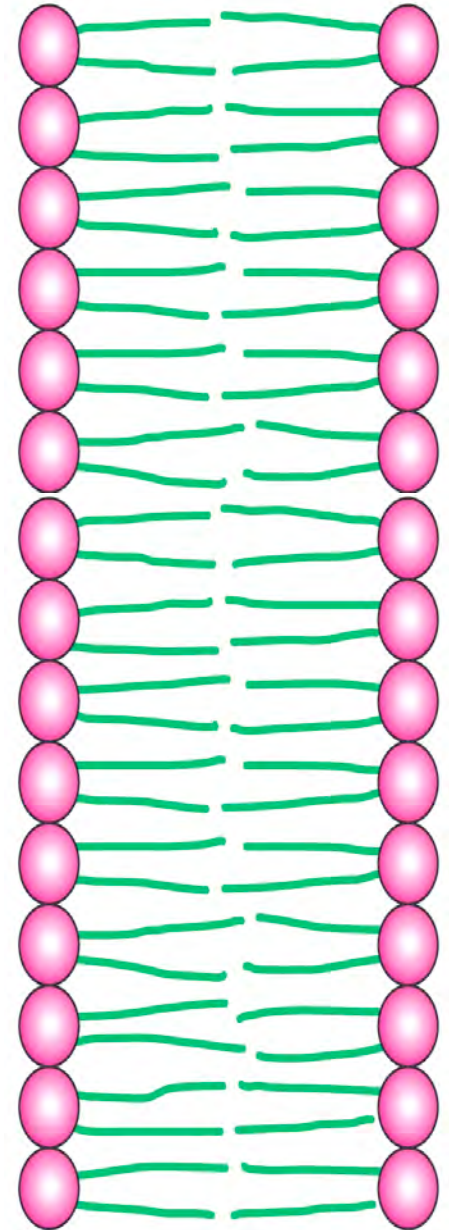
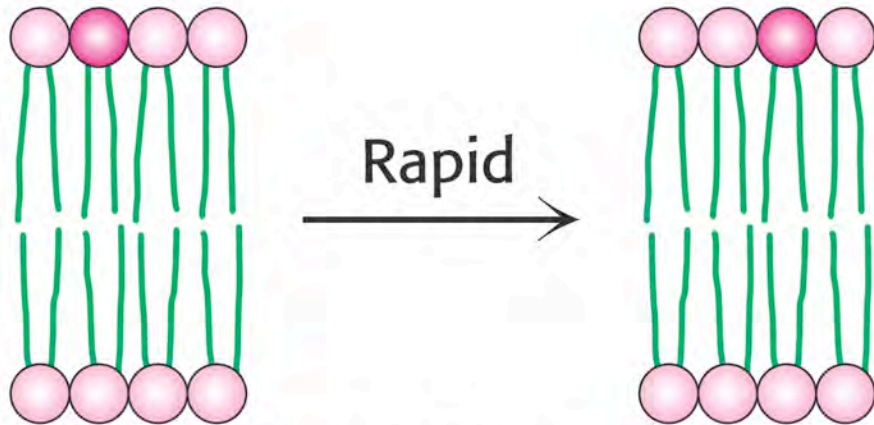


# Lipid Bilayers Are Excellent For Cell Membranes

- Hydrophobic interaction is the driving force
- Self-assembly in water
- Tendency to close on themselves
- Self-sealing (a hole is unfavorable)
- Extensive: up to millimeters



# Lipid Diffusion in Membrane

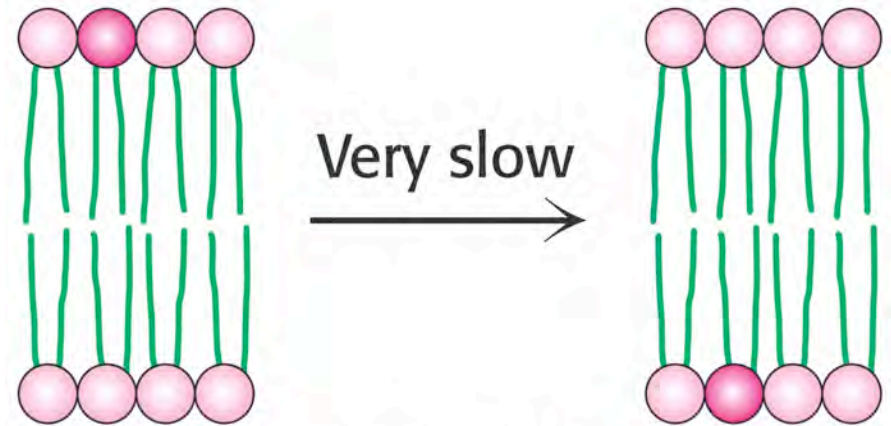


Lateral diffusion

$$D = 1 \mu\text{m}^2 \cdot \text{s}^{-1}$$

$$50 \text{ \AA} \text{ in } \sim 2.5 \times 10^{-5} \text{ s}$$

$$D_{\text{lip}} = 10^{-8} \text{ cm}^2 \cdot \text{s}^{-1}$$
$$D_{\text{wat}} = 2.5 \times 10^{-5} \text{ cm}^2 \cdot \text{s}^{-1}$$



Transverse diffusion  
(flip-flop)

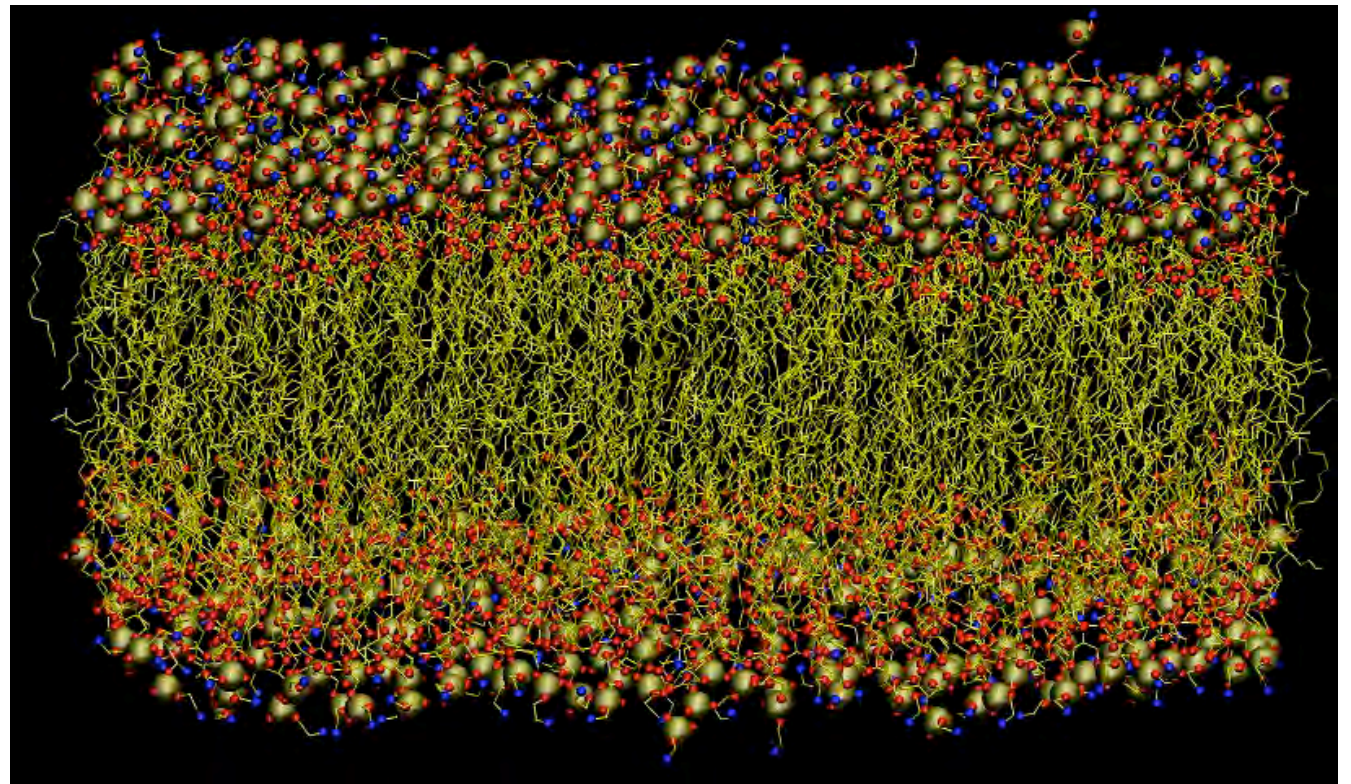
Once in several hours!  
( $10^4 \text{ s}$ )

**~9 orders of magnitude  
difference**

# Technical difficulties in Simulations of Biological Membranes

- Time scale
- Heterogeneity of biological membranes ☹️

60 x 60 Å  
Pure POPE  
5 ns  
~100,000  
atoms



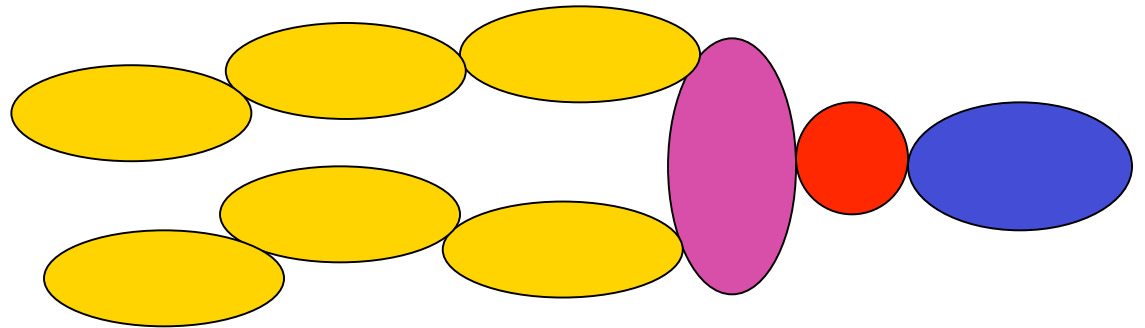
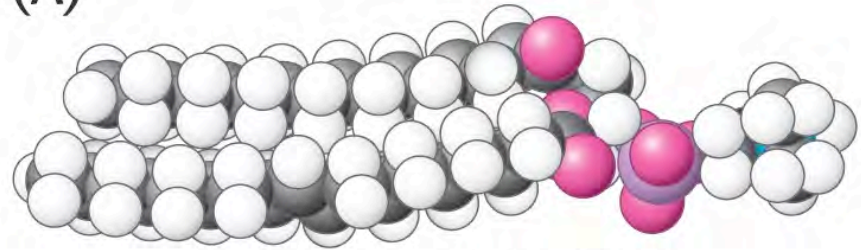
# Coarse grain modeling of lipids

150 particles



9 particles!

(A)



Also, increasing the time step by orders of magnitude.

# Analysis of Molecular Dynamics Simulations of Biomolecules

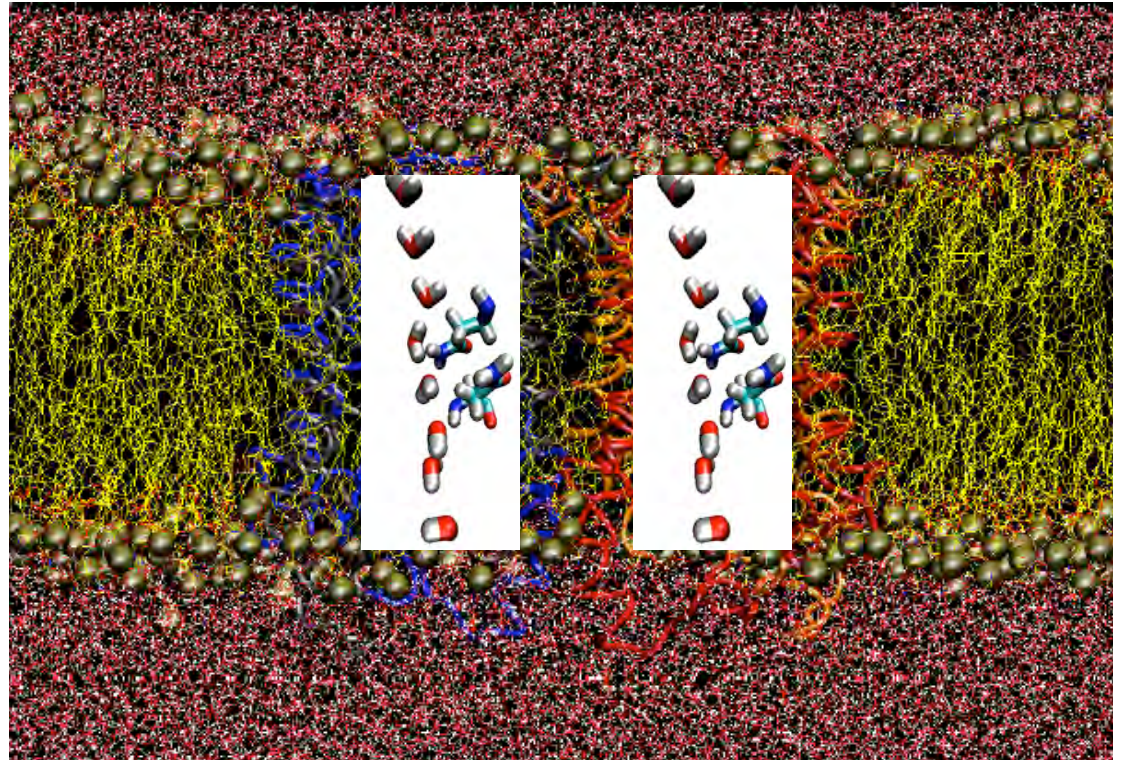
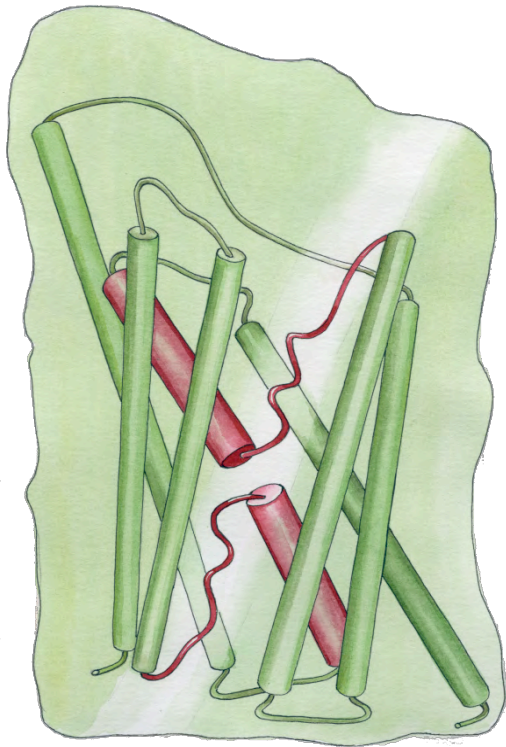
- A very complicated arrangement of hundreds of groups interacting with each other
- Where to start to look at?
- What to analyze?
- How much can we learn from simulations?

