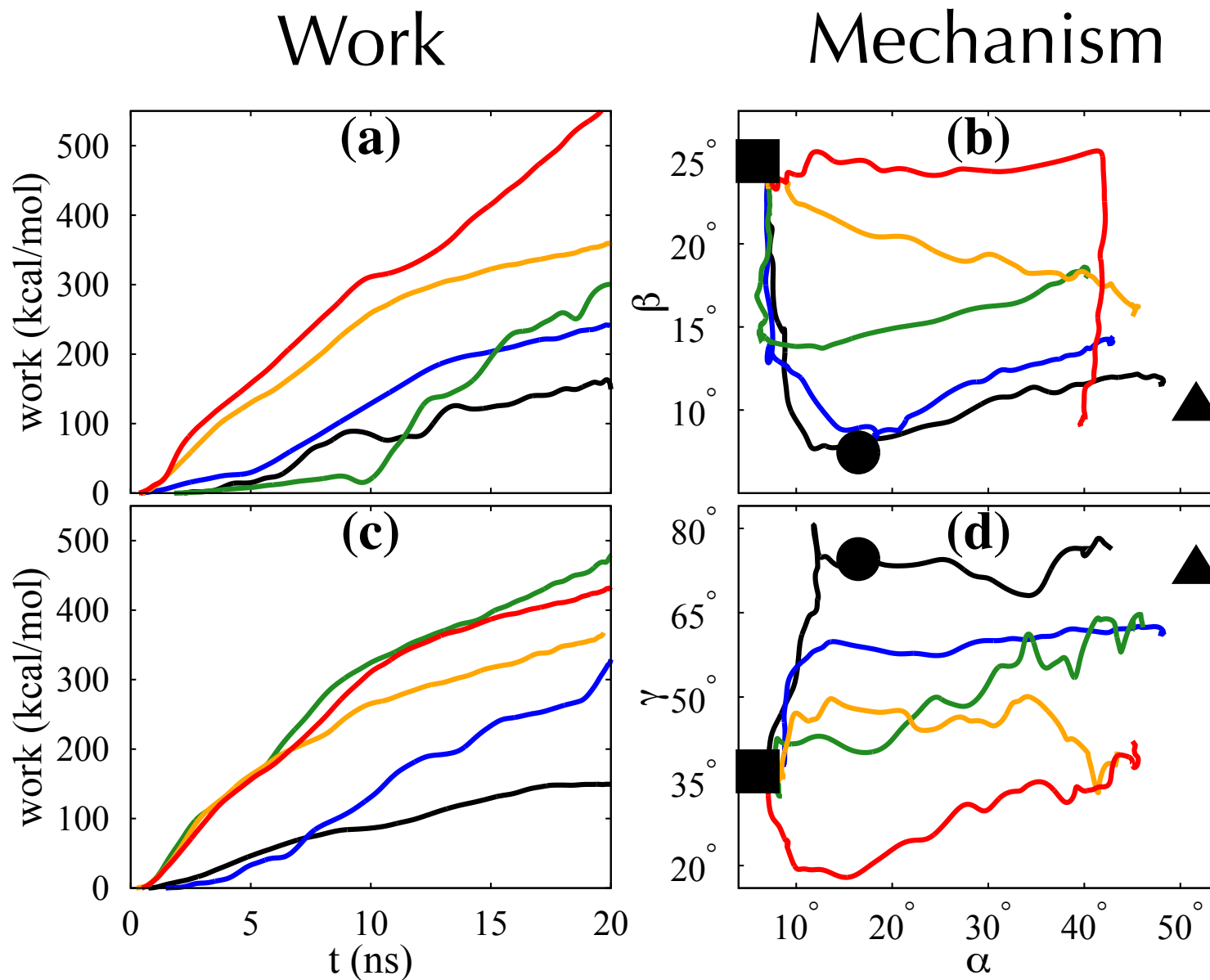
The diagram illustrates the biasing potential  $U_{dr}(\mathbf{x}, t)$  used in non-equilibrium driven molecular dynamics. The equation is  $U_{dr}(\mathbf{x}, t) = \frac{1}{2}k \left( \xi(\mathbf{x}) - \xi_A + (\xi_B - \xi_A) \frac{t}{T} \right)^2$ . Labels with arrows point to various parts of the equation: 'Harmonic constant' points to  $k$ ; 'Initial state' points to  $\xi_A$ ; 'Final state' points to  $\xi_B$ ; 'Total simulation time' points to  $T$ ; and 'Biassing potential' points to the entire equation. A red box highlights the collective variables: RMSD, distance, R<sub>g</sub>, angle, and orientation quaternion, which are associated with the  $\xi$  terms in the equation.

M. Moradi and ET (2013) **PNAS**, 110:18916–18921.

M. Moradi and ET (2014) **JCTC**, 10: 2866–2880.

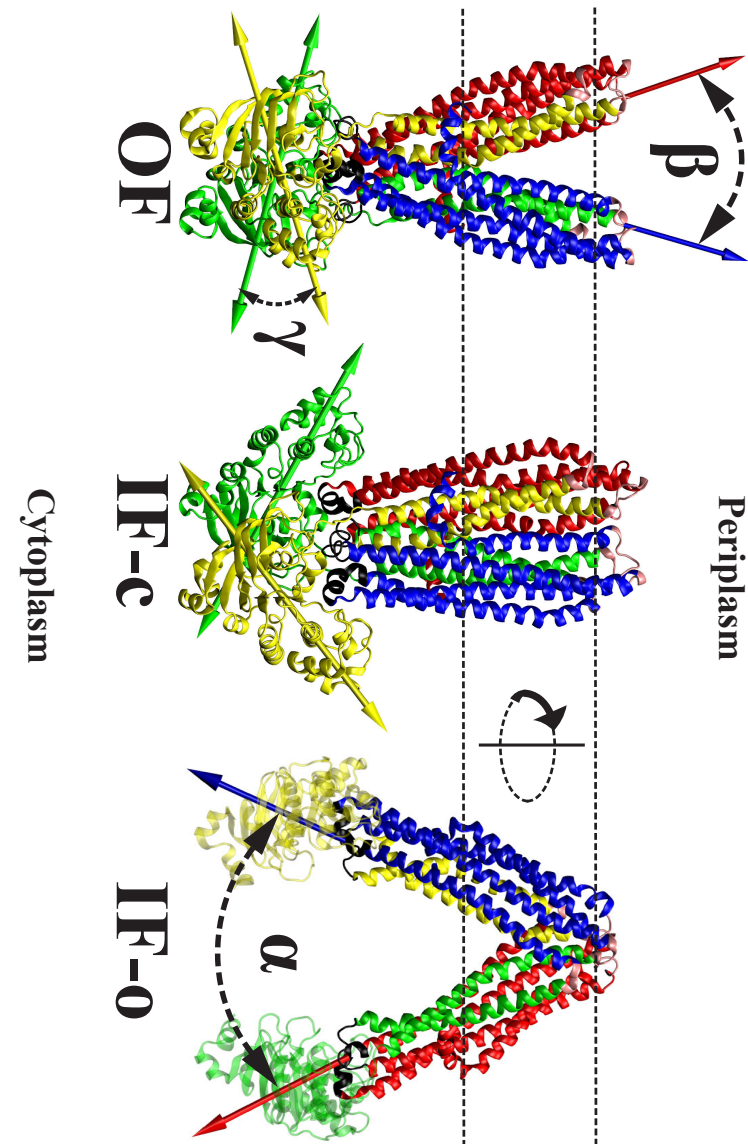
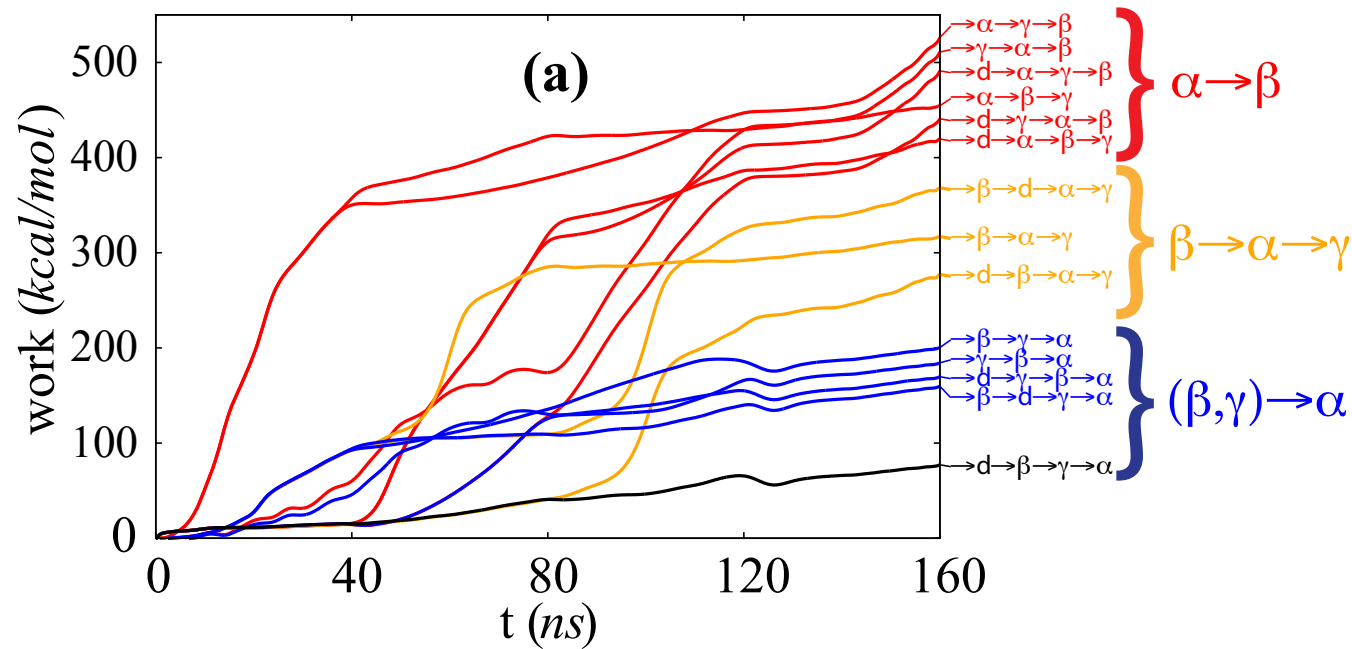
M. Moradi, G. Enkavi, and ET (2015) **Nature Comm.**, 6:8393.

