

# MOLECULAR DYNAMICS POLYMER NANO-COMPOSITES

BEATRIZ A. PAZMIÑO<sup>1</sup>, FRANCIS W. STARR<sup>1</sup>, JACK F. DOUGLAS<sup>2</sup>

<sup>1</sup>Department of Physics, Wesleyan University, Middletown, CT

<sup>2</sup>Polymer Division, NIST, Gaithersburg, MD

Workshop on GPU Programming for Molecular Modeling 2013

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ESPE  
B.S.  
Electronic Engineering

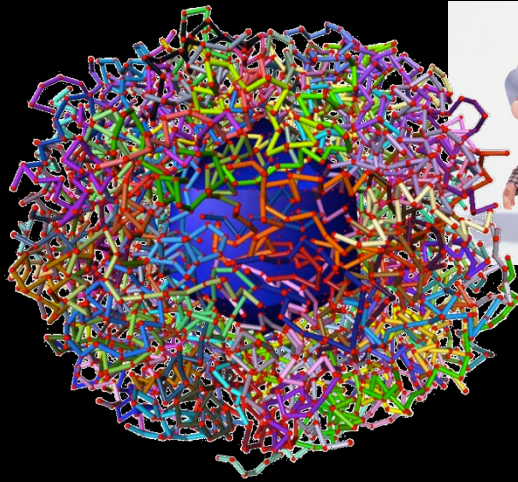
PhD. Candidate  
Wesleyan University



Prof. Francis Starr  
Wesleyan University

# GPU Projects:

- MD program



Motivation

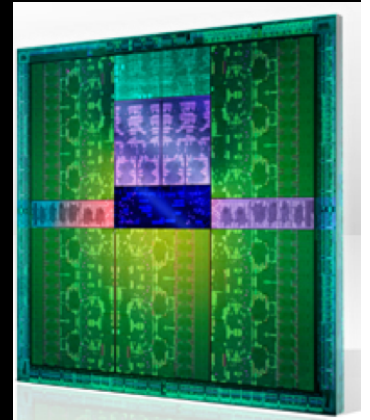
*Computational Model*  
*Key Algorithms*  
*GPU Challenges*

- STRINGS program



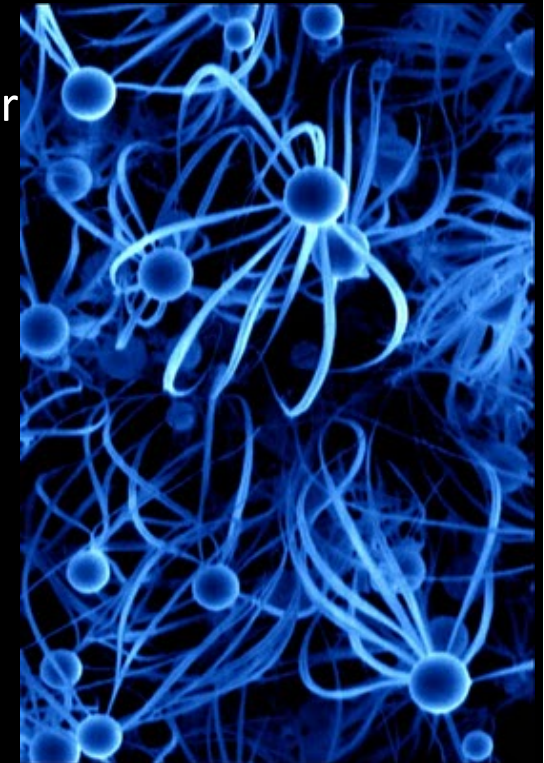
Motivation

Computational Model  
Key Algorithms  
GPU Challenges

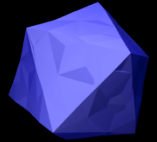


# Polymer Nano-composites

- ✓ Polymer-Nanocomposite = Polymer + Nanoparticles
- ✓ Additives to polymer common to change properties or cost
- ✓ Only small concentration of NP needed (<15%)
- ✓ Substantial improvements possible for:
  - Tensile strength
  - Thermal stability
  - Heat distortion temperature
  - Chemical resistance
  - Electrical conductivity
  - Optical clarity
- ✓ Polymer nanocomposites are typically glasses



<http://www.zeitnews.org/node/1163>



## What is the problem?

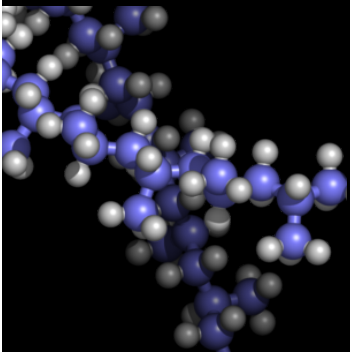
- ✓ How can we understand and manipulate the dynamics and glass transition of polymers by adding nanoparticles (NP)?

## Why do we care?

- ✓ Polymers are a \$2.4 trillion industry
- ✓ Fundamental insight into the origin of the glass transition

“The deepest and most interesting unsolved problem in solid state theory is probably the theory of the nature of glass and the glass transition.”

Philip W. Anderson (1995)  
(Nobel Laureate 1977)



# COOPERATIVE MOTION IN POLYMER NANO-COMPOSITES

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# COOPERATIVE MOTION IN POLYMER NANOCOMPOSITES

What is the specific relationship with  
their dynamical properties?