It is very important to get acquainted with your system



# Aquaporins

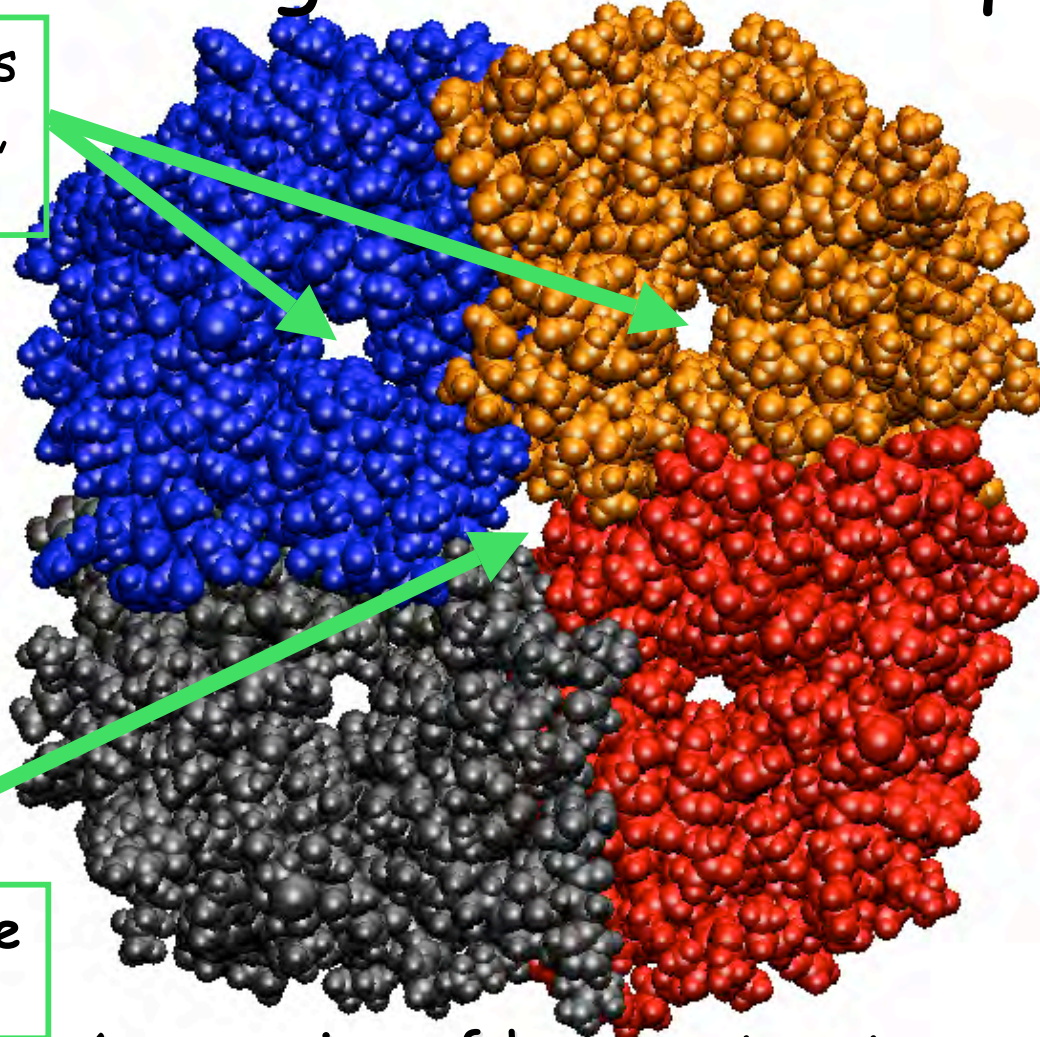
## Membrane water channels





# Structural Organization of Aquaporins

Monomeric pores  
Water, glycerol,  
urea, H<sub>2</sub>S, ...



Tetrameric pore  
????

Aquaporins of known structure:

**GlpF** - E. coli glycerol channel

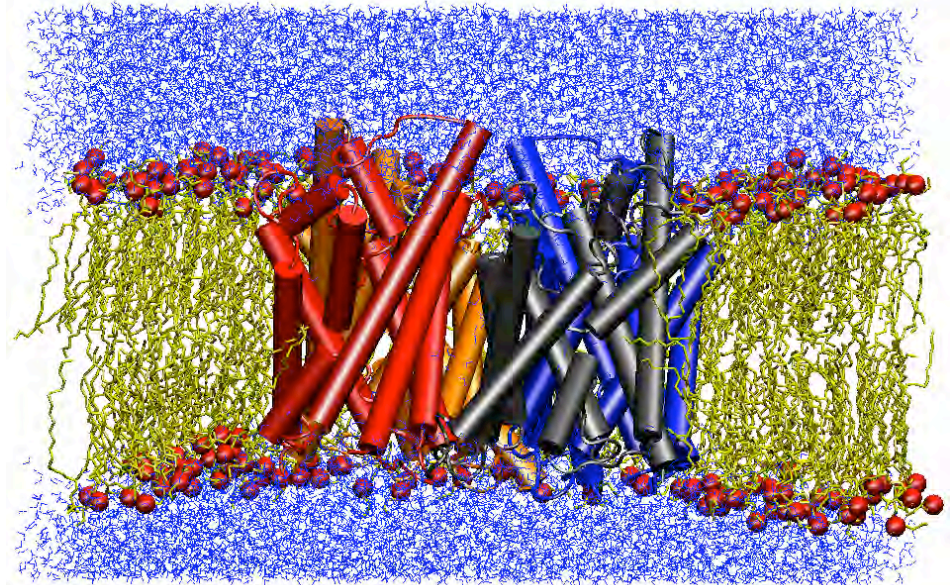
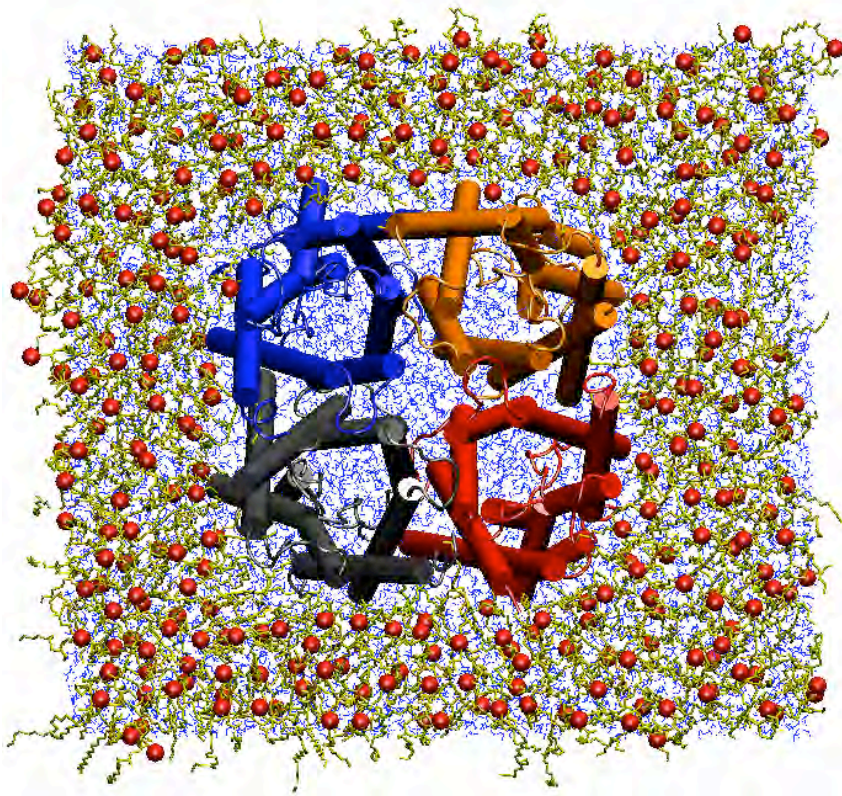
**AQP1** - Mammalian aquaporin-1

AqpZ and AQP0 (2004, 2005), AqpM (2005), soPIP2 (2006)



# Molecular Dynamics Simulations

Protein: ~ 15,000 atoms  
Lipids (POPE): ~ 40,000 atoms  
Water: ~ 51,000 atoms  
Total: ~ 106,000 atoms



