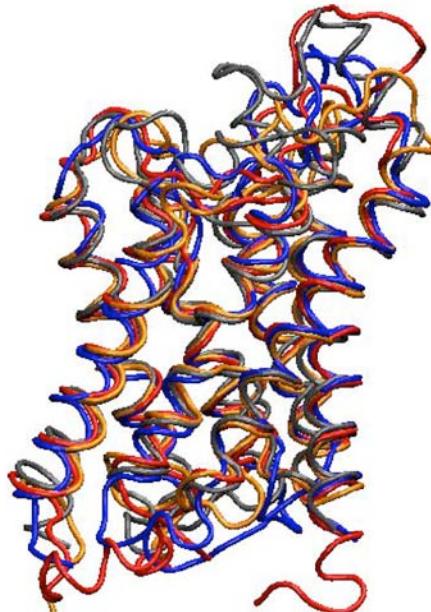


Sequence and Structure Alignment

Z. Luthey-Schulten, UIUC
Chicago, 2005



VMD 1.83

Multiple Sequence Alignment

F... To... H...

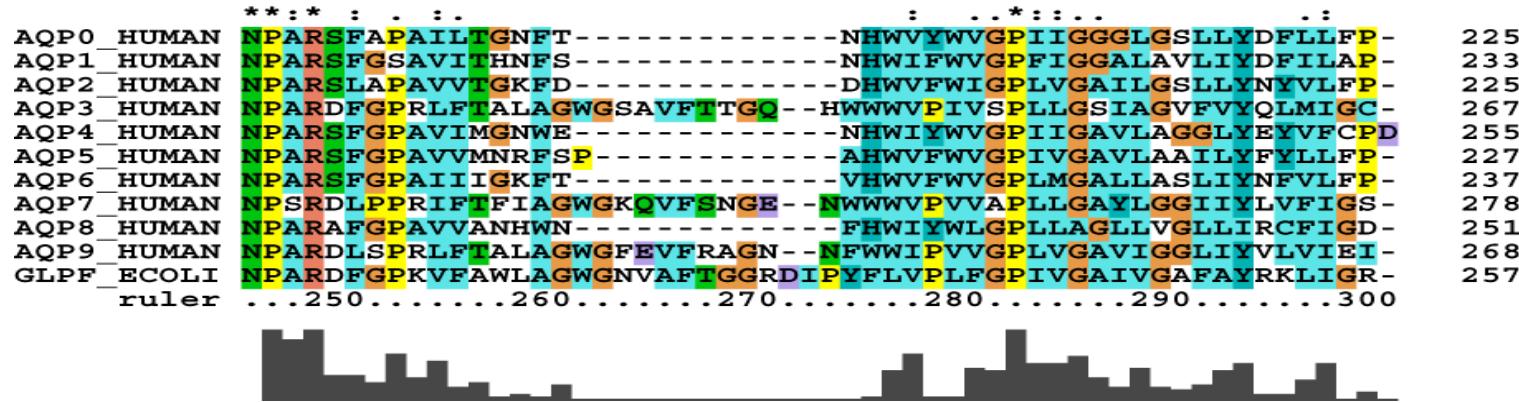
Align Molecules... FASTA Highlight PDB Pairwise RMSD

Sequence Display

	ifqy	lj4n	llda	lrc2
-----	-KLFWRRAVVAEFLATTLFVFISIGSAL-GF-KY---	-PVGNNQTAQVDNVKVSLAFLGLSIATLAQS-VGHISGAHLNPAVTLGLLSCQIISIF-RAI		
MASEFKKKLFWRAVVAAEFLAMILFIFISIGSAL-GF-HYFIKSNQT-TGAVQDNVKVSLAFLGLSIATLAQSVGH-ISGAHLNPAVTLGLLSCQ-1SVLRAI				
-----	-TLEGQClIAEFLGTGLLIFFGVGCVAA-LKVA-----	G-A-SFGQWEISVINGLGVAMAIYLTA-GVSGAHLNPAVTIALNLFA-CFDKRRV		
MFRKLAAECFGTFWLVFGGCGSAVLA-AG-----	PPE-LGIGFAGVALAFGLTVLTMAFAVG-HISGGHEPNPAVTIGLWAGG-RFPAKEV			

Why Look at More Than One Sequence?