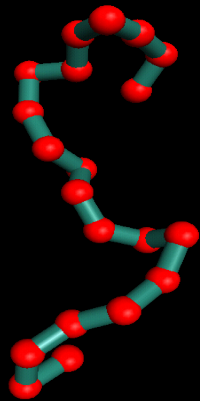


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## Tool

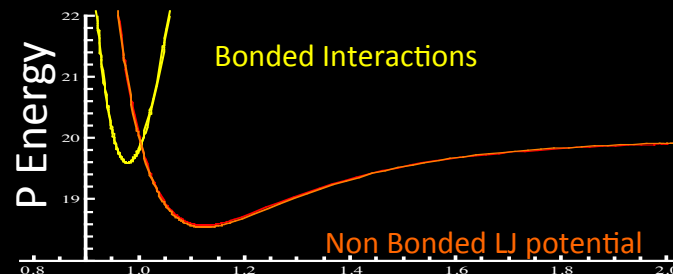
### -Polymer Model



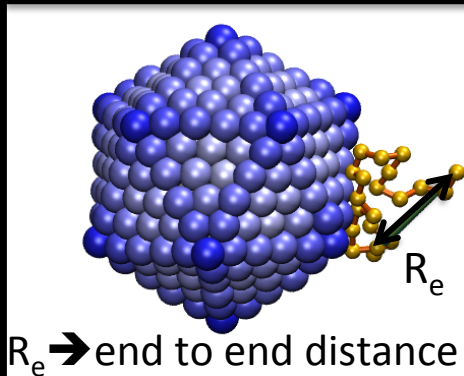
## Molecular Dynamics Simulation

Chain of (LJ) monomers

Inhibit crystallization Phys. Rev. A 33, 3628 (1986)

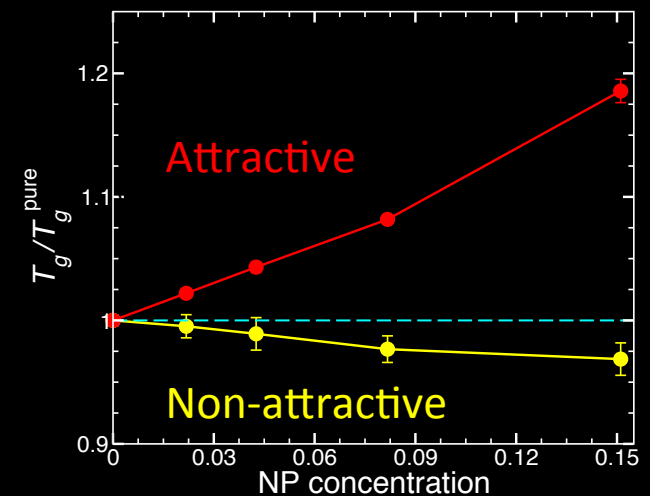


### -Nano-particle Model Icosahedral Macromolecules 35, 4481 (2002)



Surface Interactions:

- Attractive
- Non-attractive



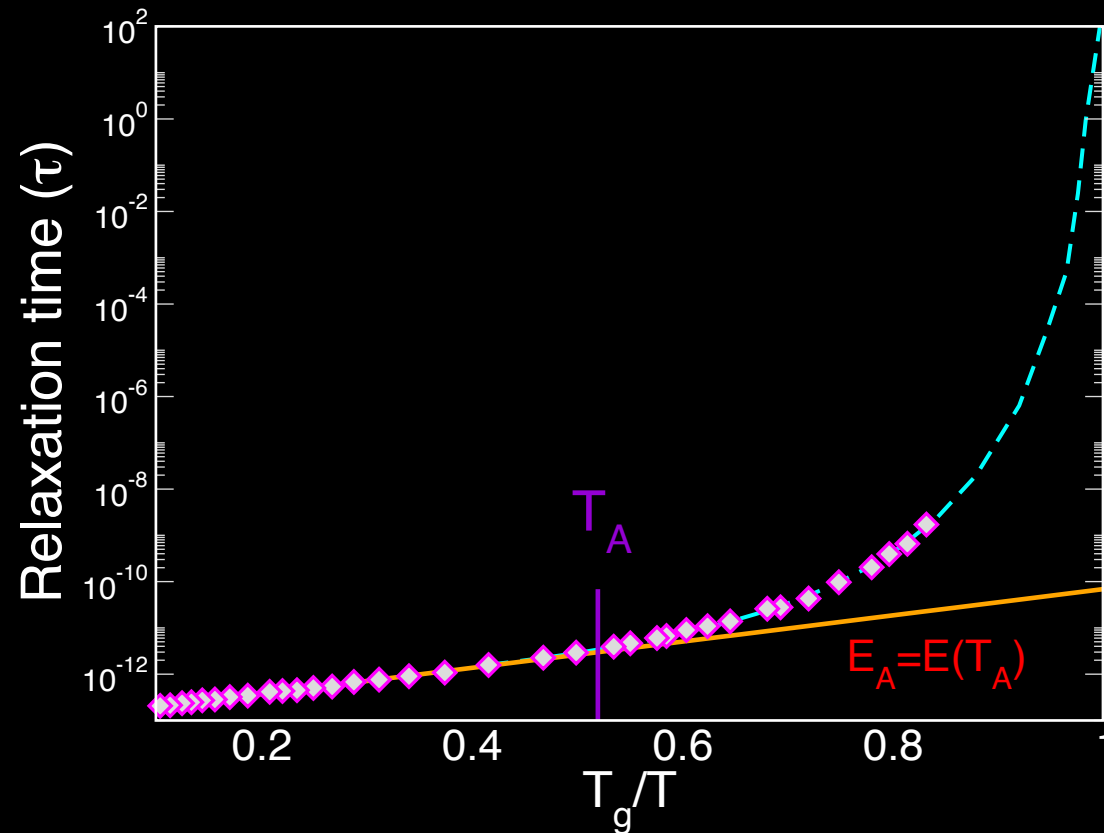
Ideal Mono-dispersion of Nanoparticles  
NP concentration  $\phi < 15\%$





$$\tau = \tau_0 e^{\frac{E(T)}{T}}$$

$$E(T) = T \ln \left( \frac{\tau}{\tau_0} \right)$$



## Activation Energy

Relaxation time can be parameterized by the Activation Energy  
 Can we describe AE in a more detailed way?