NAMD, CHARMM27, PME

NpT ensemble at 310 K

1ns equilibration, 4ns production

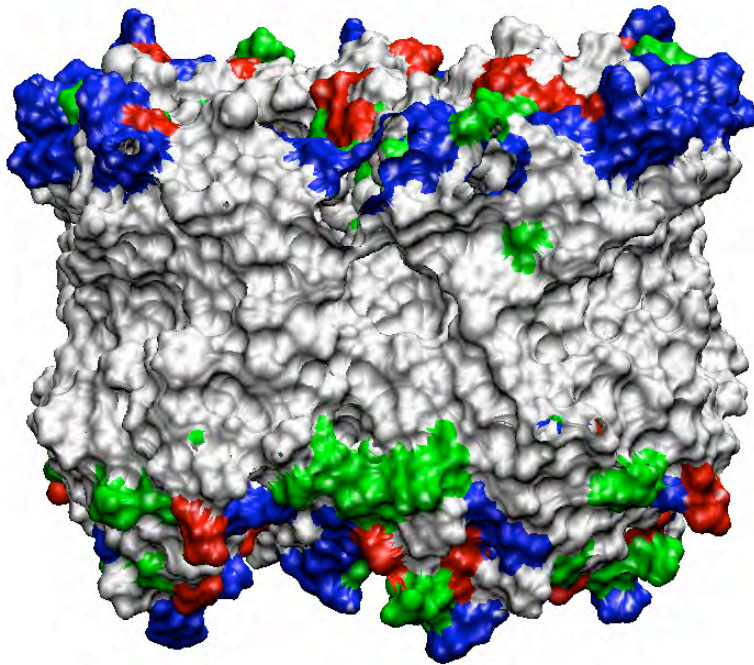
10 days /ns - 32-proc Linux cluster

3.5 days/ns - 128 O2000 CPUs

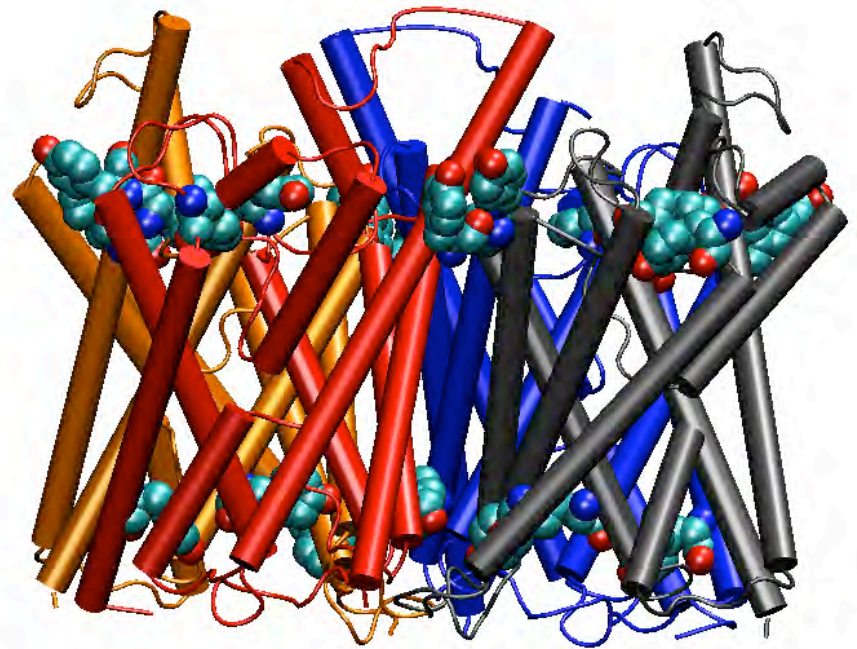
**0.35 days/ns - 512 LeMieux CPUs**



# Protein Embedding in Membrane

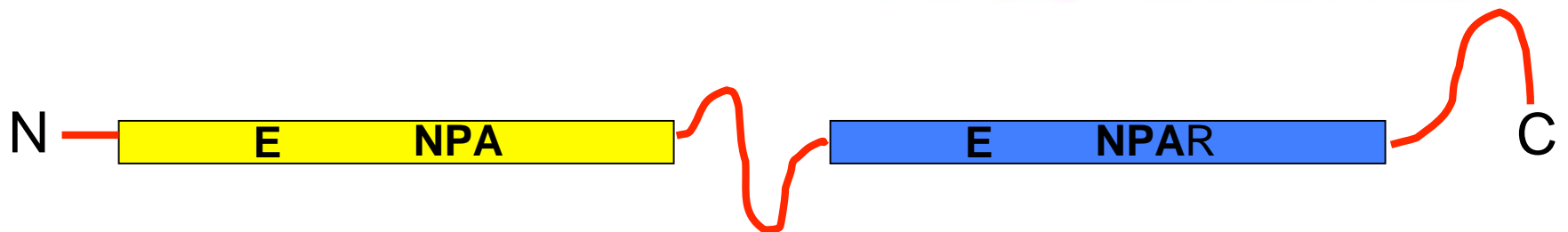
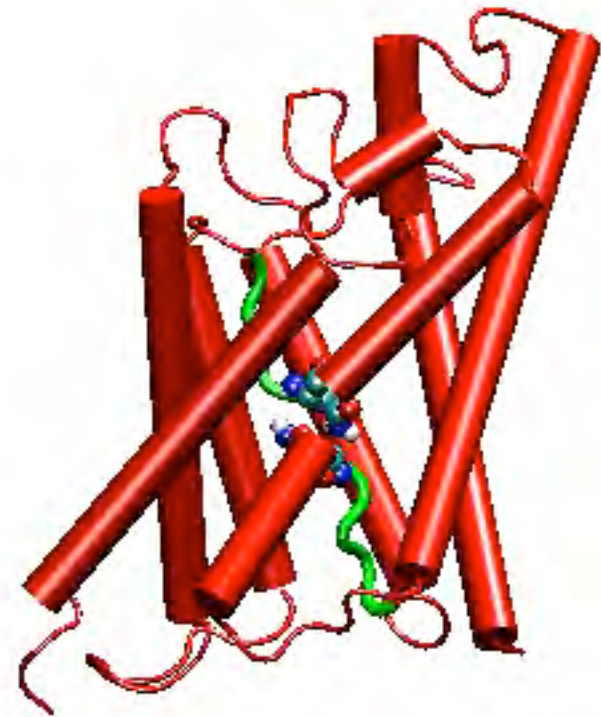
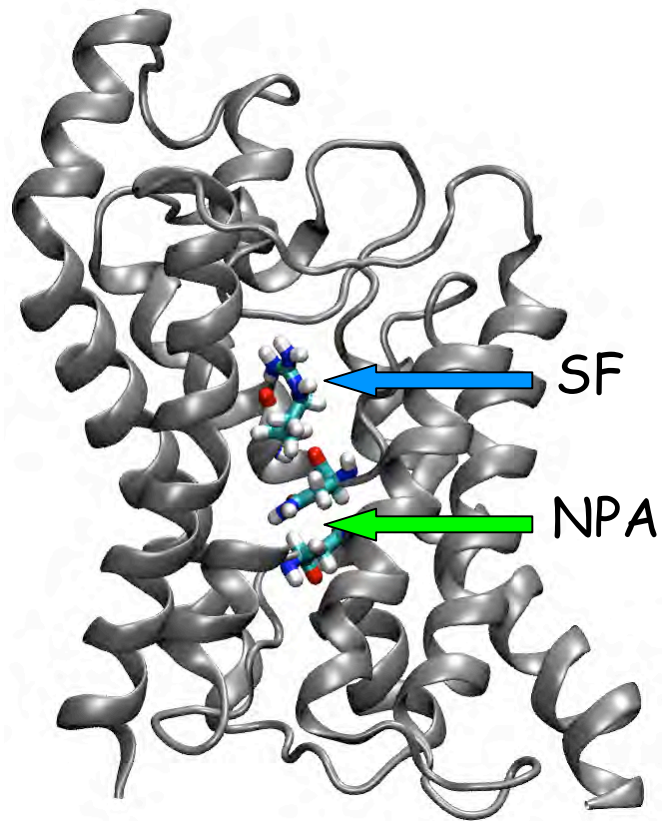


Hydrophobic surface  
of the protein

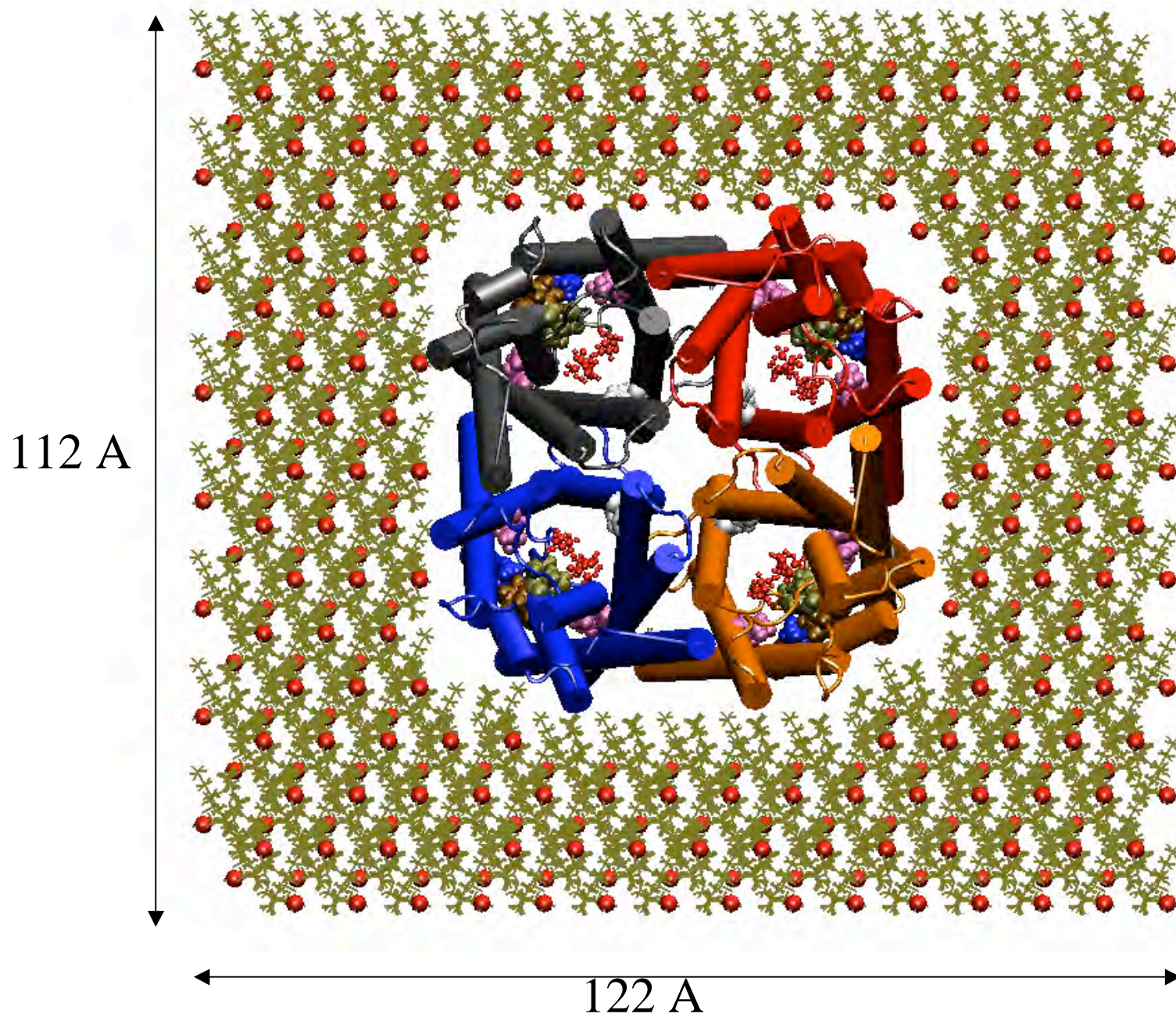


Ring of  
Tyr and Trp

# Structurally Conserved Features





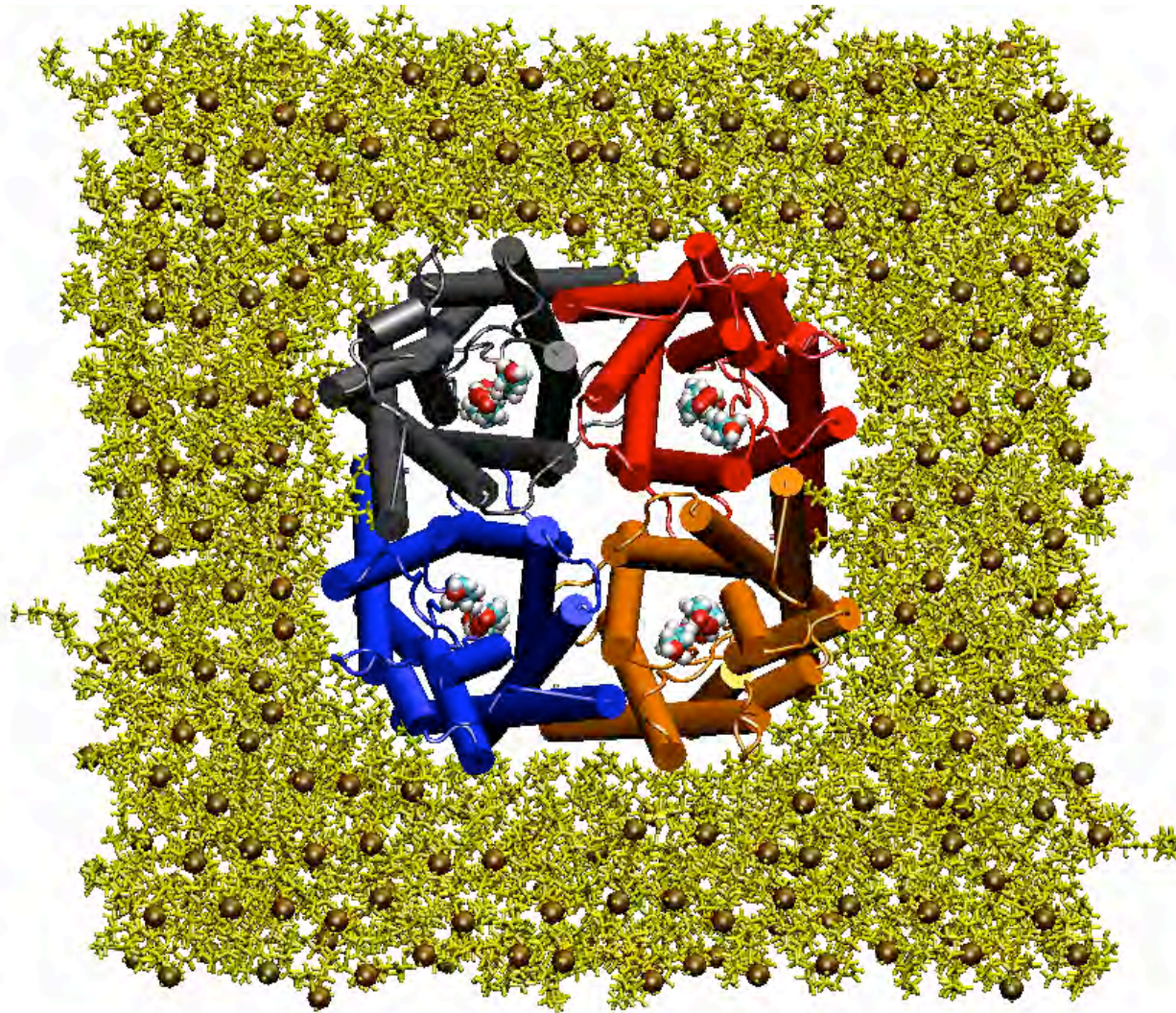


# A Recipe for Membrane Protein Simulations

- Insert your protein into a hydrated lipid bilayer.
- Fix the protein; minimize the rest and run a short "constant-pressure" MD to bring lipids closer to the protein and fill the gap between the protein and lipids.
- Watch water molecules; if necessary apply constraints to prevent them from penetrating into the open gaps between lipids and the protein.
- Monitor the volume of your simulation box until it is almost constant. Do not run the system for too long during this phase.
- Now release the protein, minimize the whole system, and start an NpT simulation of the whole system.
- If desired, you may switch to an NVT simulation, when the system reaches a stable volume.