# Progressively Optimizing the Biasing Protocol/Collective Variable using non-Equilibrium Work as a Measure of the Path Quality



Example set taken from a subset of 20 ns biased simulations

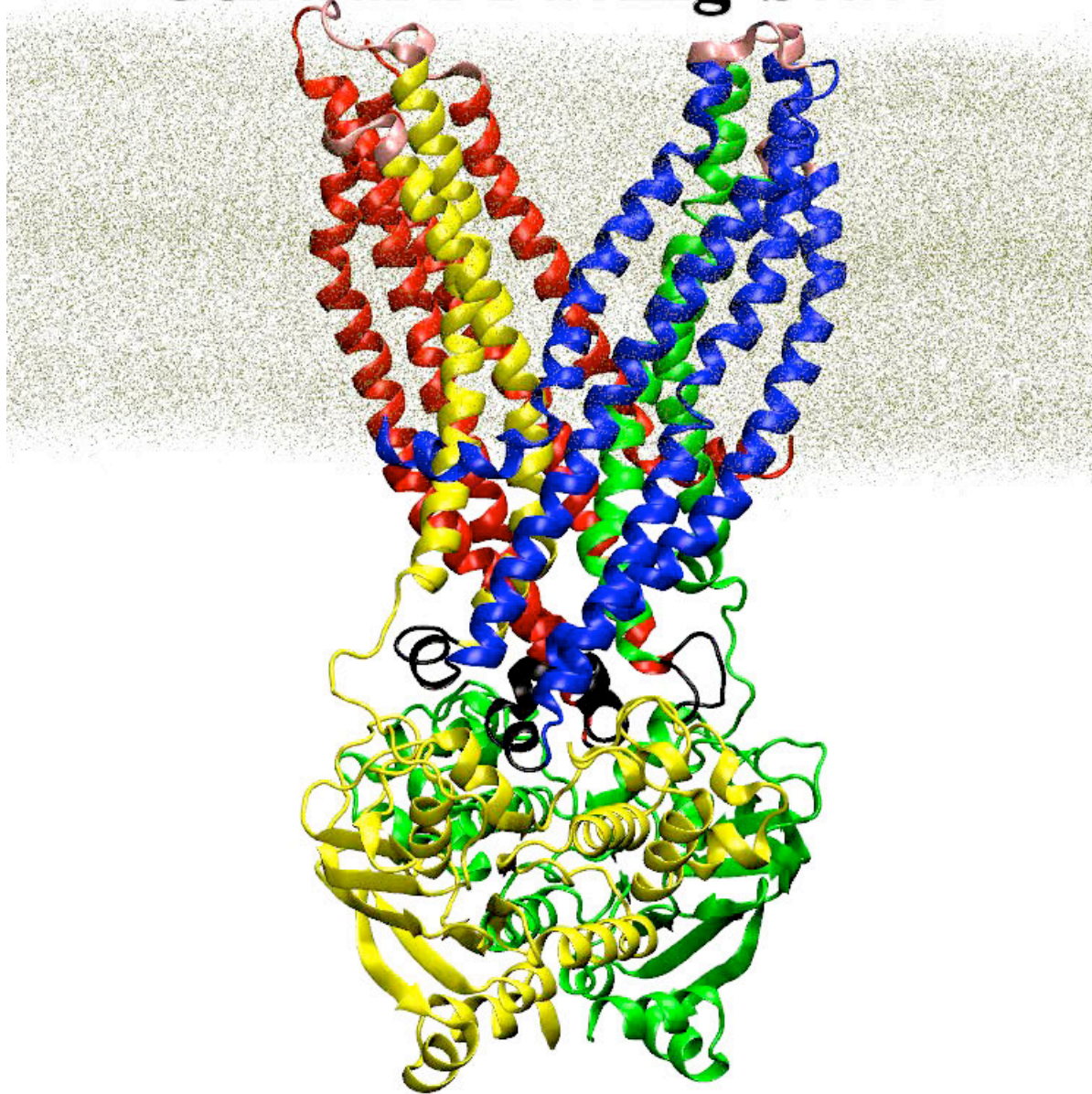
# Mechanistic Insight From Transition Pathways in ABC exporters from Non-Equilibrium Simulations