1. Multiple Sequence Alignment shows patterns of conservation



2. What and how many sequences should be included?

3. Where do I find the sequences and structures for MS alignment?

4. How to generate pairwise and multiple sequence alignments?

Sequence-Sequence Alignment

- Smith-Watermann Seq. 1: a₁ a₂ a₃ - - a₄ a₅...a_n
- Needleman-Wunsch Seq. 2: c₁ - c₂ c₃ c₄ c₅ - ...c_m

Sequence-Structure Alignment

- Threading
- Hidden Markov, Clustal

Structure-Structure Alignment

- STAMP - Barton and Russell
- CE - Bourne et al.

Sequence Database Searches

- Blast and Psi-Blast

Sequence-Sequence Alignment

- Smith-Watermann
- Needleman-Wunsch

Profile 1: A₁ A₂ A₃ - - A₄ A₅...A_n

Profile 2: C₁ - C₂ C₃ C₄ C₅ - ...C_m

Sequence-Structure Alignment

- Threading
- Hidden Markov, Clustal

Structure-Structure Alignment

- STAMP - Barton and Russell SCOP, Astral
- CE - Bourne et al. PDB

Sequence Database Searches

- Blast and Psi-Blast NCBI Swiss Prot

ExPASy Home page	Site Map	Search ExPASy	Contact us	PROSITE	Proteomics tools
Search <input type="text" value="Swiss-Prot/TrEMBL"/> <input type="button" value="for"/> <input type="text" value="aqp"/> <input type="button" value="Go"/> <input type="button" value="Clear"/>					



Swiss-Prot
Protein knowledgebase
TrEMBL
Computer-annotated supplement to Swiss-
Prot



The [UniProt Knowledgebase](#) consists of:

- **Swiss-Prot**; a curated protein sequence database which strives to provide a high level of annotation (such as the description of the function of a protein, its domains structure, post-translational modifications, variants, etc.), a minimal level of redundancy and high level of integration with other databases [[More details](#) / [References](#) / [Linking to Swiss-Prot](#) / [User manual](#) / [Recent changes](#) / [Commercial users](#) / [Disclaimer](#)].
- **TrEMBL**; a computer-annotated supplement of Swiss-Prot that contains all the translations of EMBL nucleotide sequence entries not yet integrated in Swiss-Prot.

These databases are developed by the Swiss-Prot groups [at SIB](#) and [at EBI](#).

UniProt Release 3.2 consists of:

Swiss-Prot Release 45.2 of 23-Nov-2004: 164201 entries ([More statistics](#))

TrEMBL Release 28.2 of 23-Nov-2004: 1503829 entries ([More statistics](#))

> **Swiss-Prot headlines**

Major update of C.elegans entries (Read [more...](#))

 ExPASy Home page	Site Map	Search ExPASy	Contact us	Swiss-Prot					
Hosted by NCSC US	Mirror sites:	Australia	Bolivia	Brazil <small>(new)</small>	Canada	China	Korea	Switzerland	Taiwan
Search <input type="text" value="Swiss-Prot/TrEMBL"/> for <input type="text" value="aqp"/> <input type="button" value="Go"/> <input type="button" value="Clear"/>									

Search in Swiss-Prot and TrEMBL for: aqp

Swiss-Prot Release 45.2 of 23-Nov-2004

TrEMBL Release 28.2 of 23-Nov-2004

-
- Number of sequences found in [Swiss-Prot](#)(89) and [TrEMBL](#)(122): **211**
 - Note that the selected sequences can be saved to a file to be later retrieved; to do so, go to the [bottom](#) of this page.
 - For more directed searches, you can use the Sequence Retrieval System [SRS](#).
-

Search in Swiss-Prot: There are matches to 89 out of 164201 entries

[**AQP1_BOVIN \(P47865\)**](#)

Aquaporin-CHIP (Water channel protein for red blood cells and kidney proximal tubule) (Aquaporin 1) (Water channel protein CHIP29). {GENE: Name=AQP1} - Bos taurus (Bovine)