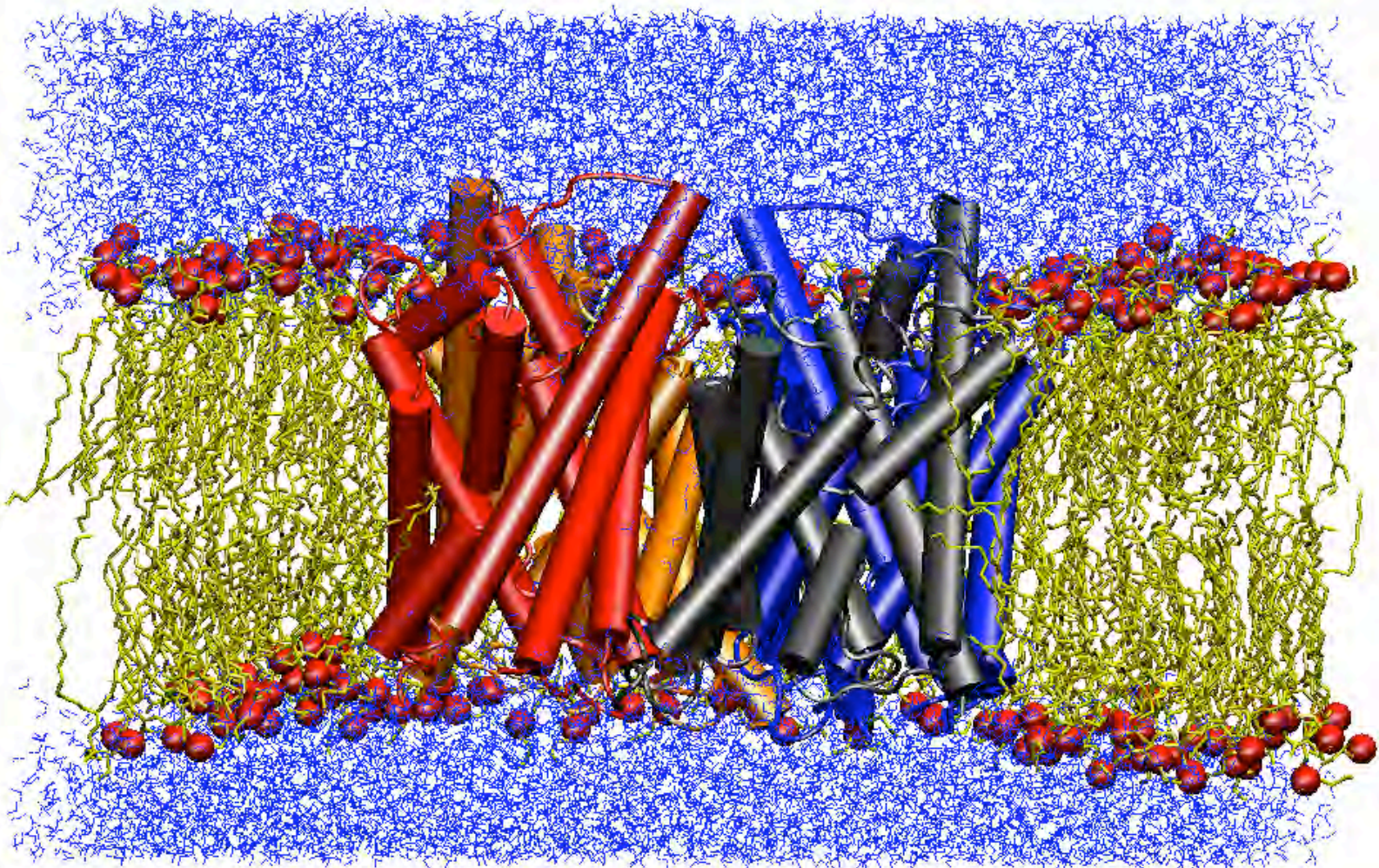


# Lipid-Protein Packing During the Initial NpT Simulation





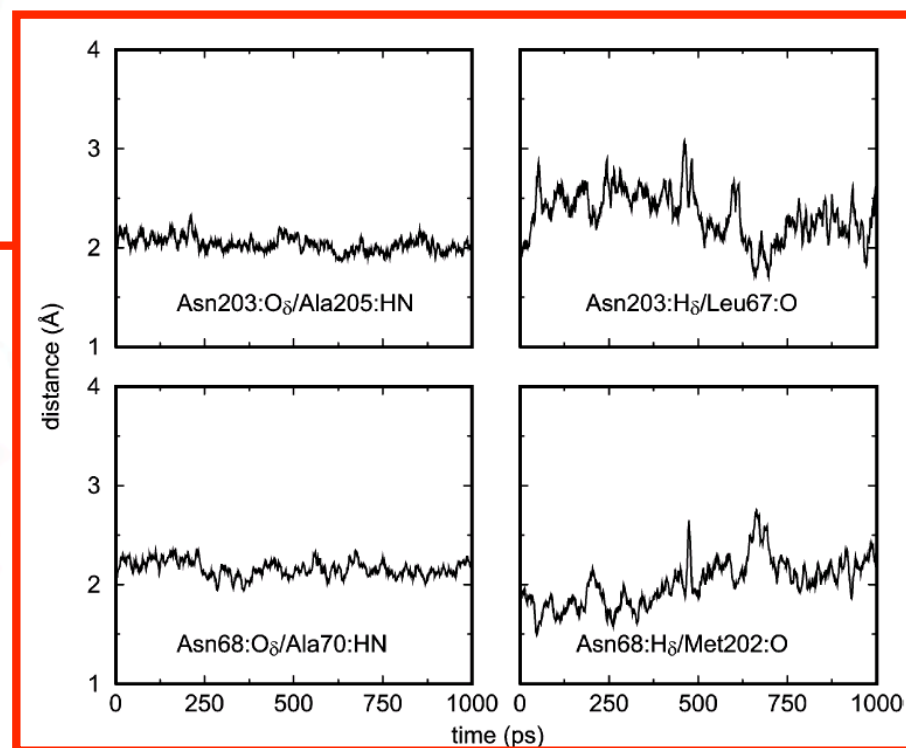
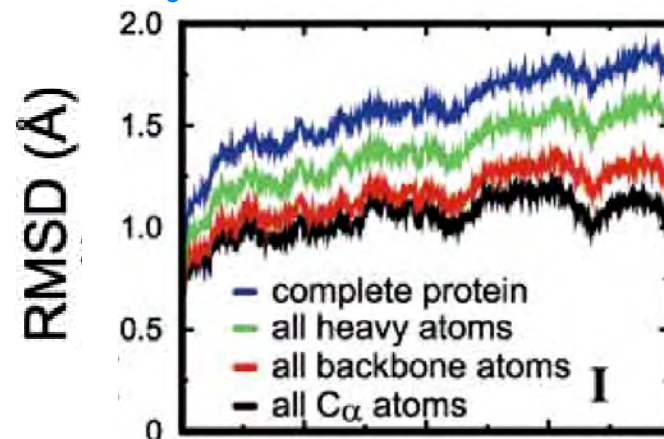
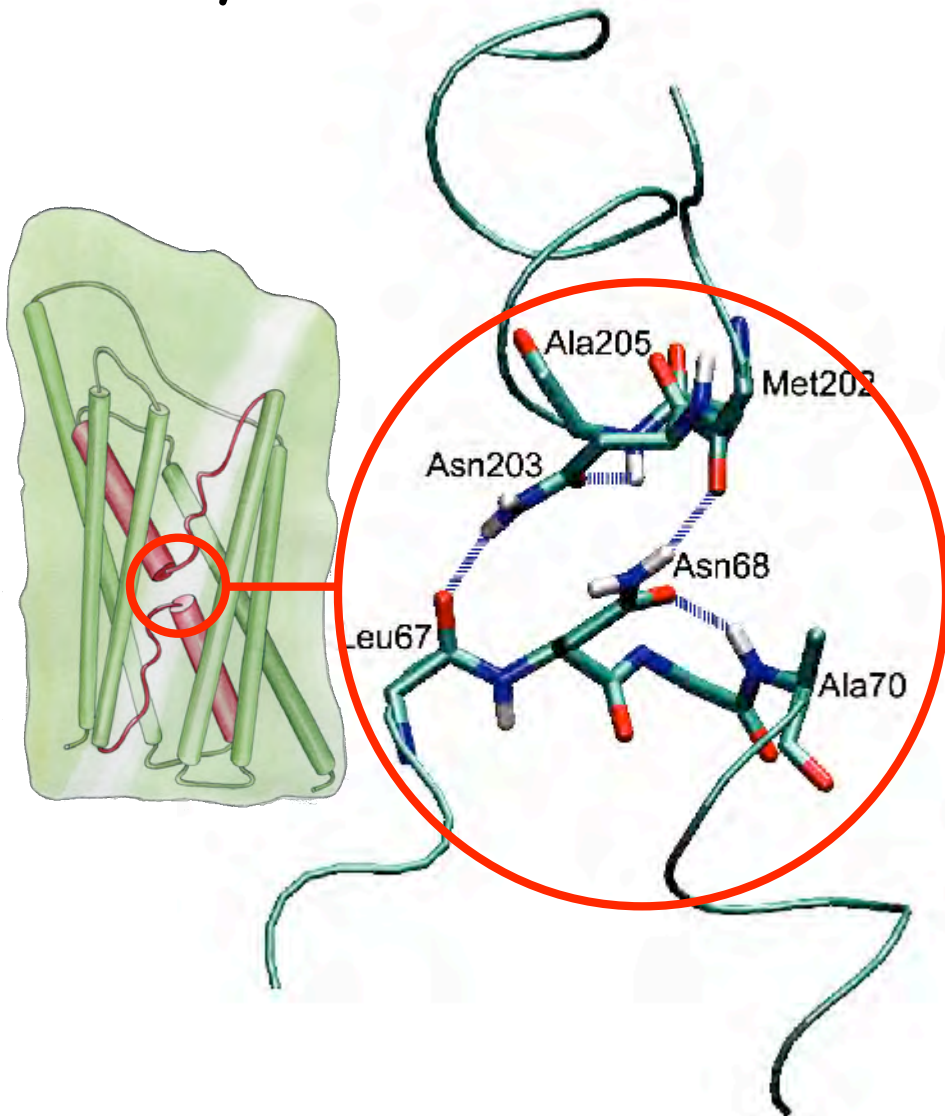
# Adjustment of Membrane Thickness to the Protein Hydrophobic Surface



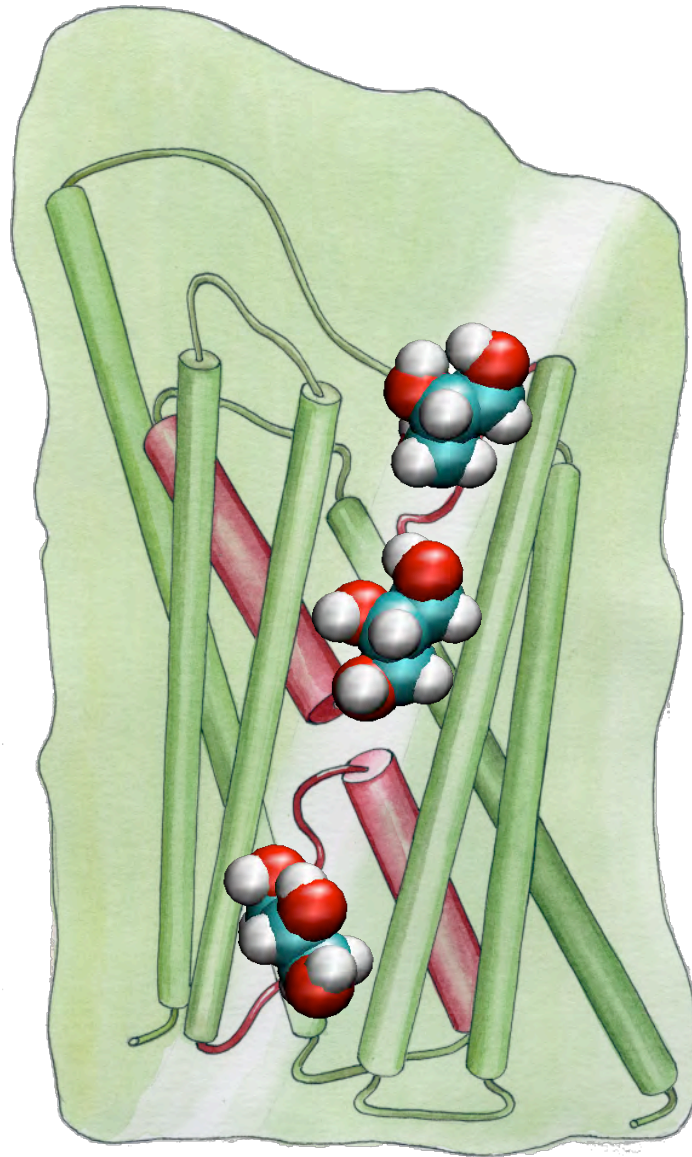


# An extremely stable protein

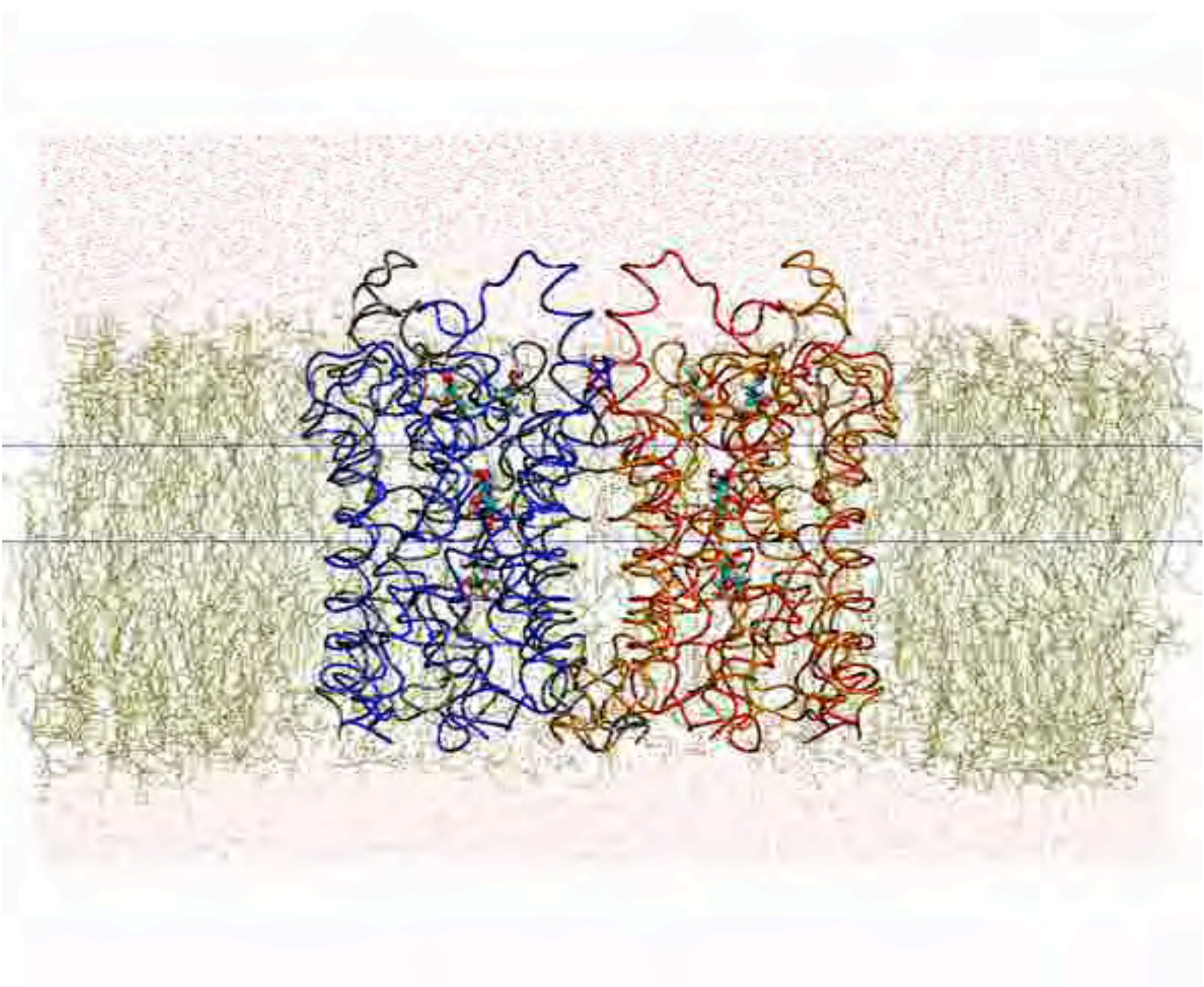
## Stability of NPA - NPA Interaction



# Glycerol-Saturated GlpF







# Complete description of the conduction pathway

Constriction region



} Selectivity filter



# Details of Protein-Substrate Interaction Are Always Important

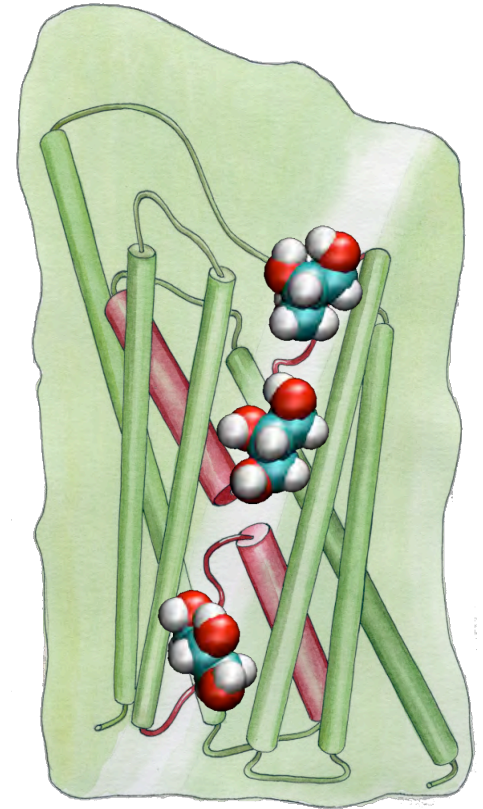
- Identify those groups of the protein that are directly involved in the main function of the protein.
- Look at the interaction of these primary residues with other groups in the protein.
- Look at buried charged residues inside the protein; they must have an important role.
- Backbone hydrogen bonds are mainly responsible for stabilization of secondary structure elements in the protein; side chain hydrogen bonds could be functionally important.