## Adams and Gibbs Theory

J. Chem. Phys. **43**, 139 (1965)

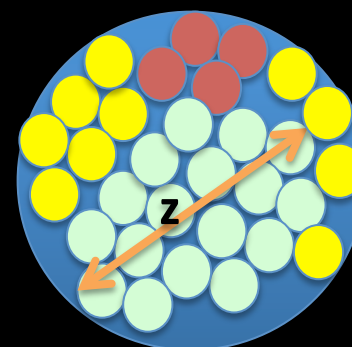
- Assumptions:
  - Relaxation time is an activated process

$$\tau = Ae^{z \frac{\Delta u}{k_B T}}$$

Where the activation energy is extensive in the size of CRR **z**

- The size **z** increases as temperature decreases

Cooperatively Rearranging Regions (CRR)

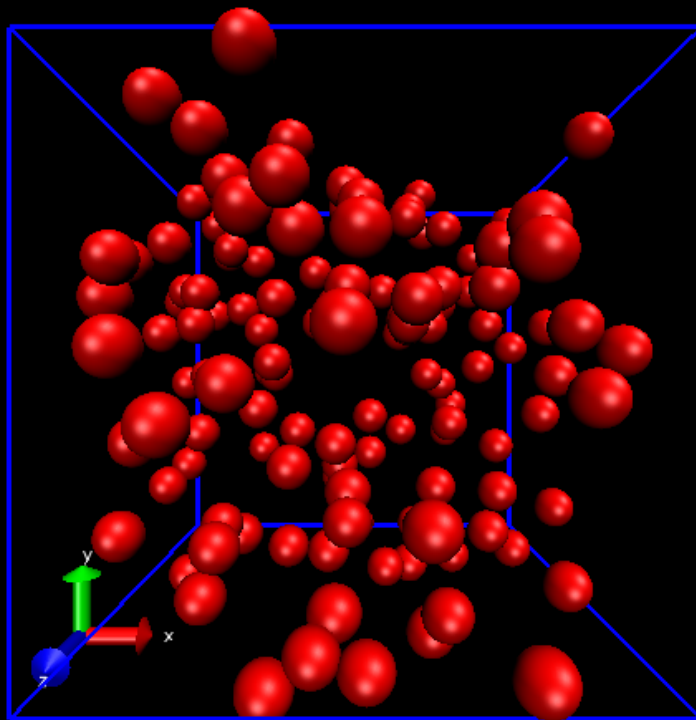


Probability of rearrange  $\sim$  size **z**  
Energy Barrier  $\sim$  size **z**

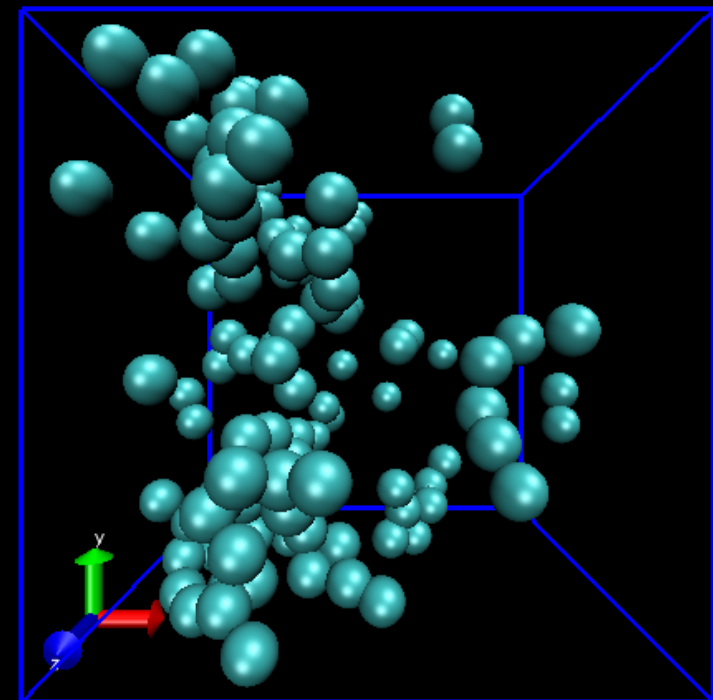
- Flaws:
  - The shape of CRR is poorly defined!