M. Moradi and ET (2013) **PNAS**, 110:18916–18921.

M. Moradi and ET (2014) **JCTC**, 10: 2866–2880.

# Outward-Facing State



**OF** → **IF**

NBD Dissociation



Periplasmic Closure



NBD Twist



Cytoplasmic Opening



**IF** → **OF**

Cytoplasmic Closure



NBD Twist



Periplasmic Opening



NBD Dimerization

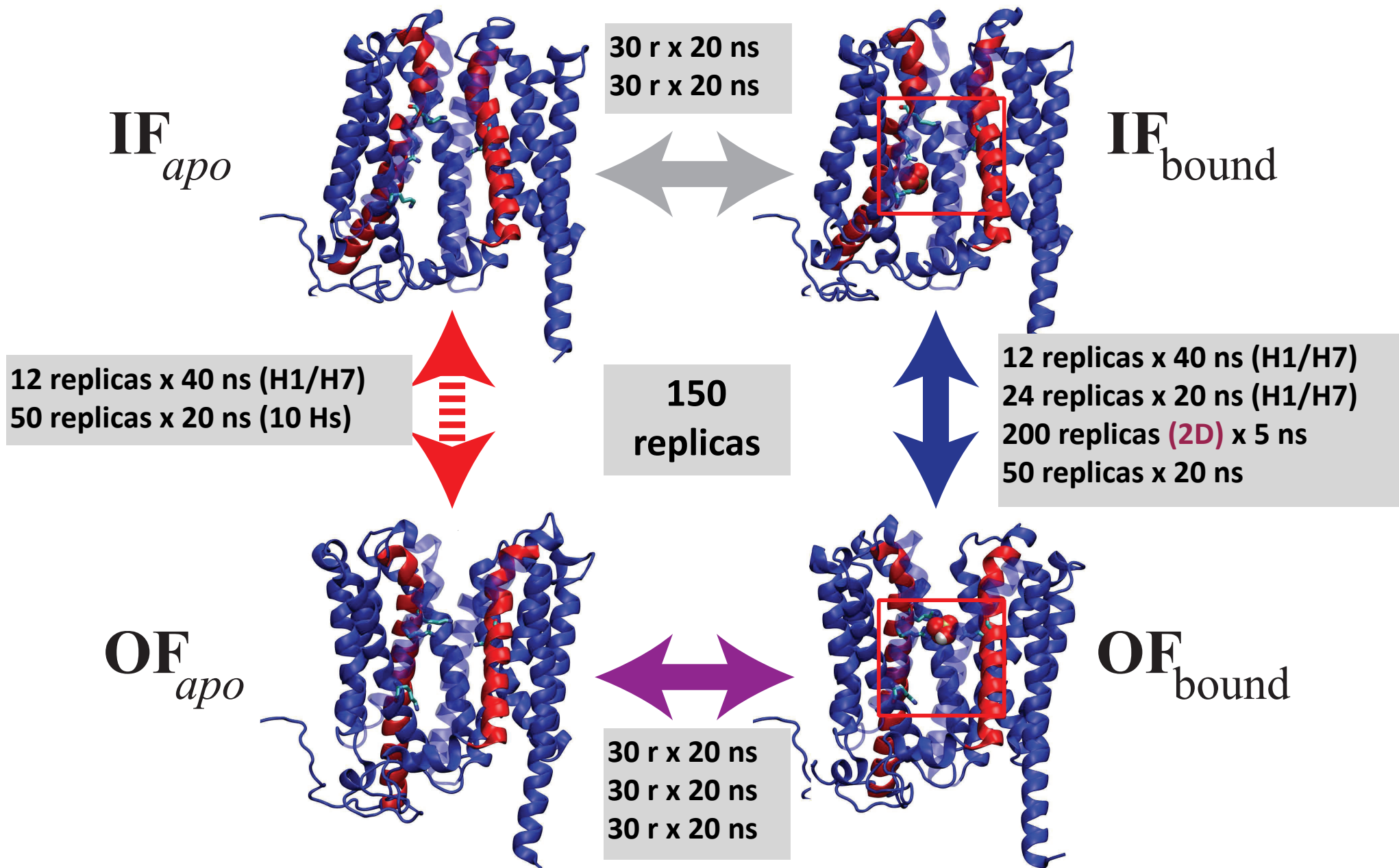


**T** Transition    **R** Relaxation

## NBD Doorknob Mechanism

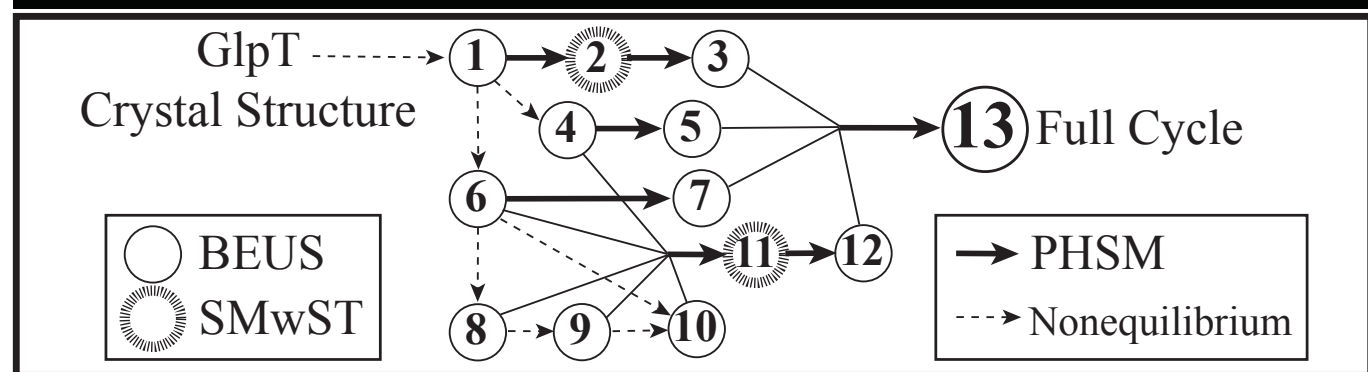
M. Moradi and ET (2013) *PNAS*, 110:18916–18921.

# Describing a Complete Cycle (Adding Substrate) Requiring a Combination of **Multiple Collective Variables**

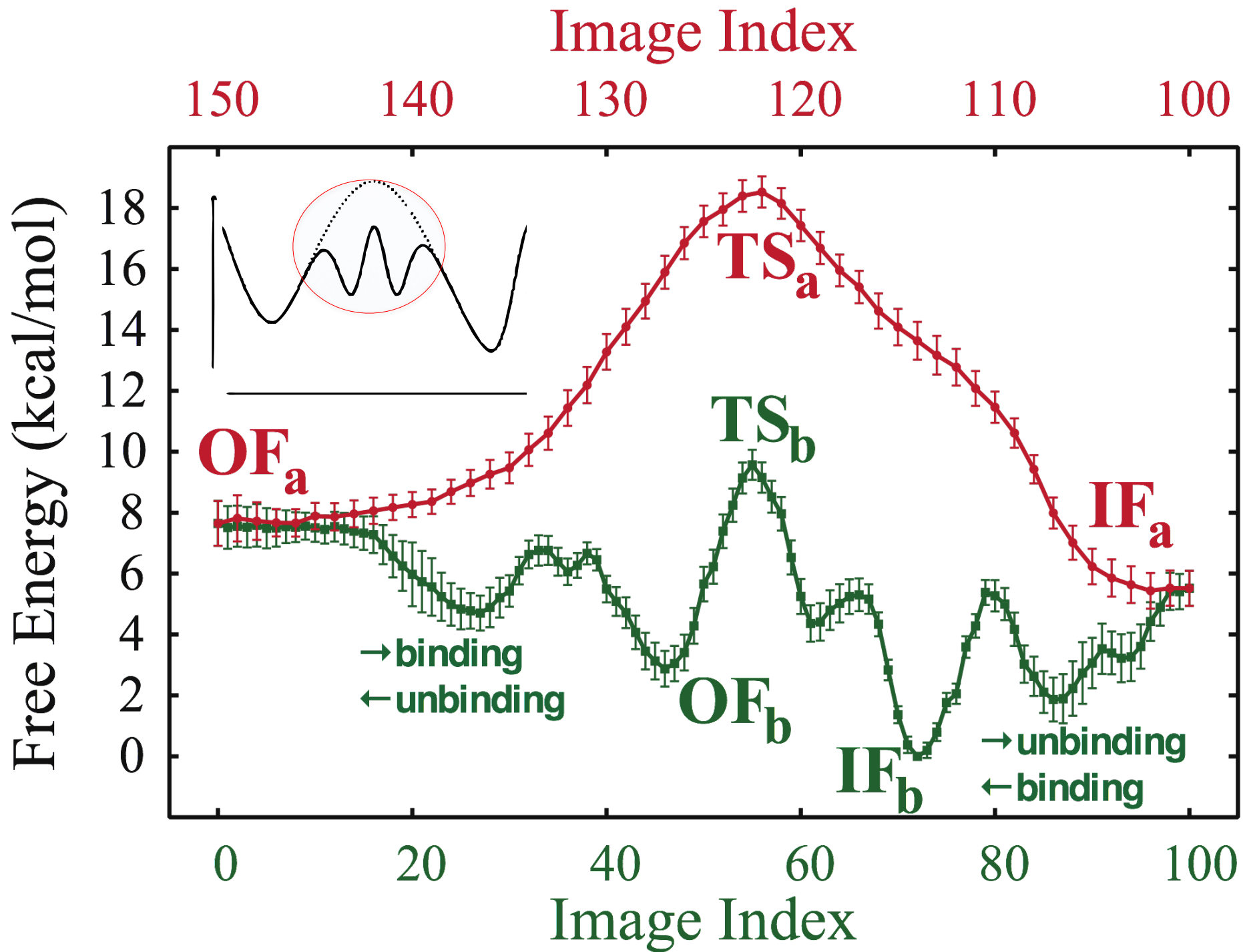


# Simulation protocols

	Transition	Technique	Collective Variables	# of Replicas × Runtime
1	$IF_a \leftrightarrow OF_a$	BEUS	$(Q_1, Q_7)$	$12 \times 40 \text{ ns} = 0.5 \mu\text{s}$
2		SMwST	$\{Q\}$	$1000 \times 1 \text{ ns} = 1 \mu\text{s}$
3		BEUS	$\{Q\}$	$50 \times 20 \text{ ns} = 1 \mu\text{s}$
4	$IF_a \leftrightarrow IF_b$	BEUS	$Z_{Pi}$	$30 \times 40 \text{ ns} = 1.2 \mu\text{s}$
5		BEUS	$(\{Q\}, Z_{Pi})$	$30 \times 40 \text{ ns} = 1.2 \mu\text{s}$
6	$OF_a \leftrightarrow OF_b$	BEUS	$Z_{Pi}$	$30 \times 40 \text{ ns} = 1.2 \mu\text{s}$
7		BEUS	$(\{Q\}, Z_{Pi})$	$30 \times 40 \text{ ns} = 1.2 \mu\text{s}$
8	$IF_b \leftrightarrow OF_b$	BEUS	$(Q_1, Q_7)$	$24 \times 20 \text{ ns} = 0.5 \mu\text{s}$
9		BEUS	$Z_{Pi}$	$15 \times 30 \text{ ns} = 0.5 \mu\text{s}$
10		2D BEUS	$(\Delta\text{RMSD}, Z_{Pi})$	$200 \times 5 \text{ ns} = 1 \mu\text{s}$
11		SMwST	$(\{Q\}, Z_{Pi})$	$1000 \times 1 \text{ ns} = 1 \mu\text{s}$
12		BEUS	$(\{Q\}, Z_{Pi})$	$50 \times 20 \text{ ns} = 1 \mu\text{s}$
13		<b>Full Cycle</b>	BEUS	$(\{Q\}, Z_{Pi})$
<b>Total Simulation Time</b>				<b>18.7 <math>\mu\text{s}</math></b>