# Channel Hydrogen Bonding Sites

...

```
{set frame 0}{frame < 100}{incr frame}{  
  animate goto $frame  
  set donor [atomselect top  
    "name O N and within 2 of  
    (resname GCL and name HO)"]  
  lappend [$donor get index] list1  
  set acceptor [atomselect top  
    "resname GCL and name O and  
    within 2 of (protein and name HN HO)"]  
  lappend [$acceptor get index] list2  
}
```

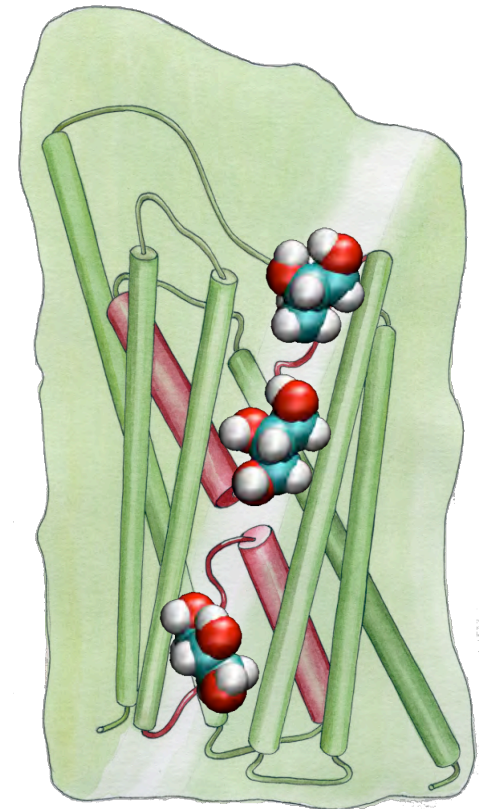
...





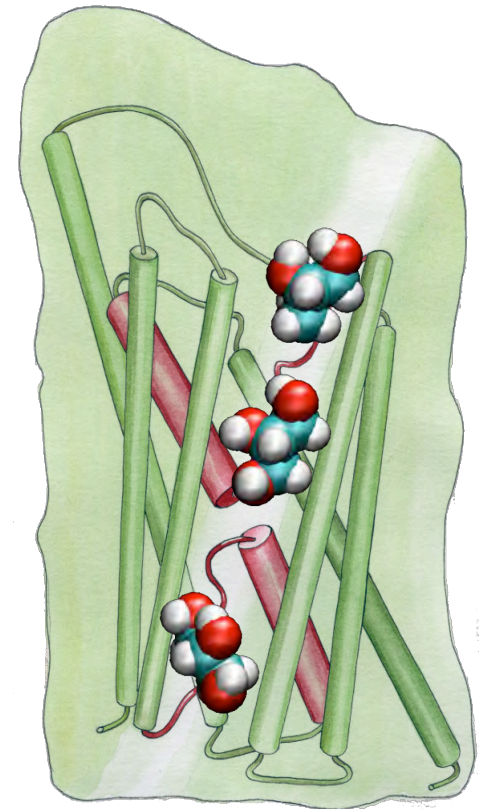
# Channel Hydrogen Bonding Sites

GLN	41	OE1 NE2	LEU	197	O
TRP	48	O NE1	THR	198	O
GLY	64	O	GLY	199	O
ALA	65	O	PHE	200	O
HIS	66	O ND1	ALA	201	O
LEU	67	O	ASN	203	ND2
ASN	68	ND2			
ASP	130	OD1	LYS	33	HZ1 HZ3
GLY	133	O	GLN	41	HE21
SER	136	O	TRP	48	HE1
TYR	138	O	HIS	66	HD1
PRO	139	O N	<u>ASN</u>	68	HD22
ASN	140	OD1 ND2	<u>TYR</u>	138	HN
HIS	142	ND1	ASN	140	HN HD21 HD22
THR	167	OG1	HIS	142	HD1
GLY	195	O	GLY	199	HN
PRO	196	O	<u>ASN</u>	203	HN HD21HD22
			<u>ARG</u>	206	HE HH21HH22



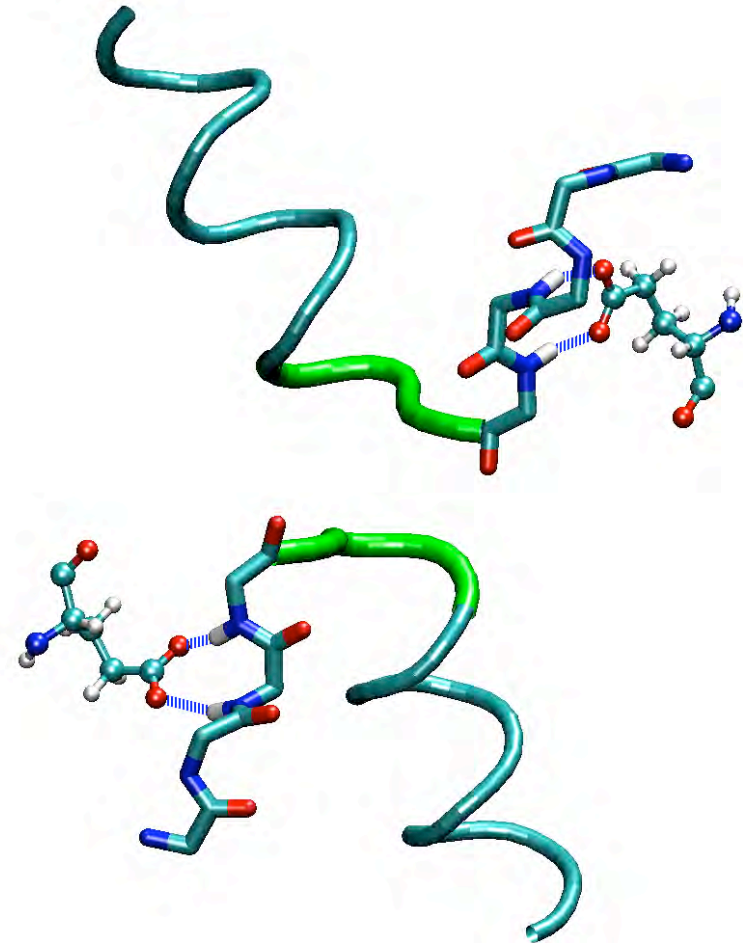
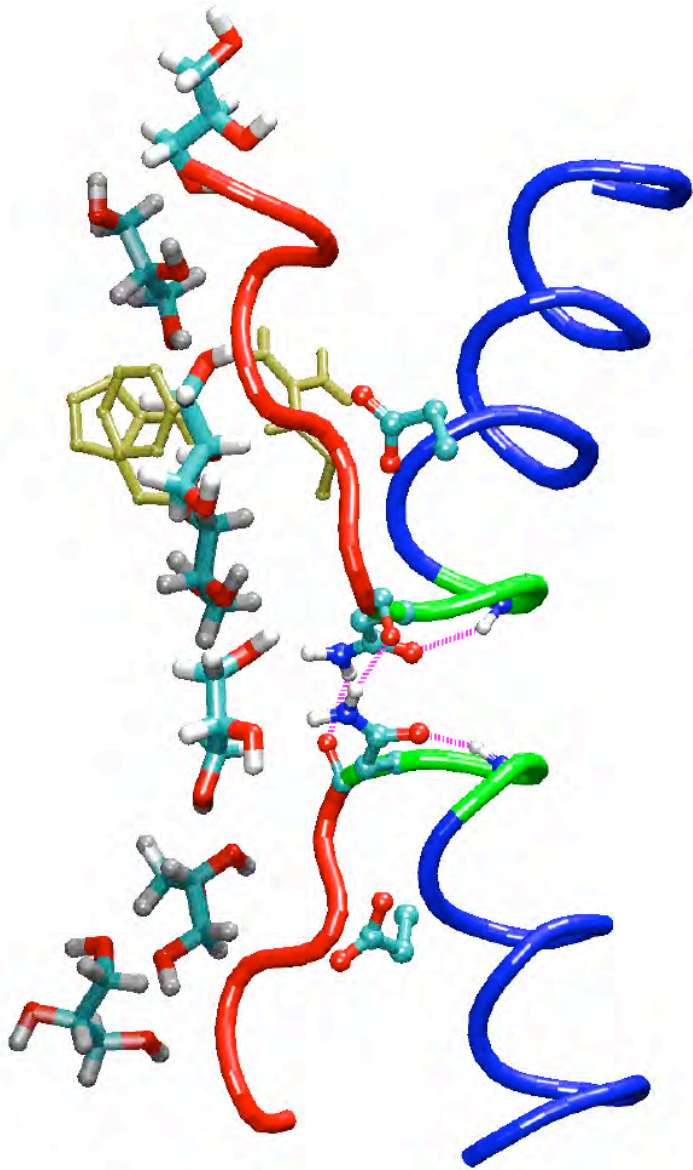
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GLN	41	OE1 NE2	LEU	197	O
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ALA	65	O	PHE	200	O
HIS	66	O ND1	ALA	201	O
LEU	67	O	ASN	203	ND2
ASN	68	ND2			
ASP	130	OD1	LYS	33	HZ1 HZ3
GLY	133	O	GLN	41	HE21
SER	136	O	TRP	48	HE1
TYR	138	O	HIS	66	HD1
PRO	139	O N	<u>ASN</u>	68	HD22
ASN	140	OD1 ND2	TYR	138	HN
HIS	142	ND1	ASN	140	HN HD21 HD22
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			<u>ARG</u>	206	HE HH21HH22