## Cooperatively Rearranging Regions (CRR)



Most mobile particles **hi T**



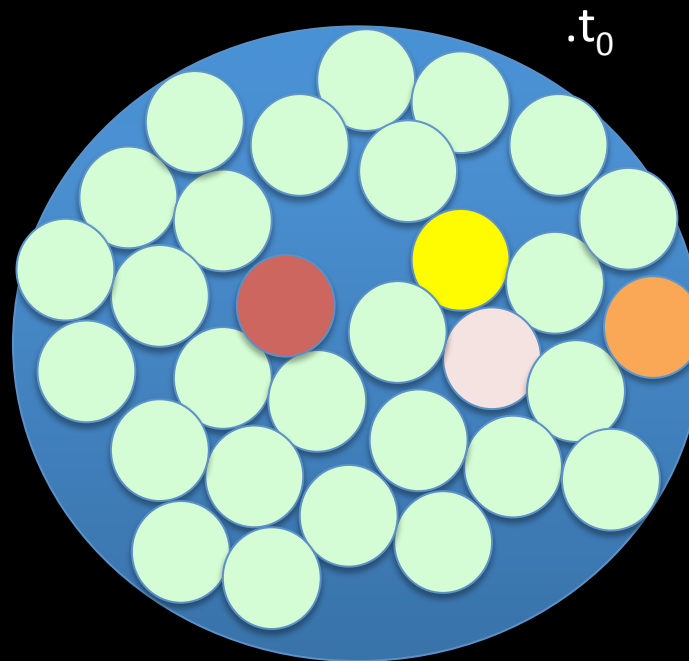
Most mobile particles **lo T**

Not all of particles move cooperatively

Below  $T_A$  : ~~Cluster of most mobile~~ particles increases

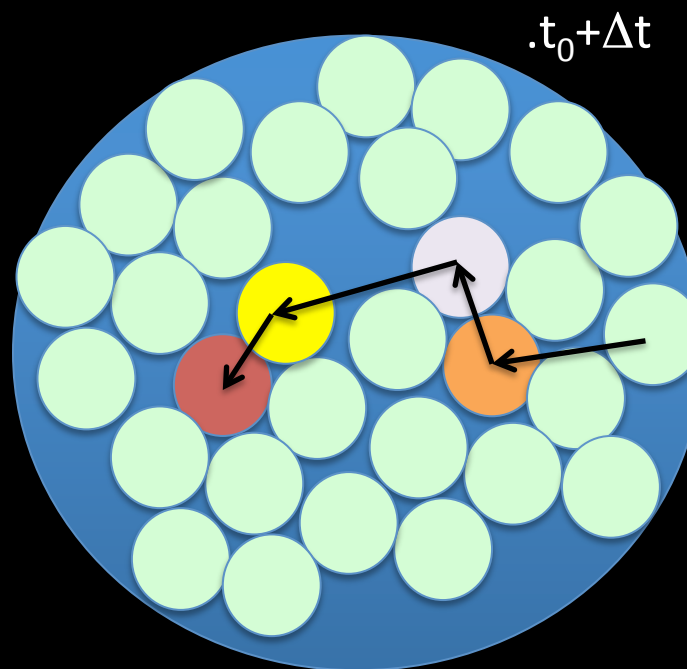


## Cooperatively Rearranging Regions (CRR)

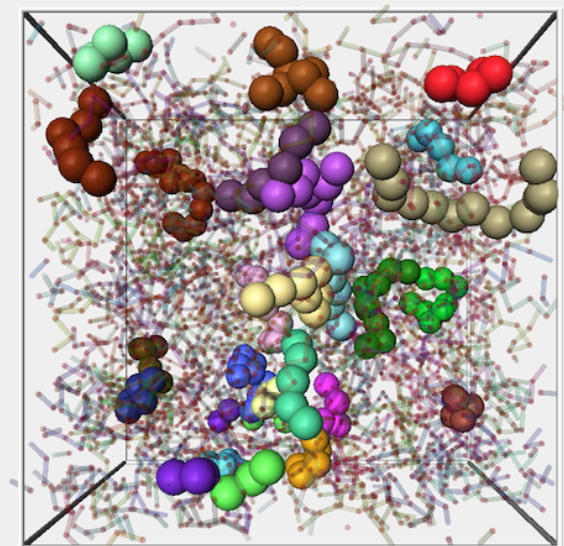




## Cooperatively Rearranging Regions (CRR)



*Soft Matter*, 2013,9, 241-254

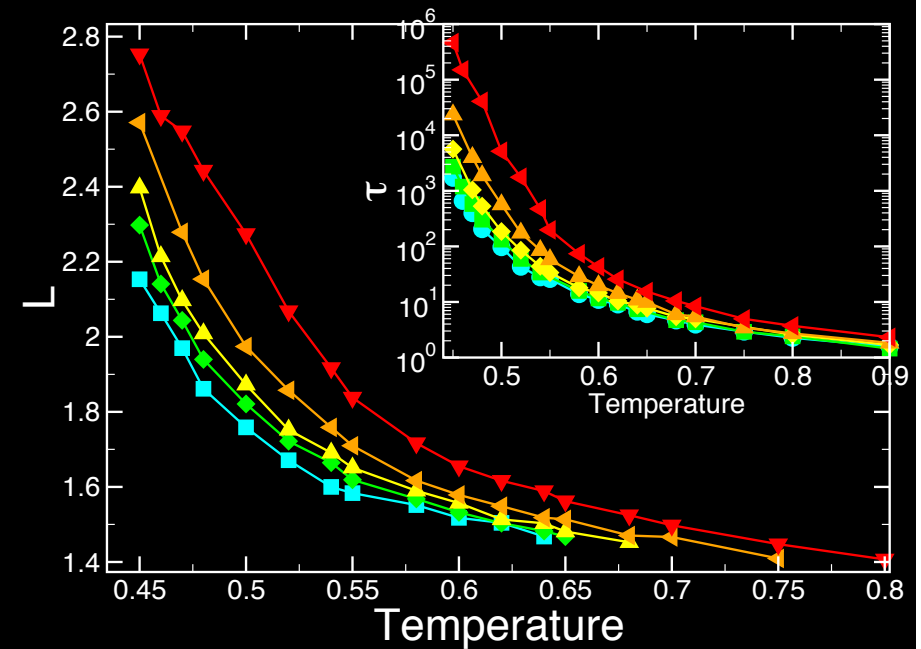
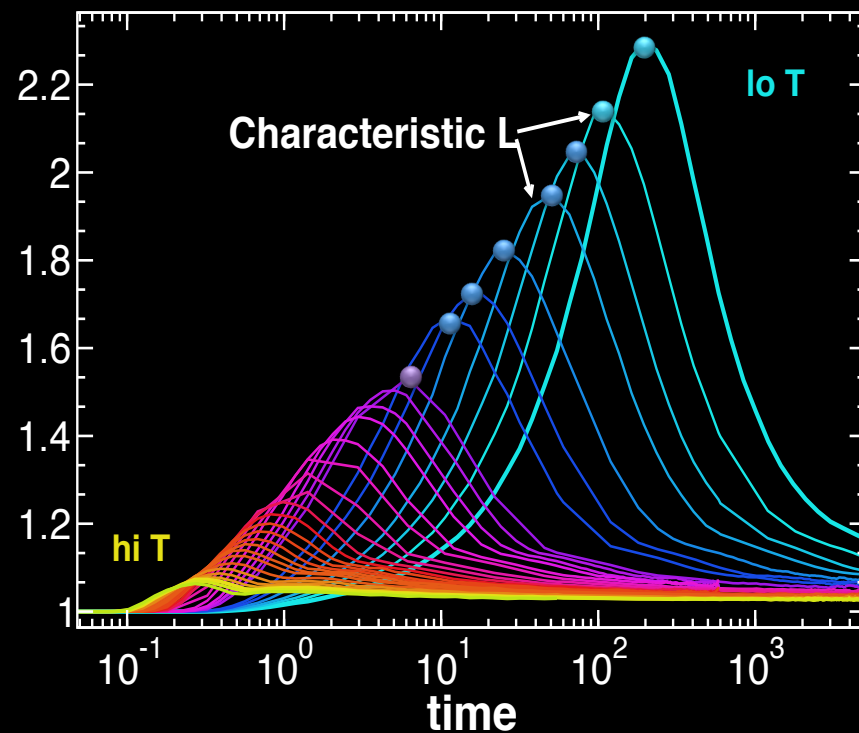