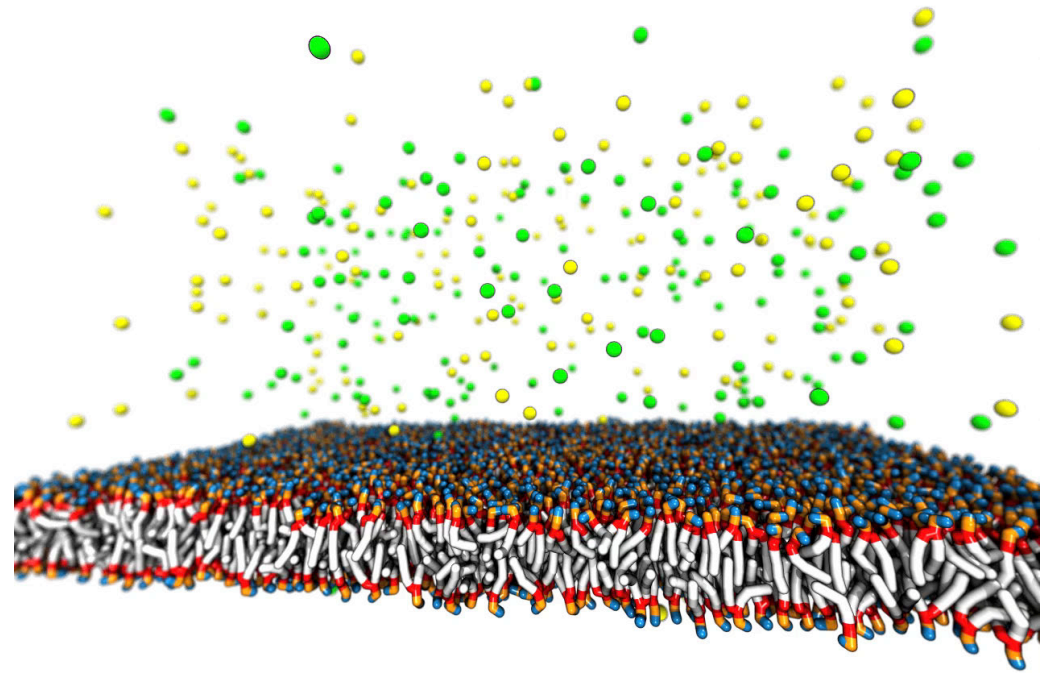


# Battling the Timescale - Case III

## Multiscale Simulations



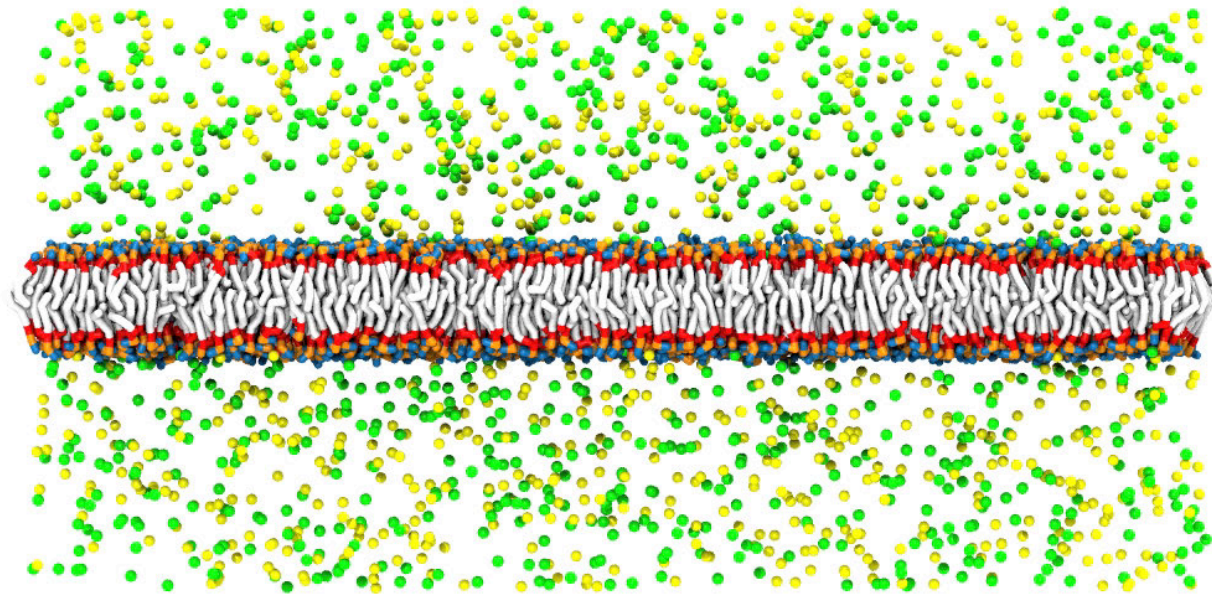
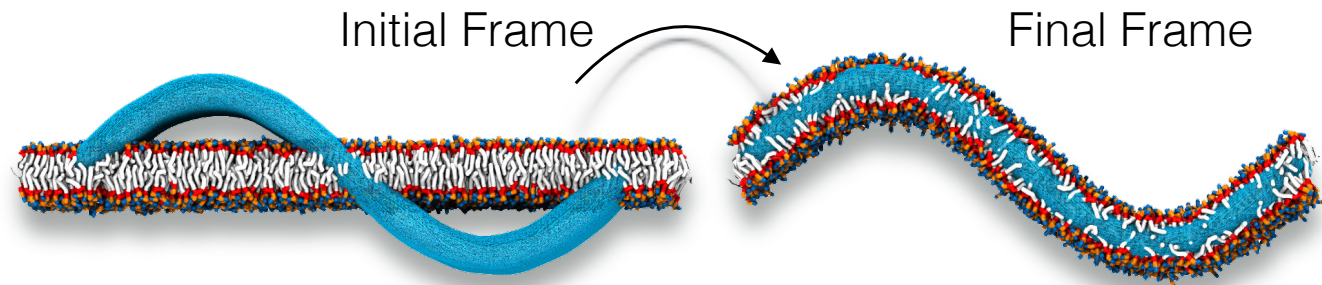
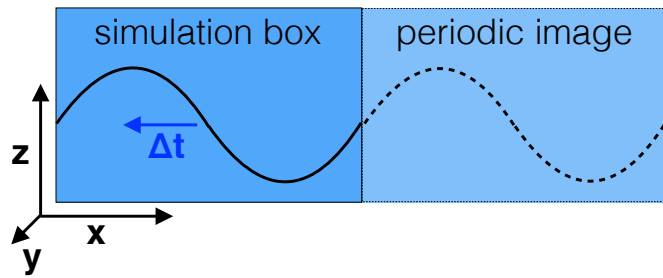
Membrane Budding/Fusion