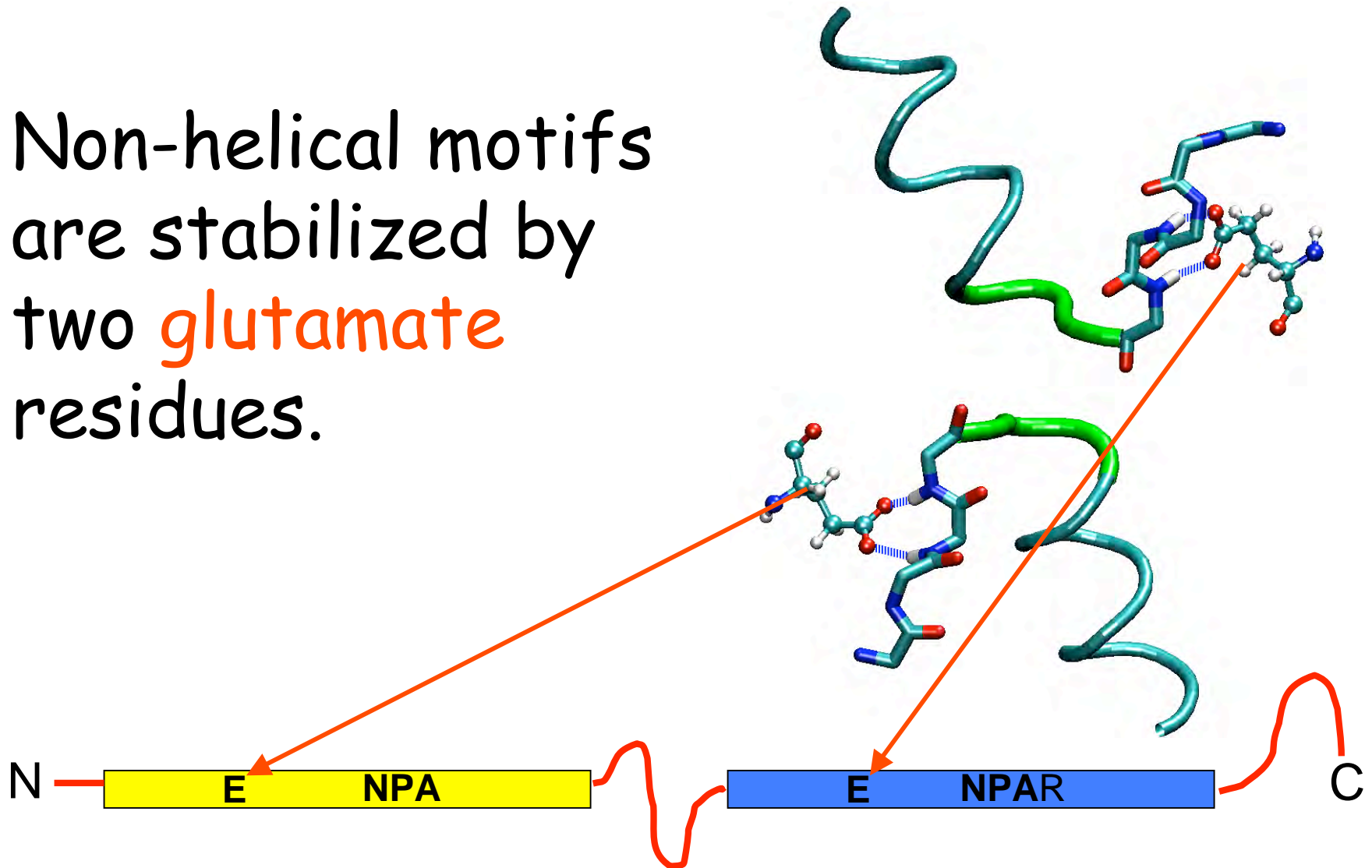


# The Substrate Pathway is formed by $C=O$ groups



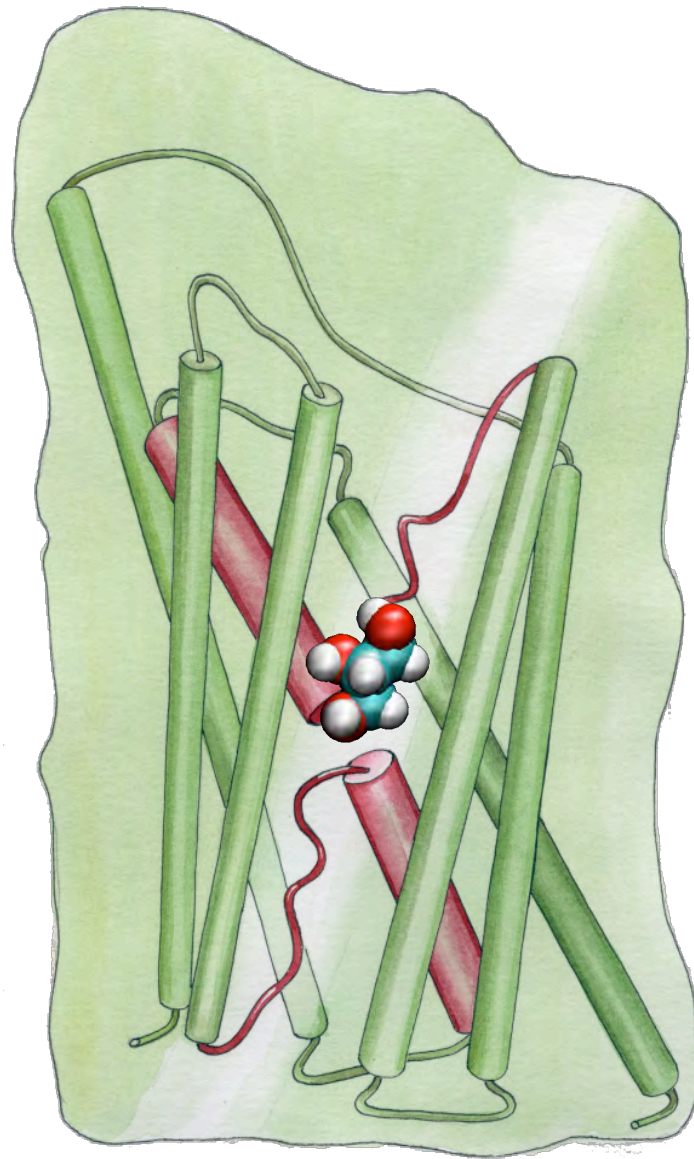
# The Substrate Pathway is formed by $C=O$ groups

Non-helical motifs  
are stabilized by  
two **glutamate**  
residues.



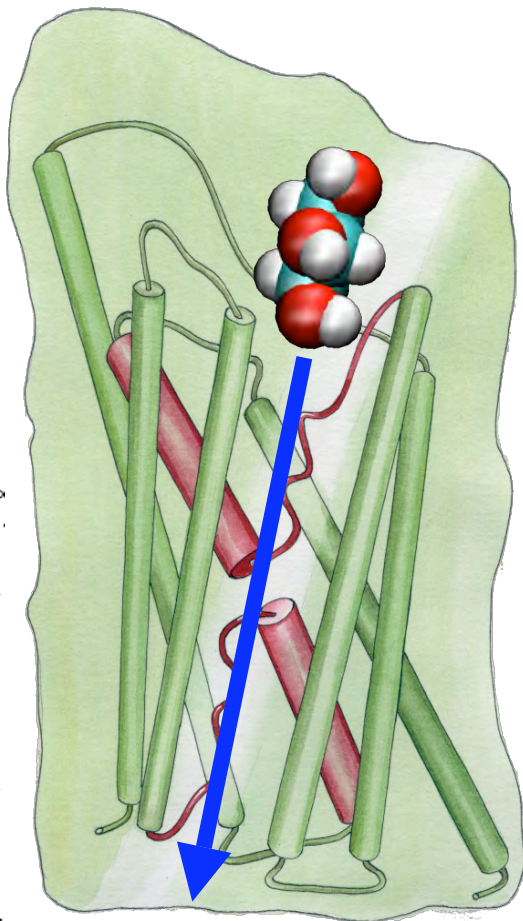
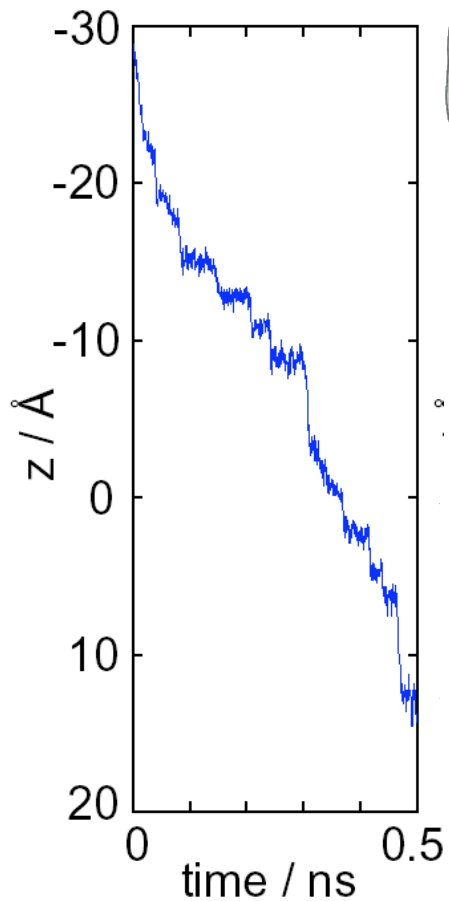


# Single Glycerol per channel

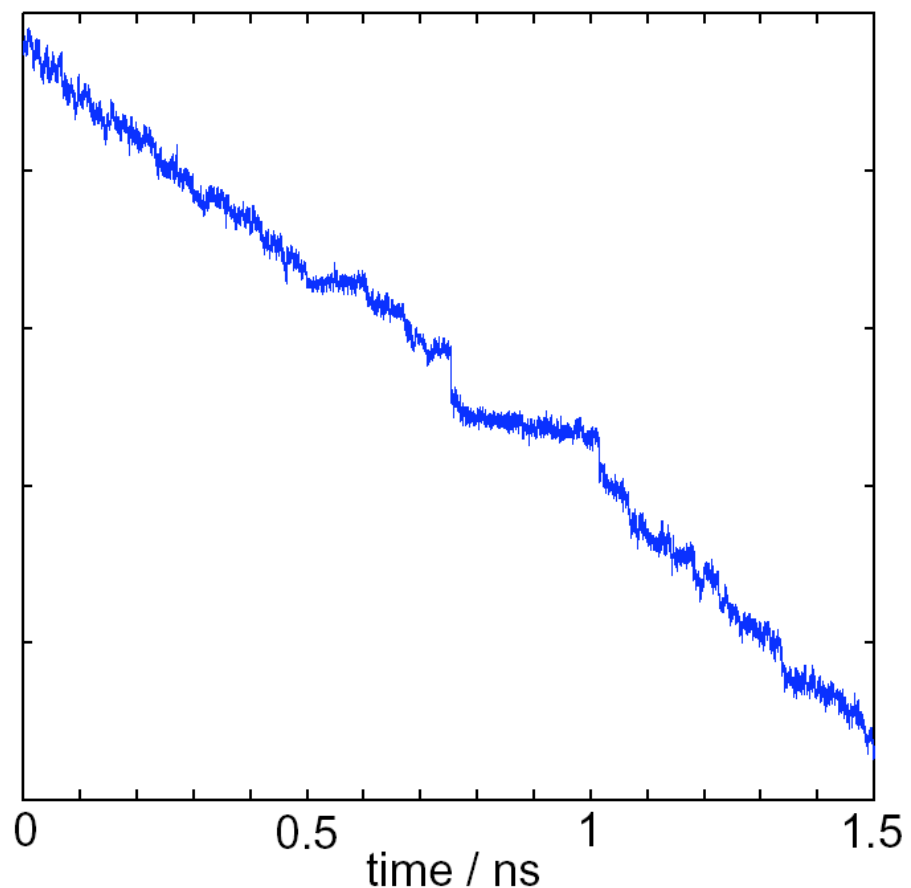


# Steered Molecular Dynamics

constant force  
(250 pN)

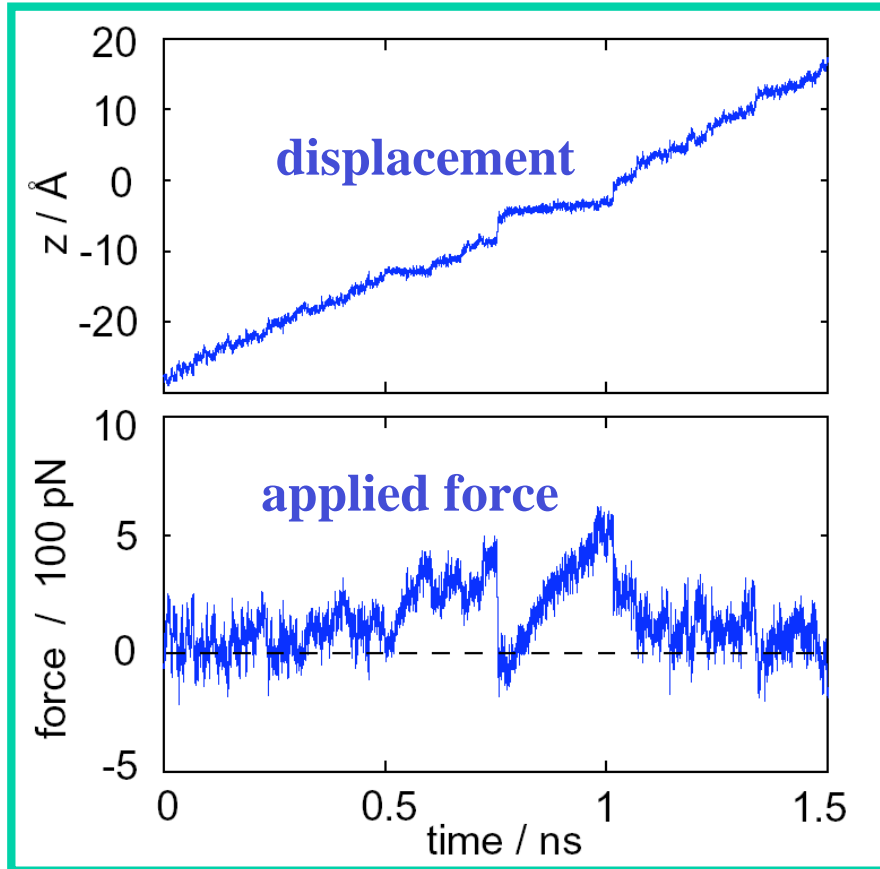


constant velocity  
(30 Å/ns)