String-like motion  
Phys. Rev. Lett. 80, 2338–2341 (1998)



## Cooperatively Rearranging Regions

“string like motion”

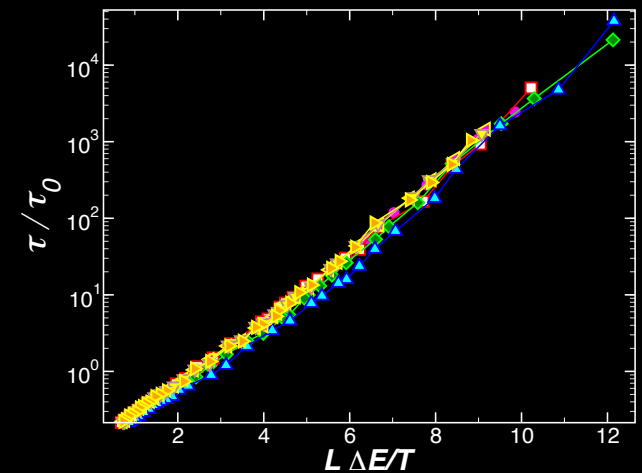
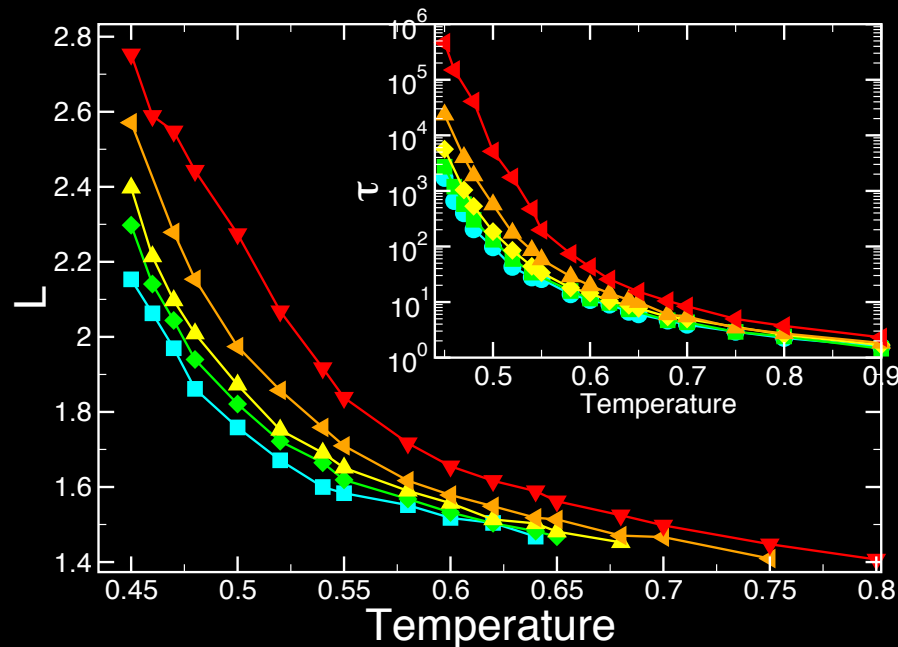






# Cooperatively Rearranging Regions

“string like motion”



References:

Phys. Rev. Lett., 2011,106, 115702

*Soft Matter*, 2013,9, 241-254

Length of the string like motion can be use as the size of CRR



## Goal

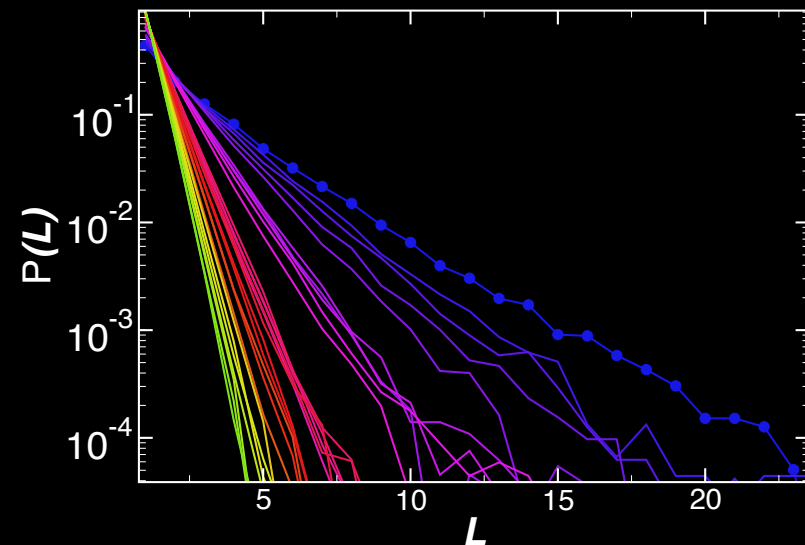
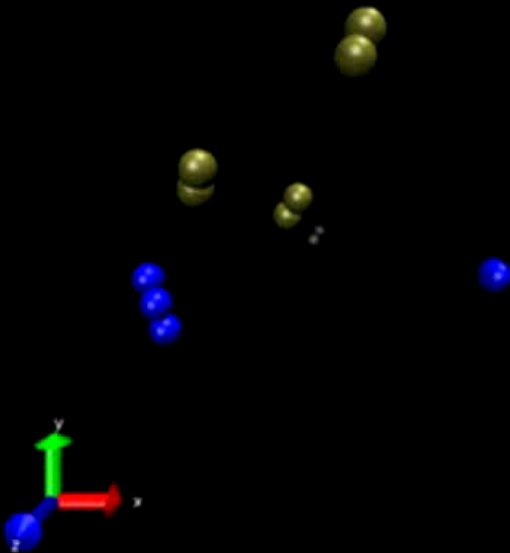
Explain  $L(T)$   $\longleftrightarrow$  Activation Energy  $\longleftrightarrow$  Relaxation Time

How do we explain the change in  $L(T)$ ?

What do we know?

They are dynamical chains




Their lengths have a exponential distribution

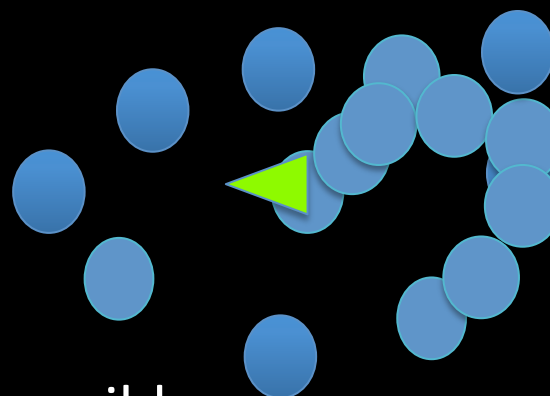




## Strings as equilibrium polymers?

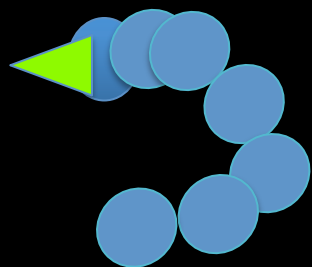
Let's consider:

- Monomers 
- Initiators 
- Monomer and Initiators react irreversible
- Only initiated units  form chains in chemical equilibrium



### Equilibrium Polymerization Model

J. Chem. Phys, Vol. 111, No. 15, pp. 7116–7130



$$\langle l(\Phi) \rangle = \frac{1}{1 - \Phi + \frac{r}{2}}$$

where:

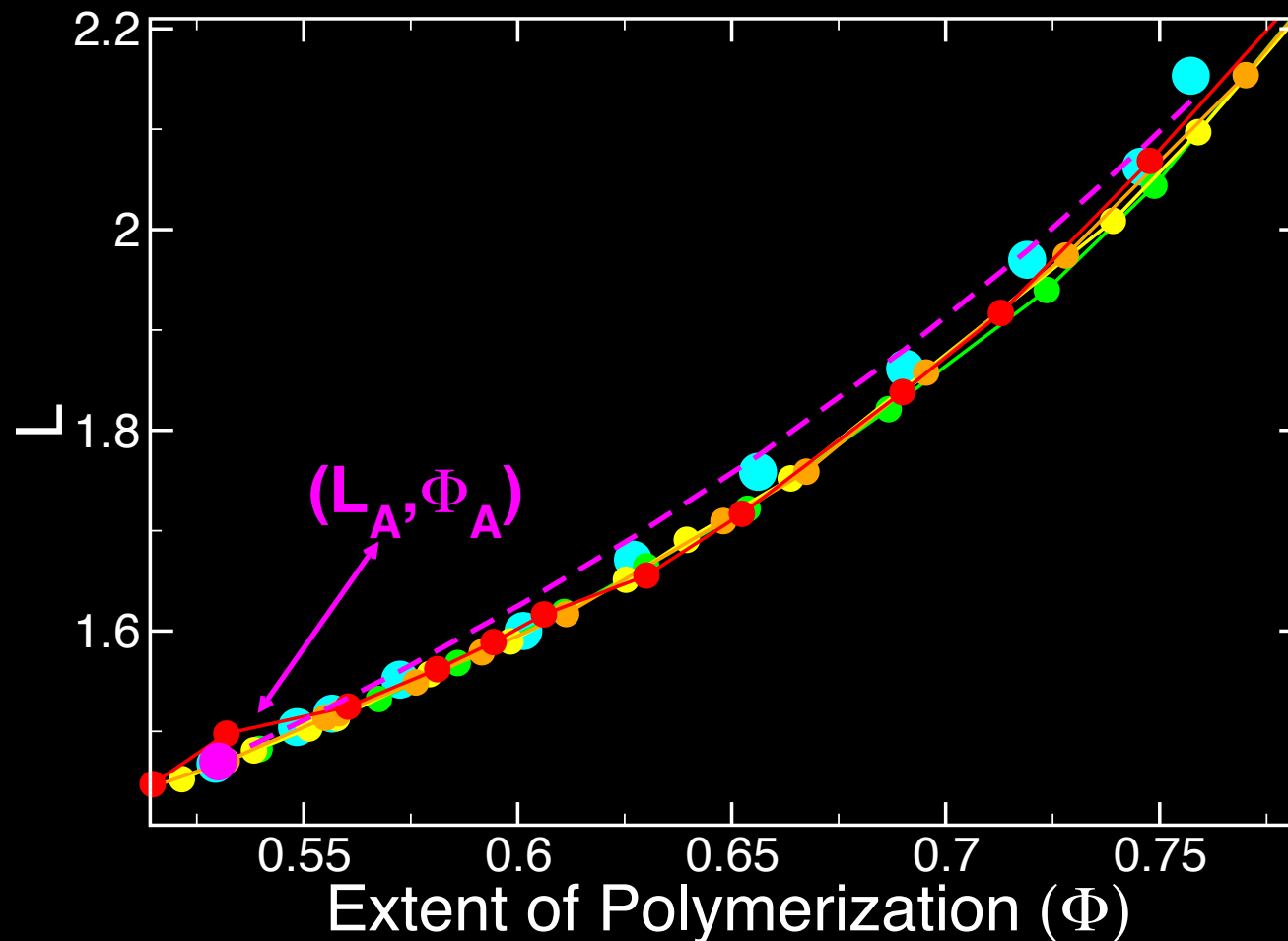
$\Phi$  Extent of polymerization

$r$  initiator concentration

$l$  length of the polymer

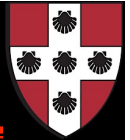


# Strings as an equilibrium polymer?



$$L(\Phi) = \frac{L_A \left(1 - \frac{\Phi_A}{2}\right)}{1 - \left(\Phi - \frac{\Phi_A}{2}\right)}$$

Pazmino et. al., "Self-Assembly Model for Correlated Motion in a Glass-Forming Polymer Melt" in preparation



## String-like motion “only in polymer melts?”

### Simulations:

- ✓ Kob-Anderson model *Physics Letters A 350 (2006)*
- ✓ Interfacial dynamics of grain boundaries
- ✓ Interfacial dynamics in nanoparticles
- ✓ Proteins
- ✓ Water *(to be published)*
- ✓ Lipids *(in press)*

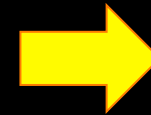
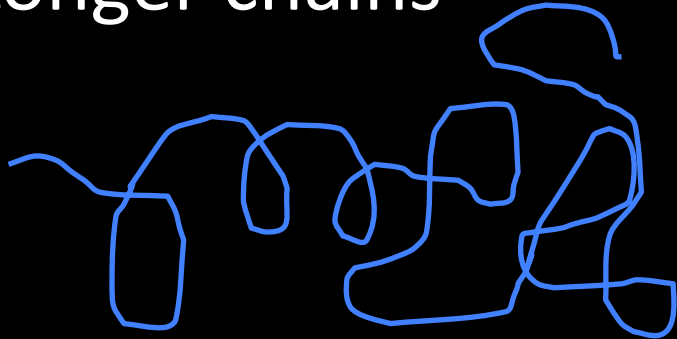
### Experiments:

- ✓ Strings have been observed experimentally in the amorphous interfacial region of crystals
- ✓ Particle tracking measurements of colloidal particle *Phys. Rev. Lett. 107 (2011)*

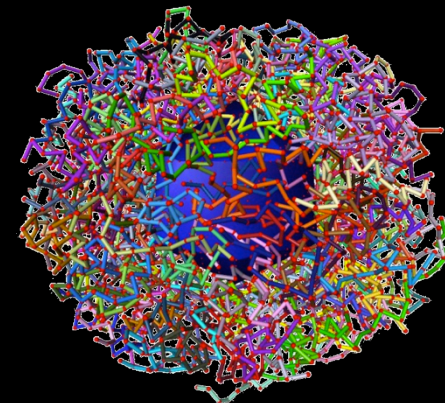
# Polymer Dynamics

## Computational Demands:

- Lower temperatures
- Longer chains



- Polymer nano-composites :
  - Less than 1% vol frac.
  - More than ( 35,000 particles )