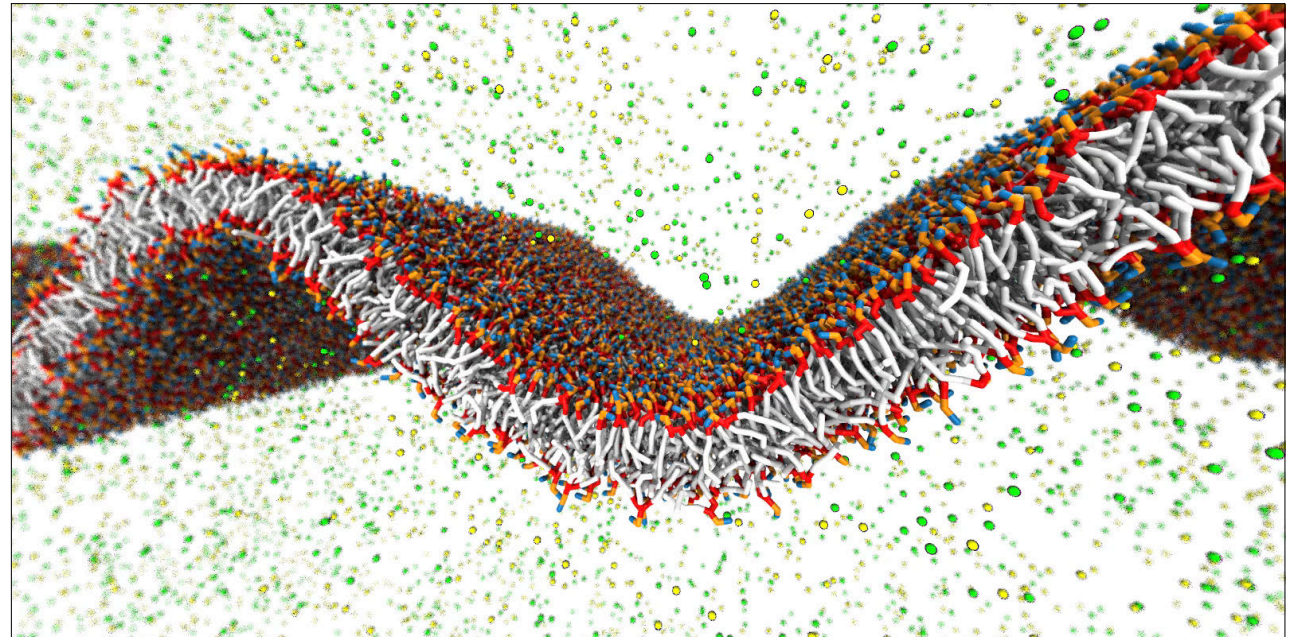
Combining multiple replica simulations and coarse-grained models to describe membrane fusion

# Workflow for Multi-Scale Modeling

Parametrically Defined Sine Function



# Workflow for Multi-Scale Modeling



# Battling the Timescale - Case IV

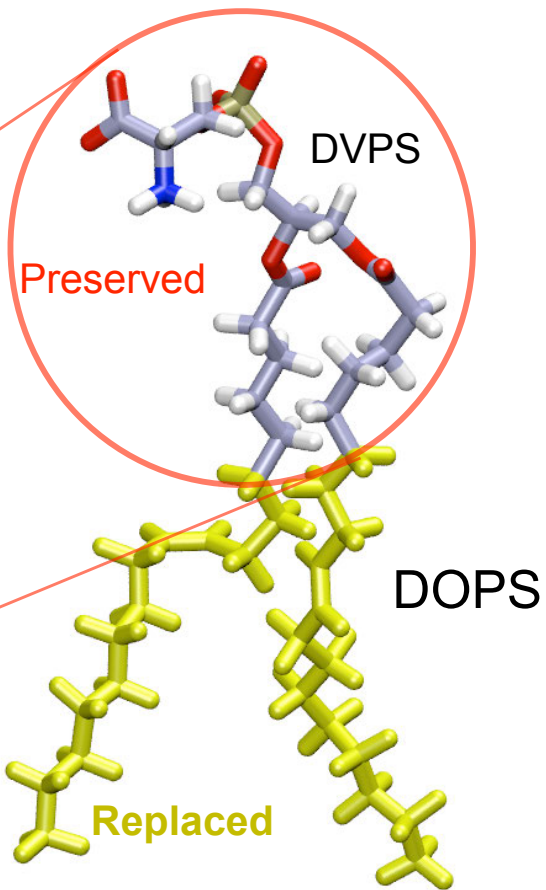
## Reduced Representations

Highly Mobile Membrane Mimetic model

Full model

HMMM model

Tails replaced by organic solvent



### Advantages

- Increased mobility of lipids
- Retain explicit headgroups allowing for atomic details

Biophys. J., 102: 2130-2139 (2012) (Cover Article)