# Free Energy Calculation in SMD



Free energy

SMD simulation  
a **non-equilibrium** process

$$\Delta G \leq \langle W \rangle$$

One needs to discount  
irreversible work

$$e^{-\Delta G / k_B T} = \left\langle e^{-W / k_B T} \right\rangle$$

Jarzynski, *PRL* 1997

Hummer, *PNAS*, *JCP* 2001

Liphardt, et al., *Science* 2002

# Constructing the Potential of Mean Force

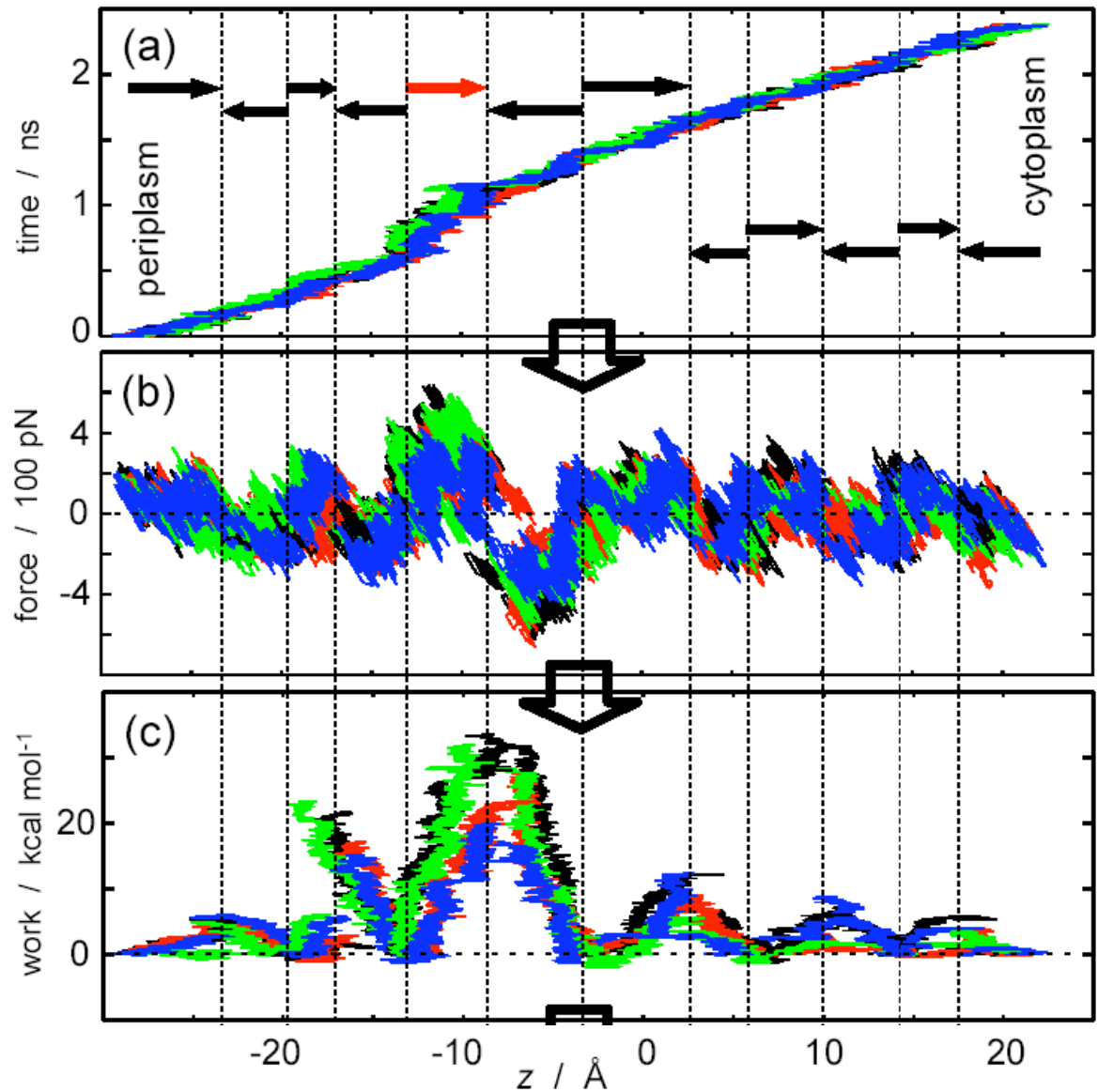
4 trajectories

$v = 0.03, 0.015 \text{ \AA/ps}$

$k = 150 \text{ pN/\AA}$

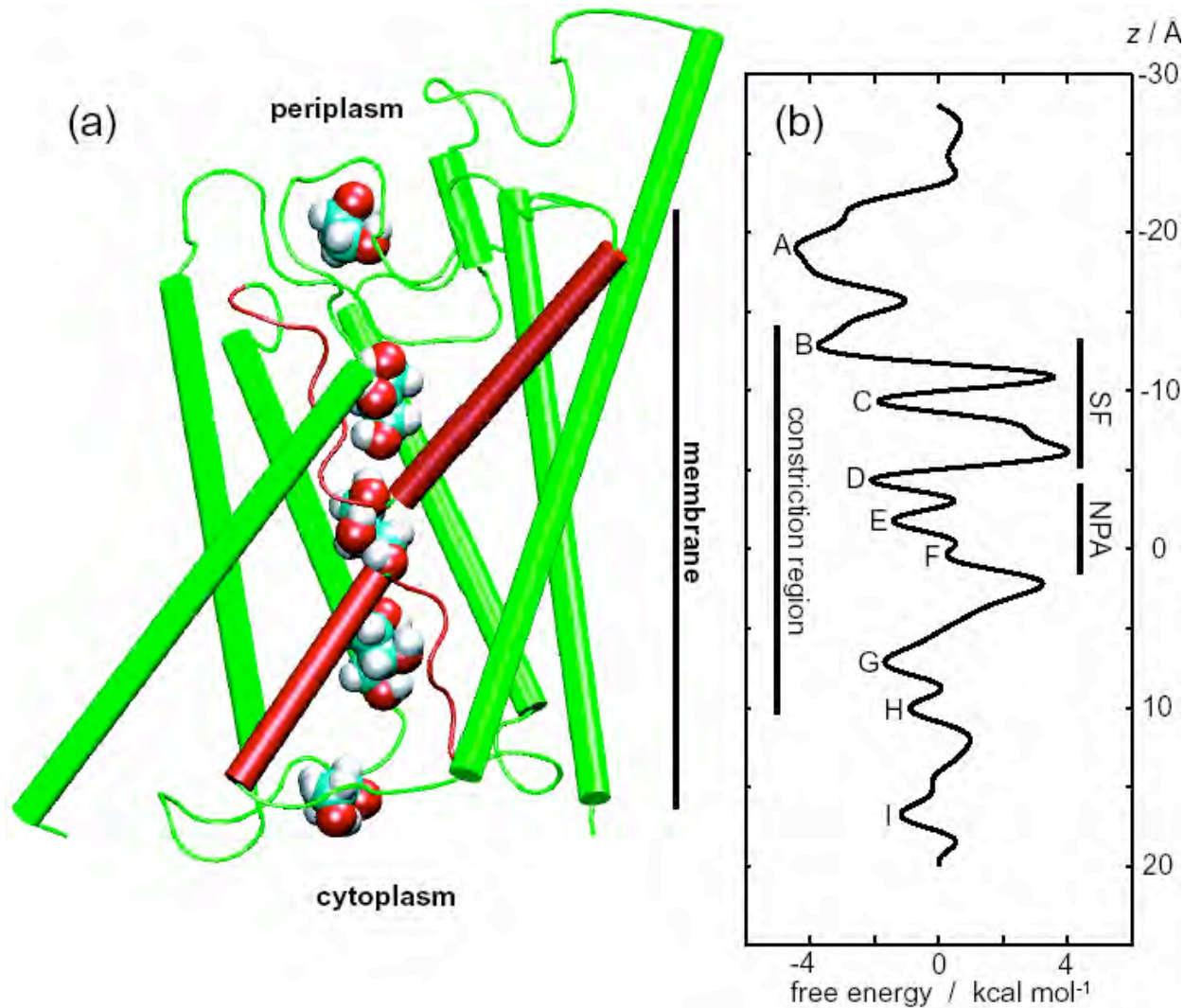
$$f(t) = -k[z(t) - z_0 - vt]$$

$$W(t) = \int_0^t dt' v f(t')$$



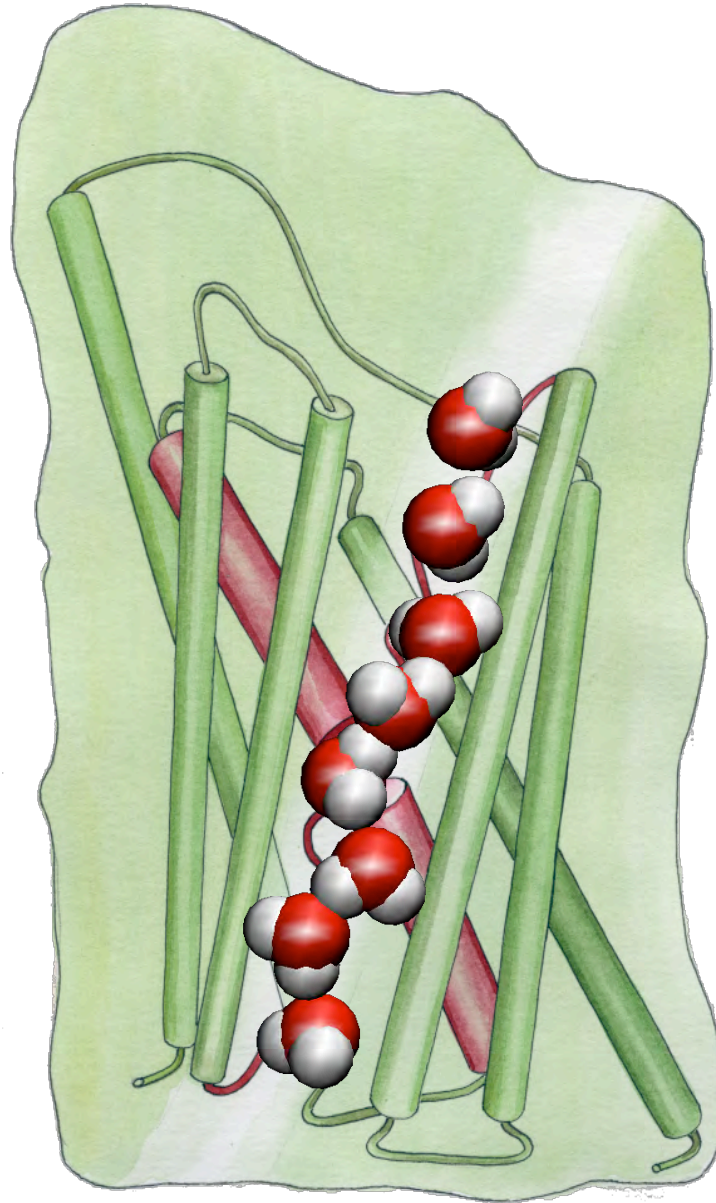


# Features of the Potential of Mean Force



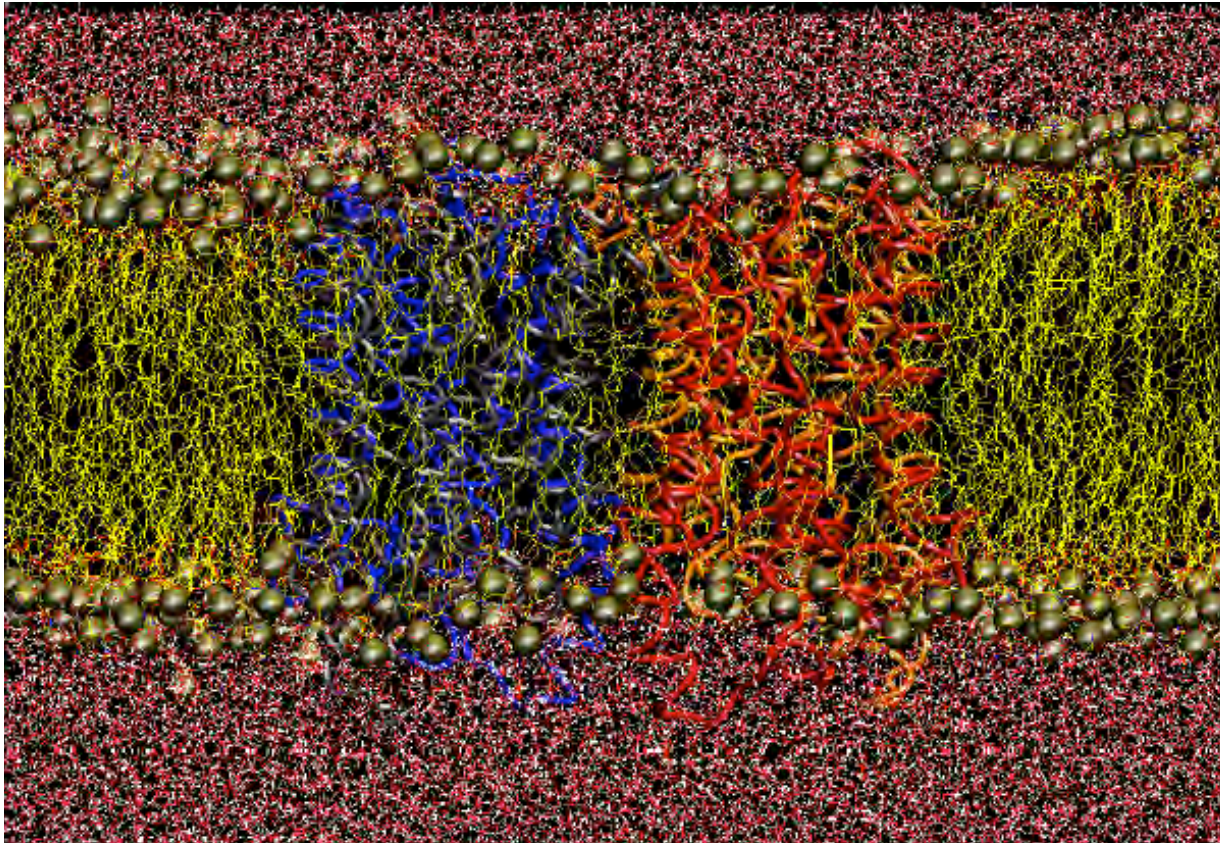
- Captures major features of the channel
- The largest barrier  $\approx$  **7.3 kcal/mol; exp.:  $9.6 \pm 1.5$  kcal/mol**

# Glycerol-Free GlpF



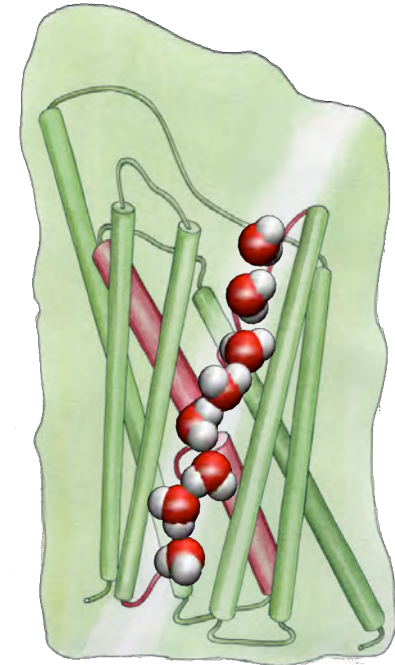


# Water permeation



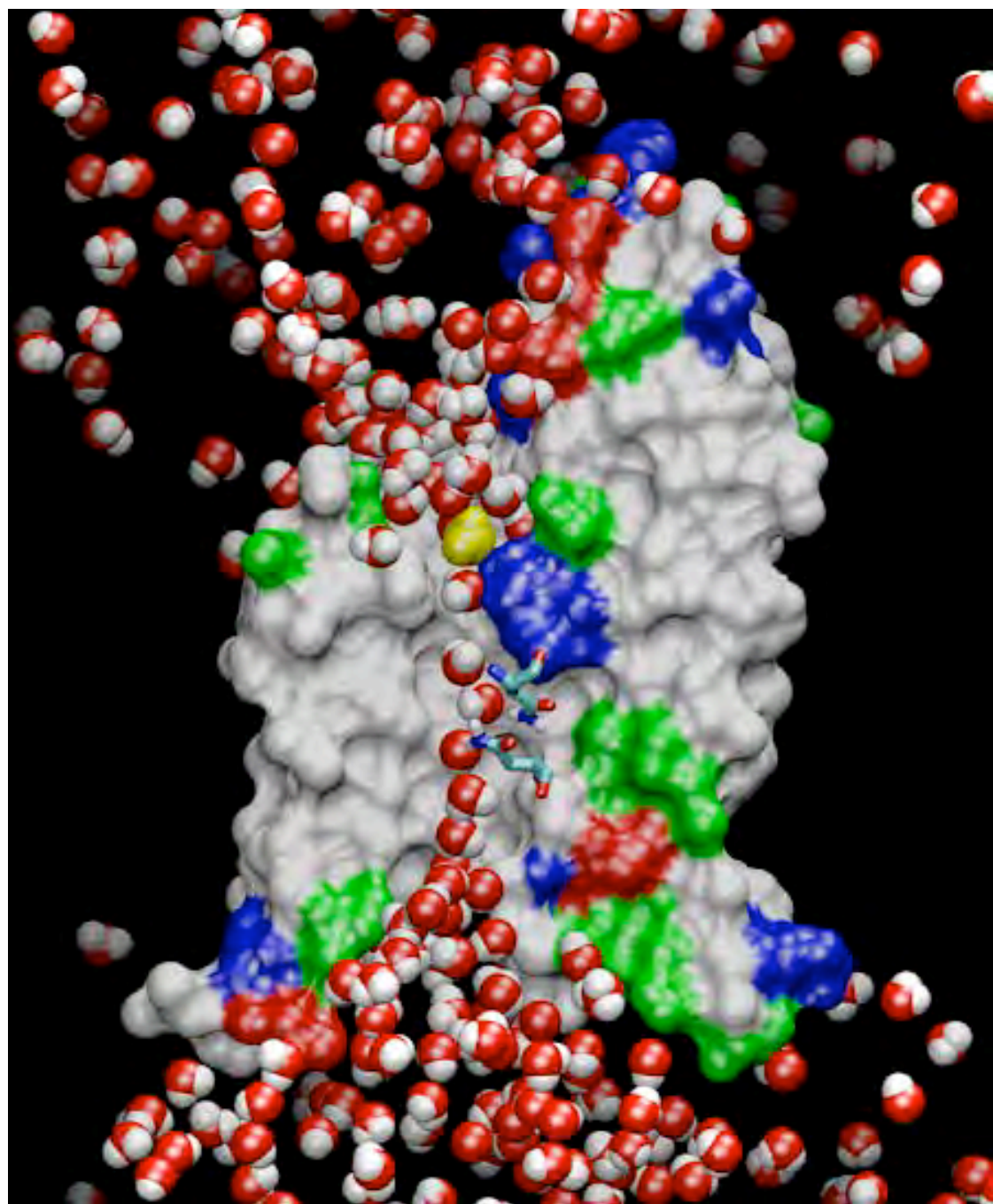
18 water conducted  
In 4 monomers in 4 ns  
1.125 water/monomer/ns  
Exp. =  $\sim 1-2$  /ns