[**AQP1_HUMAN \(P29972\)**](#)

Aquaporin-CHIP (Water channel protein for red blood cells and kidney proximal tubule) (Aquaporin 1) (AQP-1) (Urine water channel). {GENE: Name=AQP1; Synonyms=CHIP28} - Homo sapiens (Human)

[**AQP1_MOUSE \(Q02013\)**](#)

Aquaporin-CHIP (Water channel protein for red blood cells and kidney proximal tubule) (Aquaporin 1) (Early response protein DER2). {GENE: Name=Aqp1} - Mus musculus (Mouse)

Search for

NiceProt View of Swiss-Prot: P47865

[Printer-friendly view](#)[Submit update](#)[Quick BlastP search](#)[\[Entry info\]](#) [\[Name and origin\]](#) [\[References\]](#) [\[Comments\]](#) [\[Cross-references\]](#) [\[Keywords\]](#) [\[Features\]](#) [\[Sequence\]](#) [\[Tools\]](#)

Note: most headings are clickable, even if they don't appear as links. They link to the user manual or other documents.

Entry information

Entry name	AQPI_BOVIN
Primary accession number	P47865
Secondary accession numbers	None
Entered in Swiss-Prot in	Release 33, February 1996
Sequence was last modified in	Release 44, July 2004
Annotations were last modified in	Release 45, October 2004

Name and origin of the protein

Protein name	Aquaporin-CHIP
Synonyms	Water channel protein for red blood cells and kidney proximal tubule Aquaporin 1 Water channel protein CHIP29
Gene name	Name: AQP1
From	Bos taurus (Bovine) [TaxID: 9913]
Taxonomy	Eukaryota; Metazoa; Chordata; Craniata; Vertebrata; Euteleostomi; Mammalia; Eutheria; Cetartiodactyla; Ruminantia; Pecora; Bovidae; Bovinae; Bos.

References

- [1] SEQUENCE FROM NUCLEIC ACID.
TISSUE=Ocular ciliary epithelium;

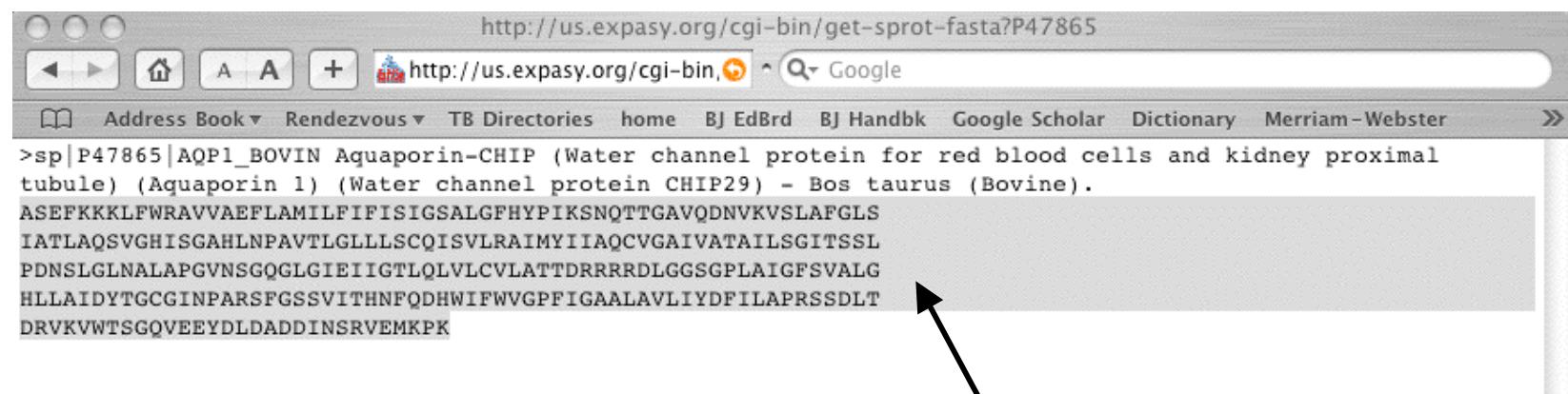
Snapz Pro X

Sequence information

Length: 270 AA | Molecular weight: 28669 Da | CRC64: F3ECAD45DCCDB309 [This is a checksum on the sequence]