Zenmei Ohkubo



Mark Arcario



Taras Pogorelov

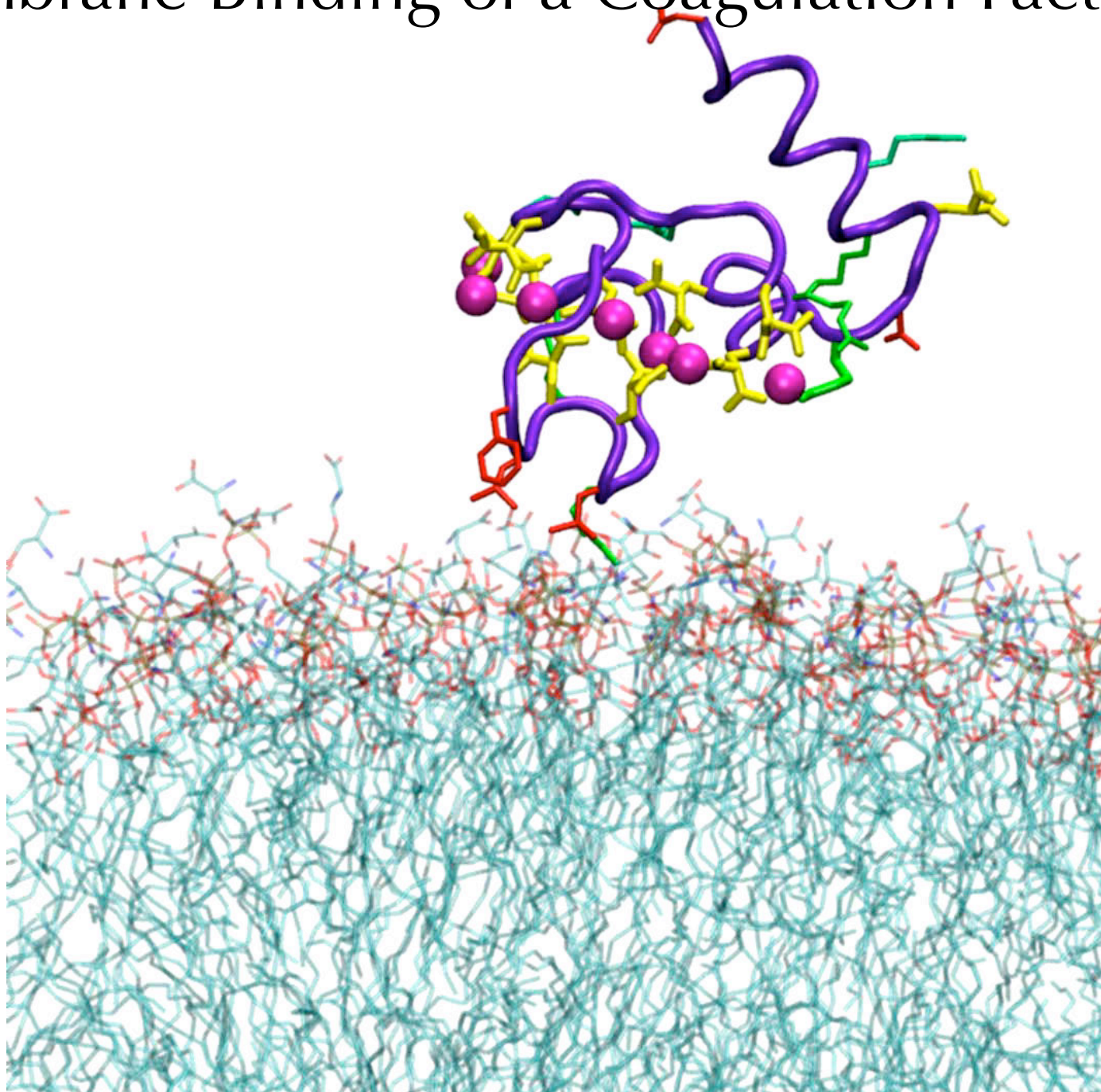


Josh Vermaas



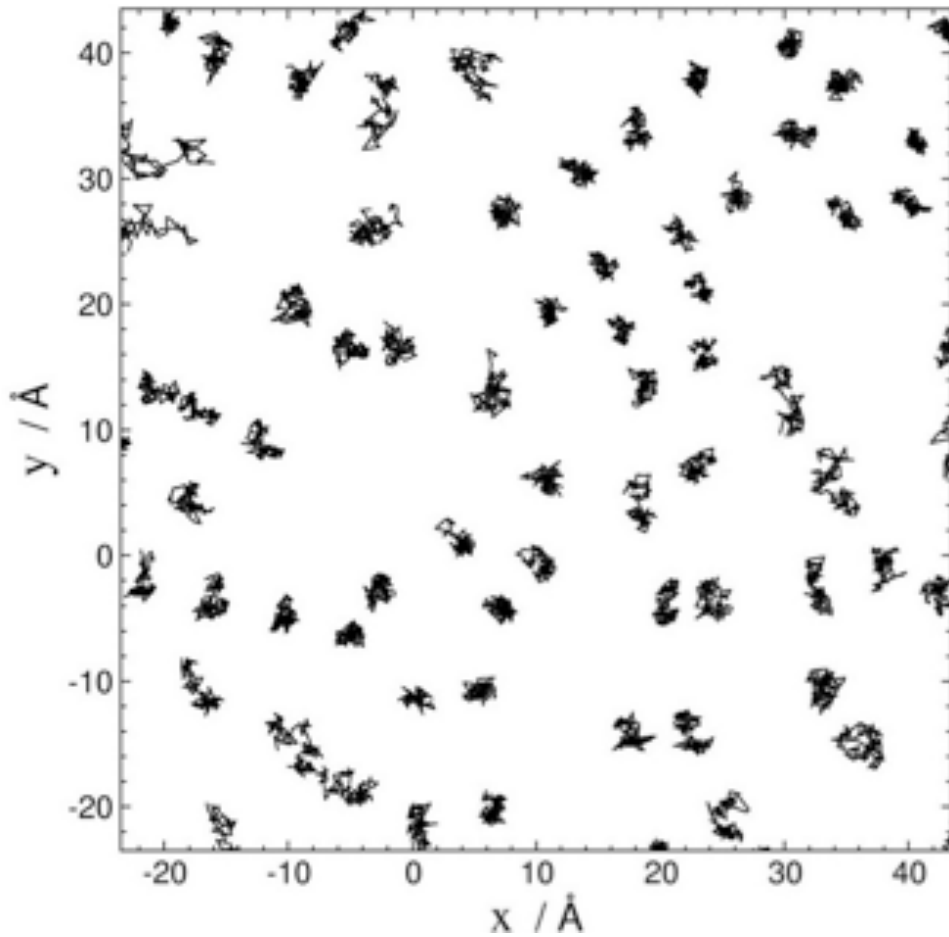
Javier Baylon

# Membrane Binding of a Coagulation Factor

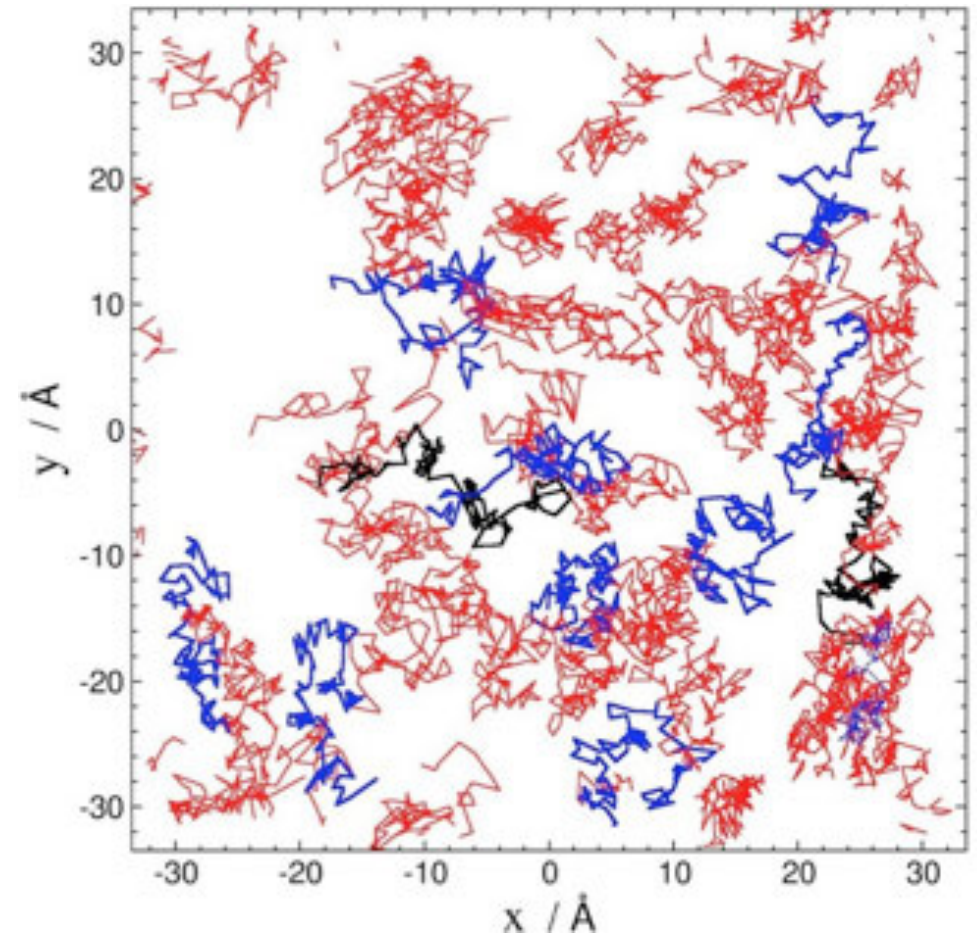


# Enhanced Lipid Lateral Diffusion

*Without Compromising Atomic Details of the Headgroups*



Conventional membrane (10 ns)

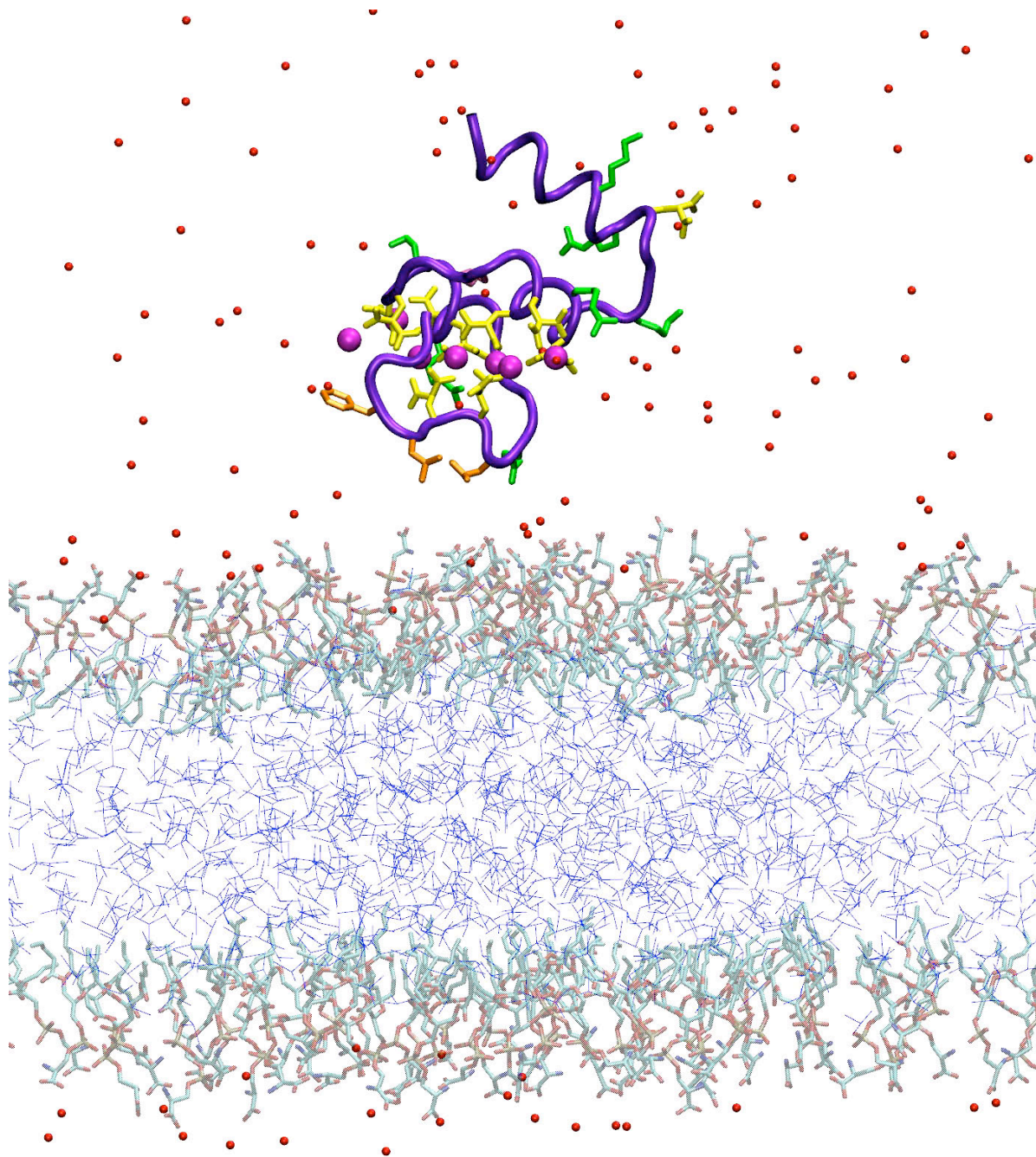


HMMM membrane (1 ns)