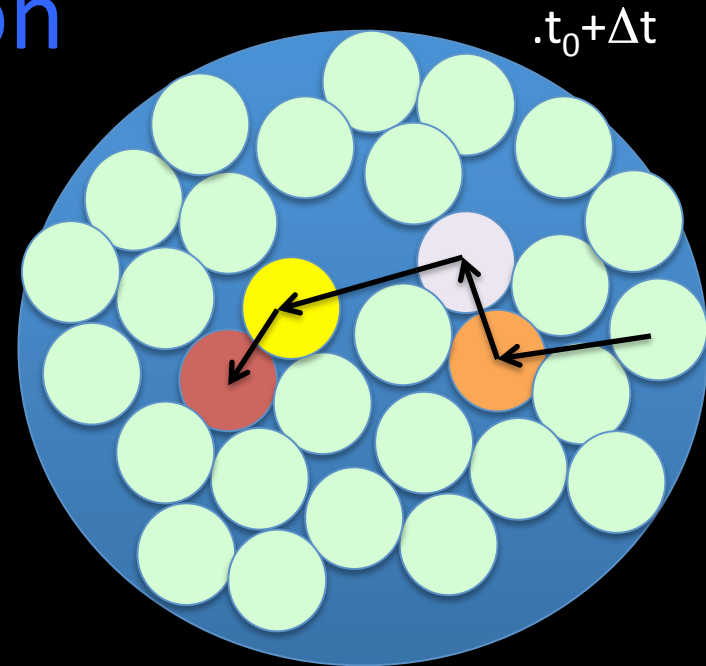
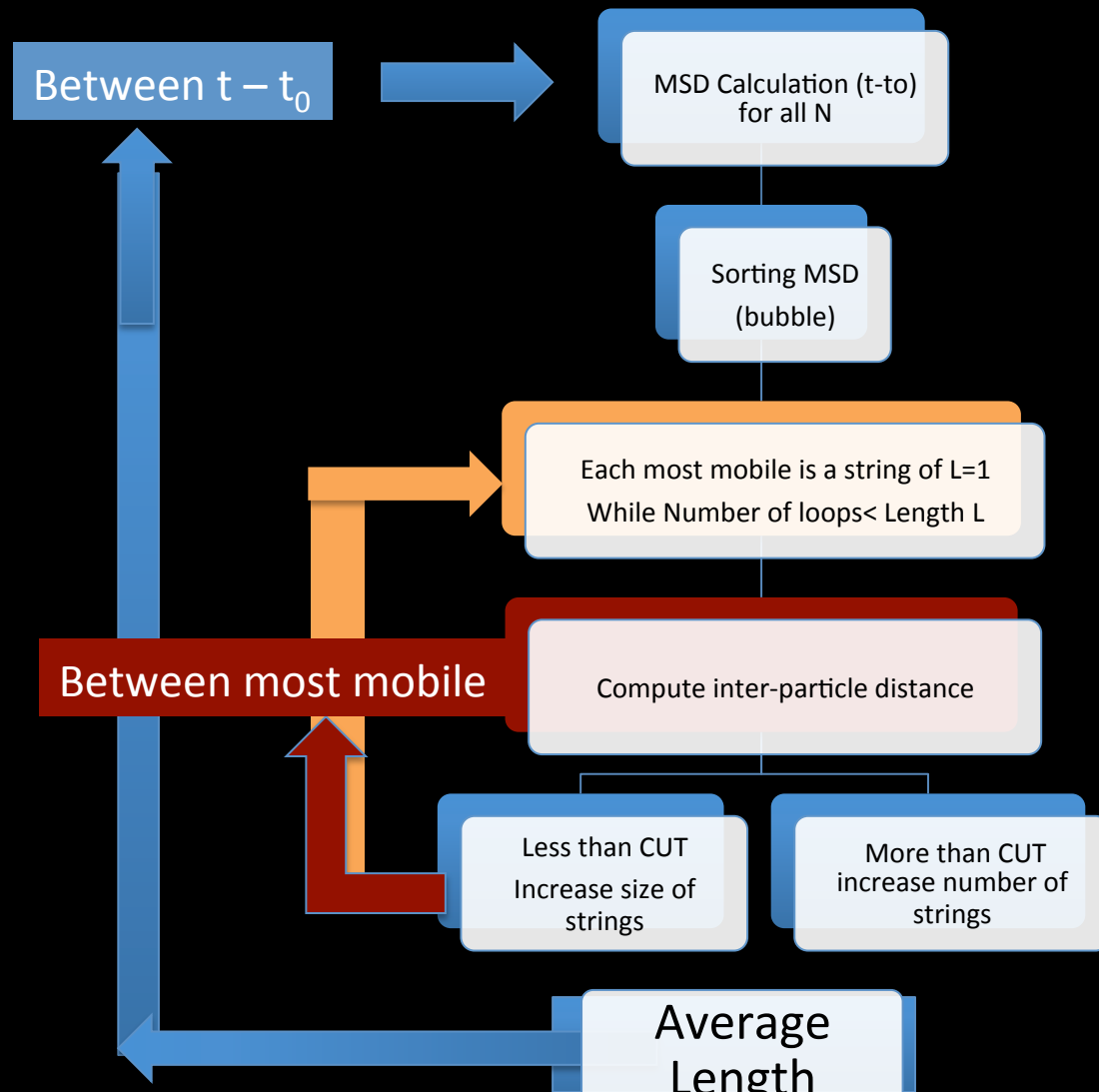
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# String Length Calculation

## Serial Key algorithms



# String Length Calculation

## GPU Challenges

- Make independent threads (Single MSD particle a thread?)
- Memory Allocation

First Target systems

Particles	$400 * 175 = 70,000$	Time steps	100
	$200 * 700 = 140,000$		800

– Using single float precision

$3 * 4\text{Bytes} * 70,000 * 2 = 1680\text{MB}$  vs 100 t.s 5.6GB

- How to scale to much bigger systems
- Among many others!!

## Possible starting points...

- Single MSD particle a thread?
- Arrange Memory to sort at each  $\Delta t$
- Flag identification of Inter-particle distance among all, at all  $t$
- Reduction scheme to average most mobile

**THANKS!**