10	20	30	40	50	60
ASEFKKKLFW	RAVVAEFLAM	ILFIFISIGS	ALGFHYPPIKS	NQTTGAVQDN	VKVSLAFGLS
70	80	90	100	110	120
IATLAQSVGH	ISGAHLNPBV	TLGLLLSCQI	SVLRAIMYII	AQCVGAIVAT	AILSGITSSL
130	140	150	160	170	180
PDNSLGLNAL	APGVNSGQGL	GIEIIGTLQL	VLCVLATTDR	RRRDLGGSGP	LAIGFSVALG
190	200	210	220	230	240
HLLAIDYTGC	GINPARSFGS	SVITHNFQDH	WIFWVGPFIG	AALAVLIYDF	ILAPRSSDLT
250	260	270			
DRVKVWTSGQ	VEEYDLDADD	INSRVERMKPK			

P47865 in FASTA format



cut



NCBI

protein–protein BLAST

Nucleotide

Protein

Translations

Retrieve results for an
RID[Search](#)

```
ASEFKKKLFWRRAVVAEFLAMILFIFISIGSALGFHYPPIKSNQTTGAVQDNVKVSLAFLS
IATLAQSVGHISGAHLNPATLGLLLSCQISVLRAIMYIIAQCVGAIVATAILSGITSSL
PDNSLGLNALAPGVNSGQGLGIEIIGTLQLVLCLVLTTRRRRLGGSGPLAIGFSVALG
HLLAIDYTGCINPARSGFSSVTHNFQDHWIFWVGPFIGAALAVLIYDFILAPRSSDLT
DRVKVWTSGQVEEYDLDADDINSRVEMKPK
```

**paste**[Set subsequence](#) From: To: [Choose database](#) [Do CD-Search](#) Now: or **Options** for advanced blasting[Limit by entrez query](#) or select from: [Composition-based statistics](#) [Choose filter](#) Low complexity Mask for lookup table only Mask lower case[Expect](#) [Word Size](#) [Matrix](#) Gap Costs **Choice of
substitution matrix
and gap penalty**



Your request has been successfully submitted and put into the Blast Queue.

Query = (270 letters)

Putative conserved domains have been detected, click on the image below for detailed results.