# PS-Dependent Spontaneous Insertion of FVII-GLA

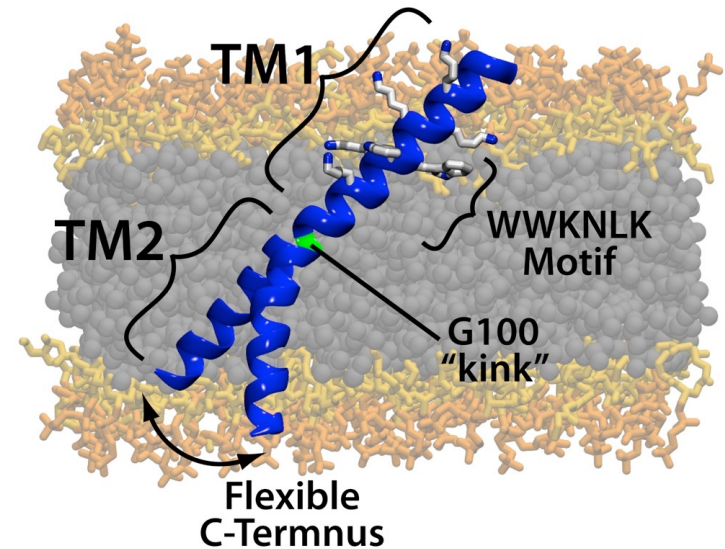
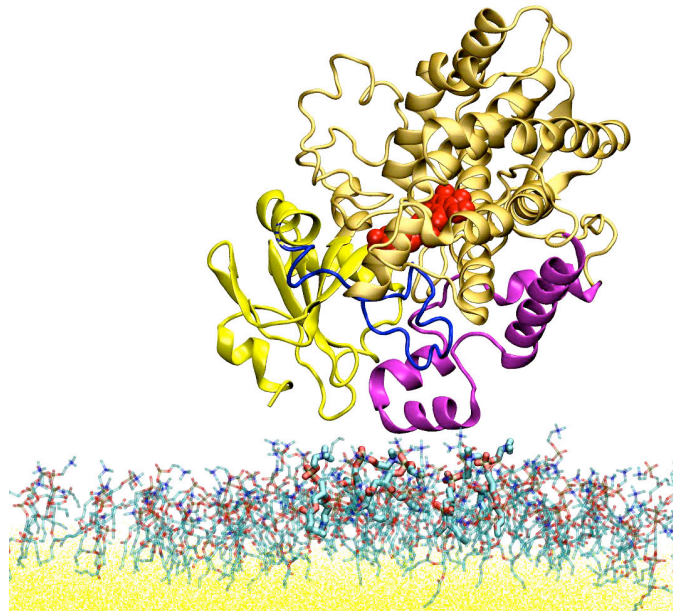
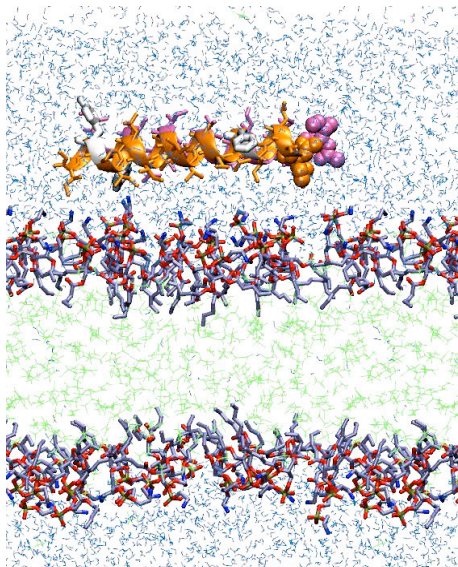
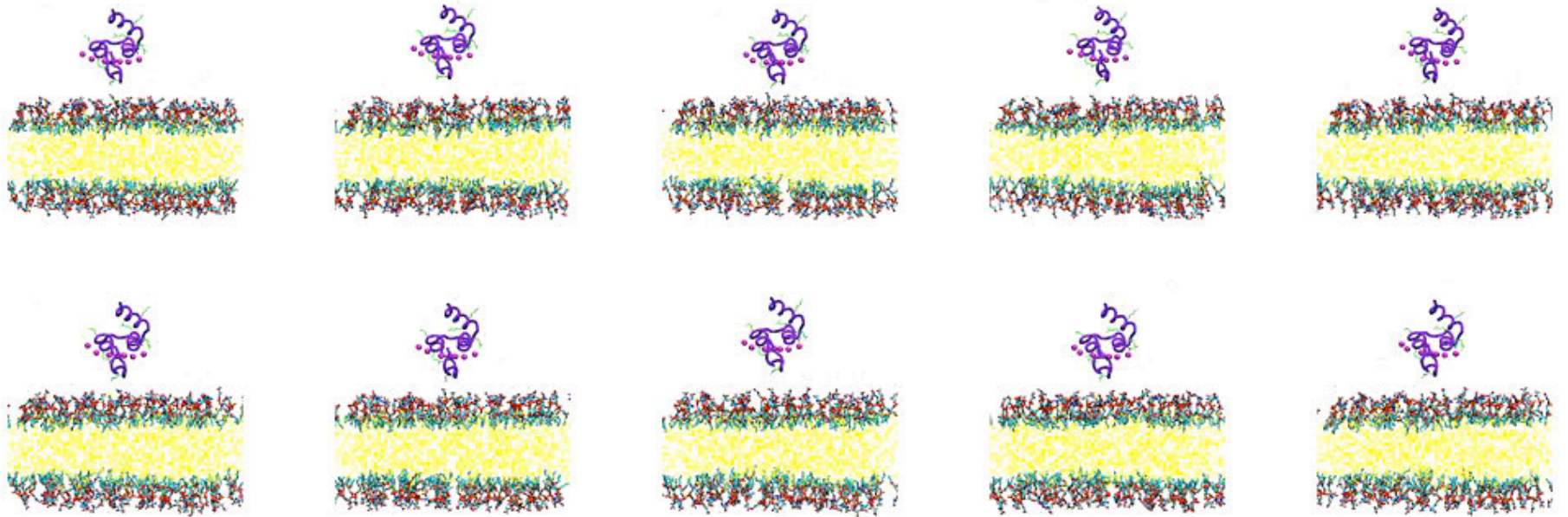