5 nanosecond  
Simulation

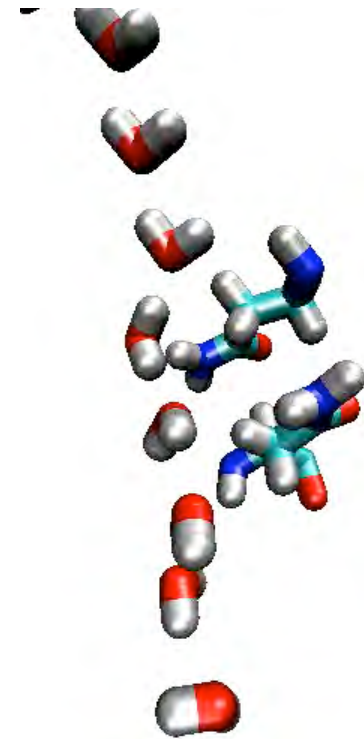
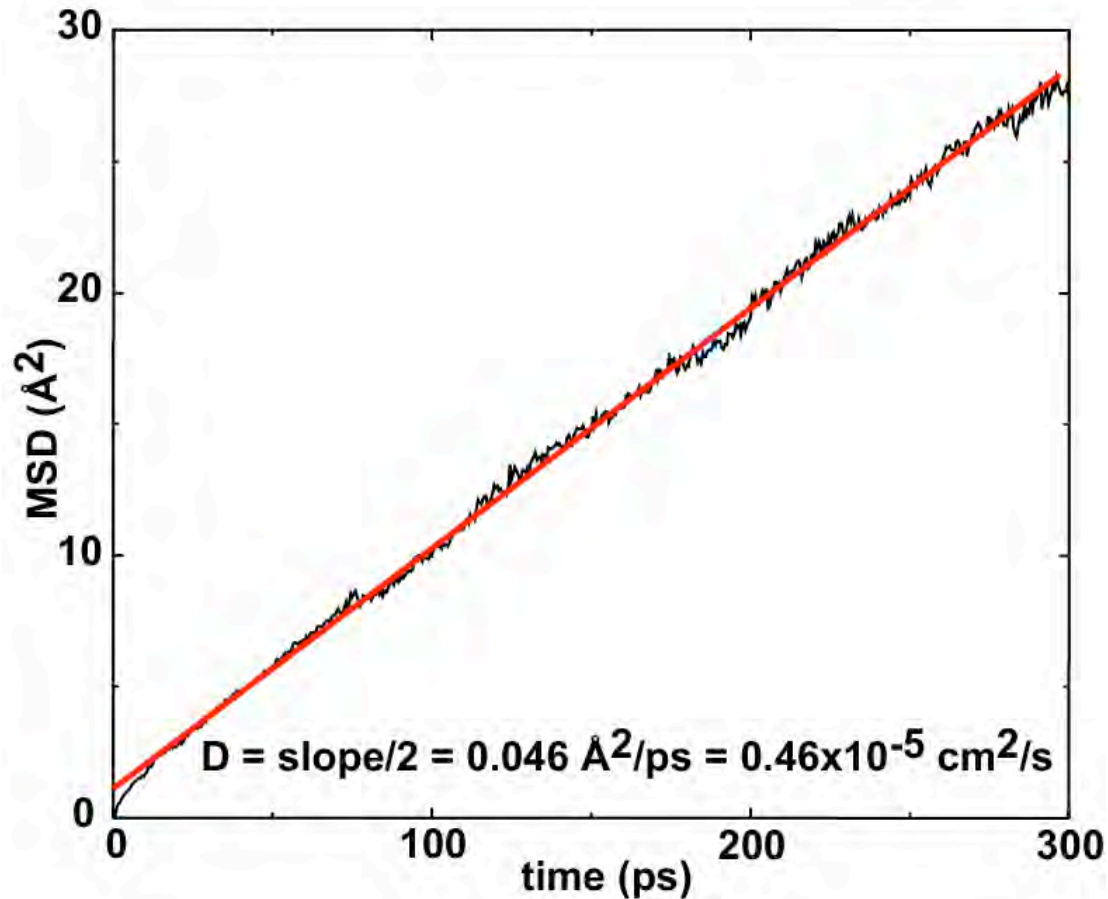


7-8 water  
molecules in each  
channel





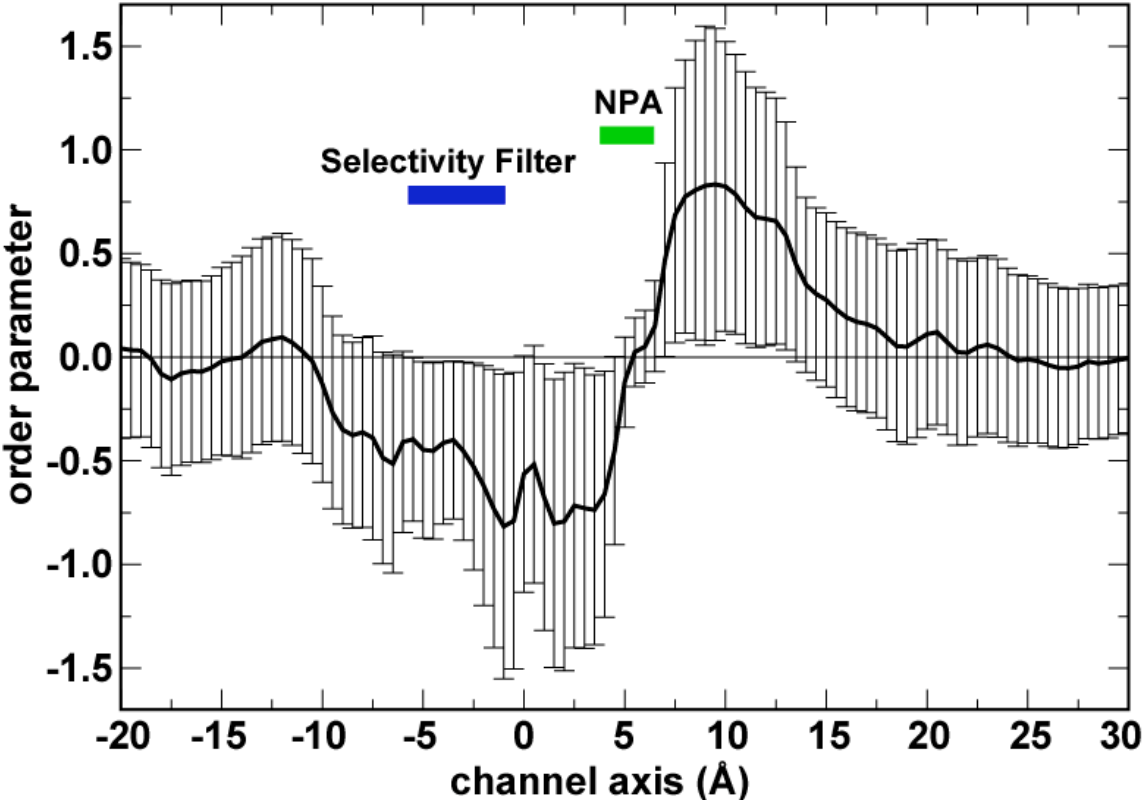
# Diffusion of Water in the channel



One dimensional diffusion:  $2Dt = \langle (z_t - z_0)^2 \rangle$

Experimental value for AQP1:  $0.4-0.8 \text{ e-}5$

**channel region (20 Å)**



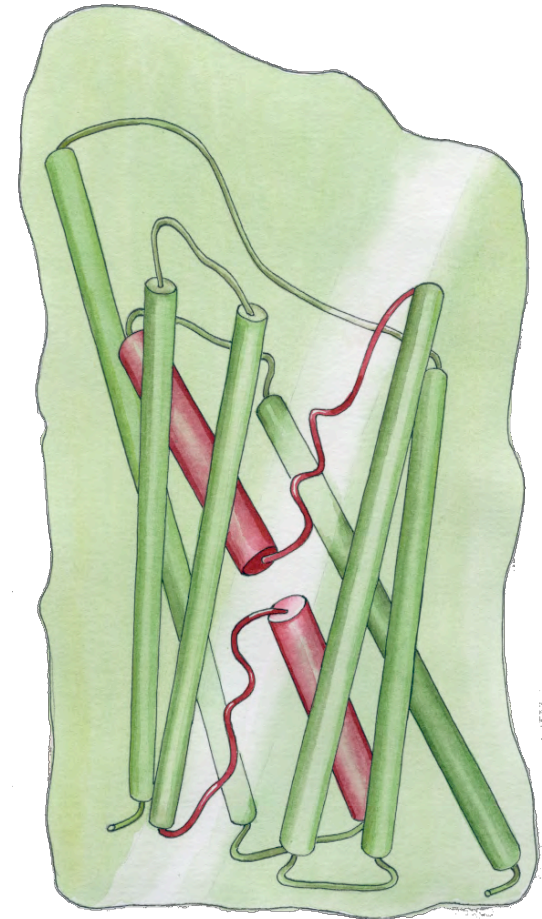
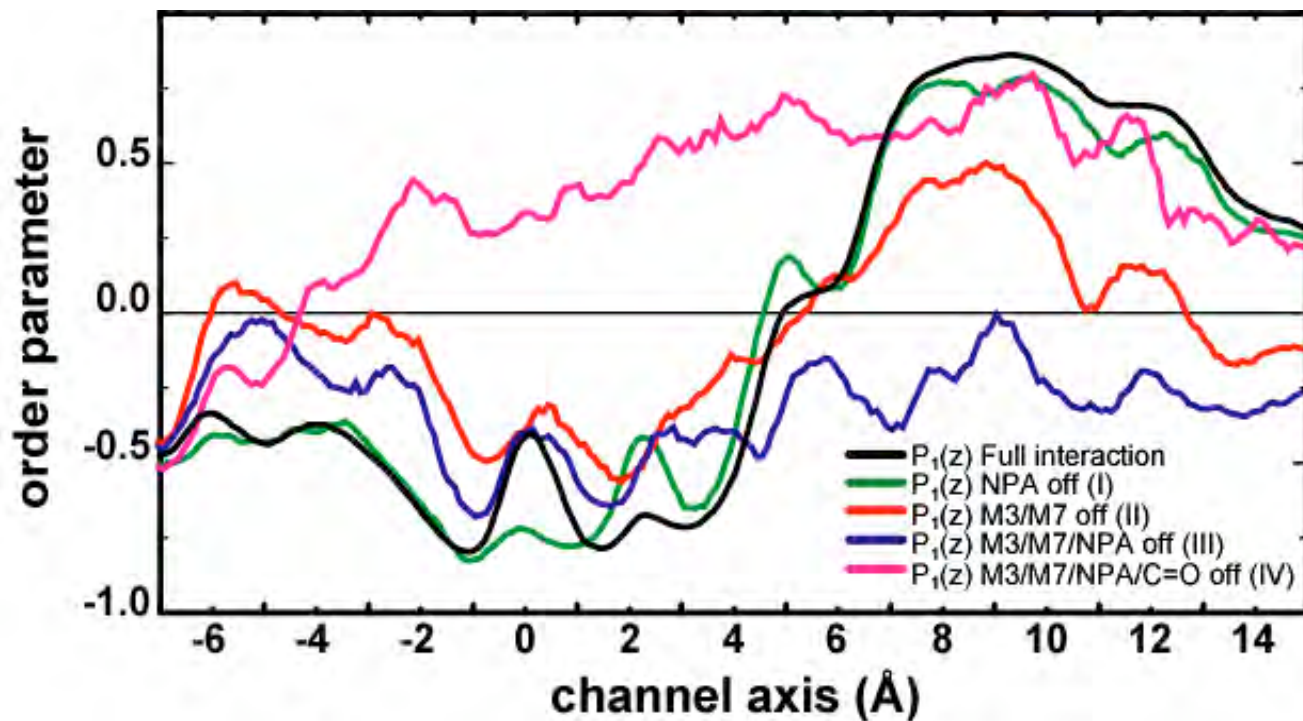


## R E M E M B E R:

One of the most useful advantages of simulations over experiments is that you can modify the system as you wish: You can do modifications that are not even possible at all in reality!

This is a powerful technique to test hypotheses developed during your simulations. **Use it!**

# Electrostatic Stabilization of Water Bipolar Arrangement



# Proton transfer through water