Zenmei Ohkubo





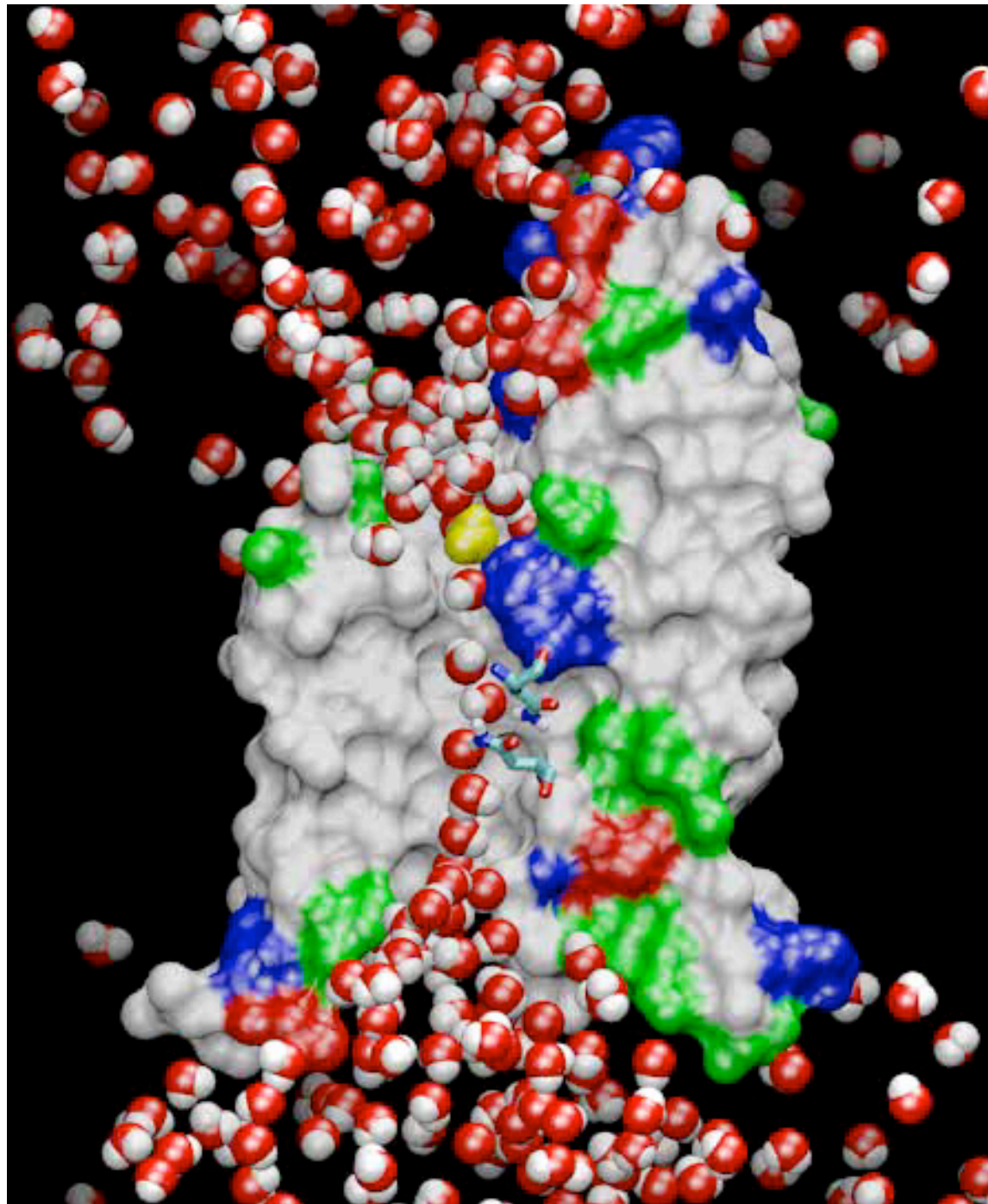
# *HMMM - More Efficient Computational Model for Membrane Proteins*



## R E M E M B E R:

One of the most useful advantages of simulations over experiments is that you can modify the system as you wish: You can do modifications that are not even possible at all in reality!

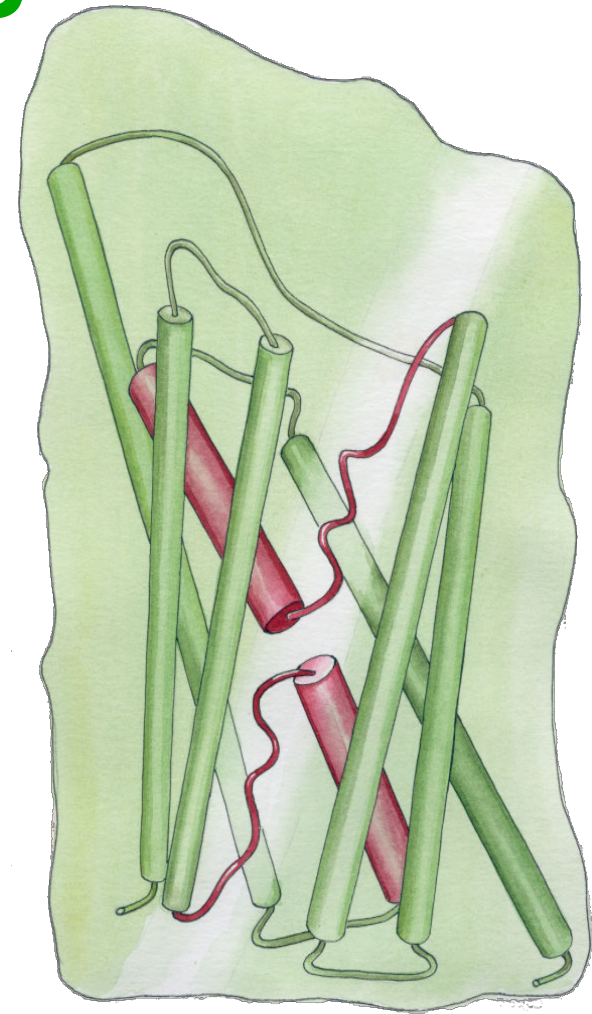
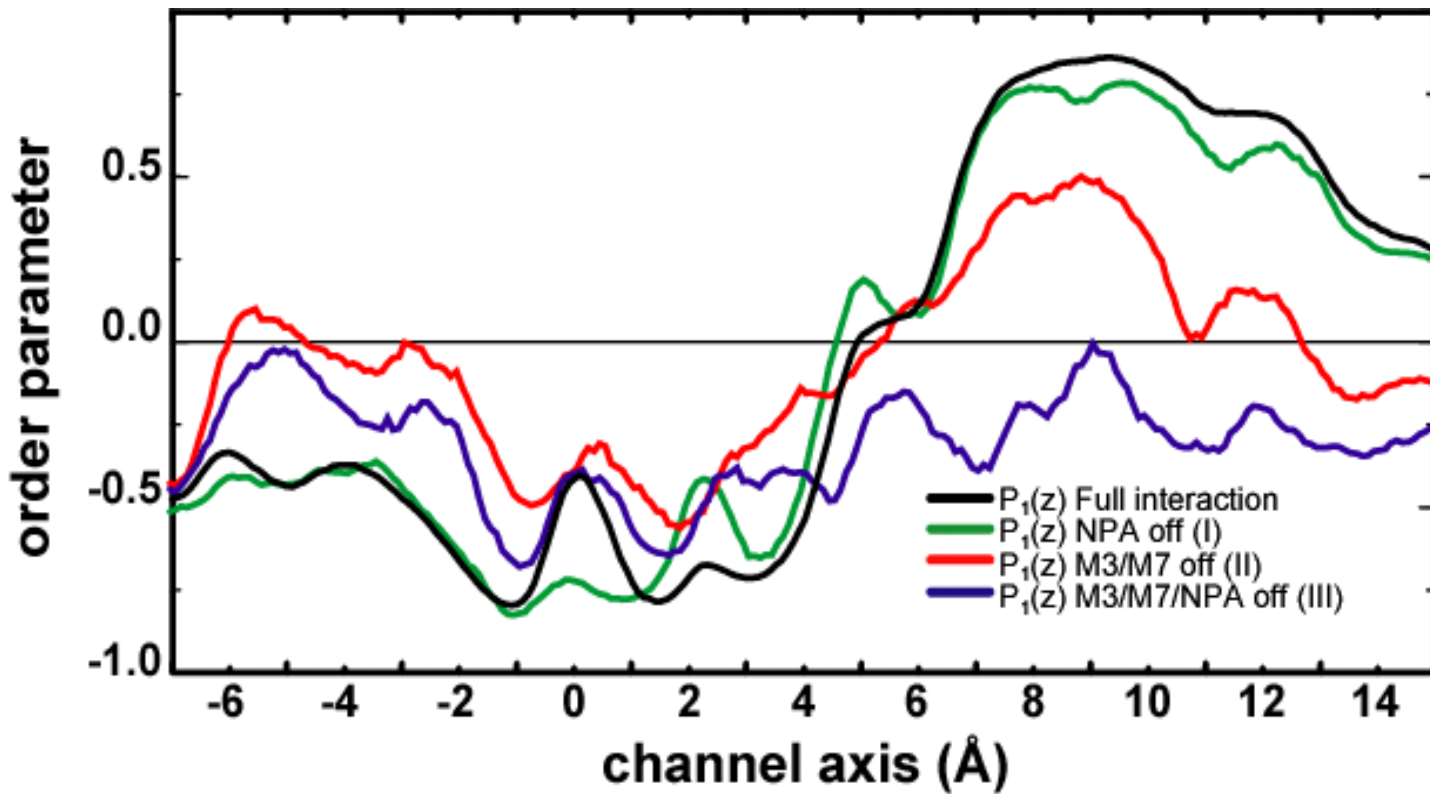
This is a powerful technique to test hypotheses developed during your simulations. **Use it!**



Animation available at the Nobel web site

E. T., et al., **Science** 2002.

# Electrostatic Stabilization of Water Bipolar Arrangement



**channel region (20 Å)**