The request ID is 1102423974-1792-209874599488.BLASTQ4

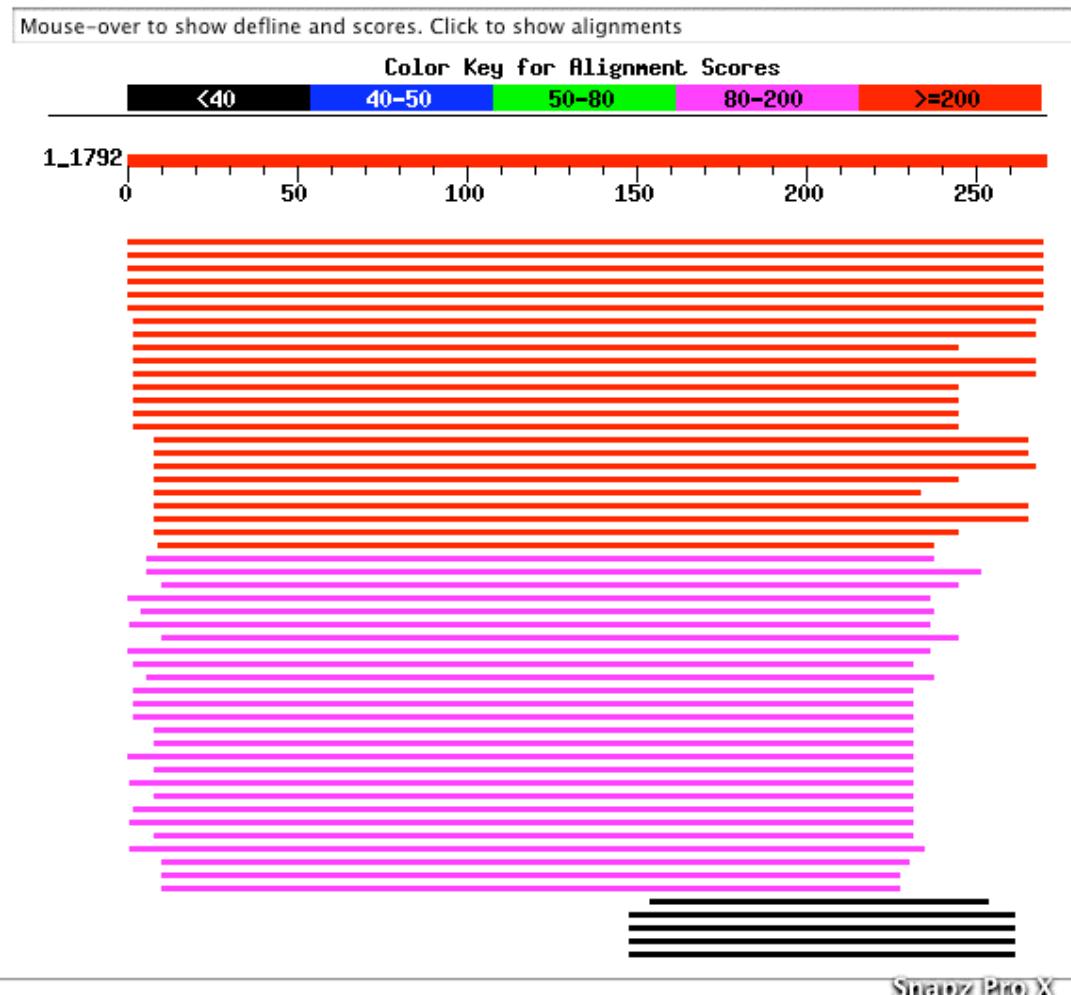
Format! or **Reset all**

The results are estimated to be ready in 28 seconds but may be done sooner.

Please press "FORMAT!" when you wish to check your results. You may change the formatting options for your result via the form below and press "FORMAT!" again. You may also request results of a different search by entering any other valid request ID to see other recent jobs.

[Taxonomy reports](#)

Distribution of 164 Blast Hits on the Query Sequence



Sequences producing significant alignments:

		score	e	bits	Value	
gi 1351965 sp P47865 AQP1_BOVIN	Aquaporin-CHIP (Water chann...	530	e-150	G		
gi 3023310 sp P56401 AQP1_SHEEP	Aquaporin-CHIP (Water chann...	521	e-148			
gi 267412 sp P29972 AQP1_HUMAN	Aquaporin-CHIP (Water channe...	481	e-136	G		
gi 543832 sp Q02013 AQP1_MOUSE	Aquaporin-CHIP (Water channe...	477	e-134	G		
gi 47117785 sp P29975 AQP1_RAT	Aquaporin-CHIP (Water channe...	474	e-134	G		
gi 1703359 sp P50501 AOPA_RANES	Aquaporin FA-CHIP	431	e-121			
gi 730026 sp Q06019 MIP_RANPI	Lens fiber major intrinsic pr...	238	1e-62			
gi 127102 sp P06624 MIP_BOVIN	Lens fiber major intrinsic pr...	236	3e-62	G		
gi 728874 sp P41181 AQP2_HUMAN	Aquaporin-CD (AQP-CD) (Water...	235	7e-62	G		
gi 127106 sp P09011 MIP_RAT	Lens fiber major intrinsic prot...	233	5e-61	G		
gi 47117800 sp P51180 MIP_MOUSE	Lens fiber major intrinsic ...	231	1e-60	G		
gi 266537 sp P30301 MIP_HUMAN	Lens fiber major intrinsic pr...	231	1e-60	G		
gi 3913084 sp O62735 AQP2_SHEEP	Aquaporin-CD (AQP-CD) (Wate...	231	2e-60			
gi 23503041 sp P56402 AQP2_MOUSE	Aquaporin-CD (AQP-CD) (Wat...	228	9e-60	G		
gi 461529 sp P34080 AQP2_RAT	Aquaporin-CD (AQP-CD) (Water c...	225	8e-59	G		
gi 1351967 sp P47863 AQP4_RAT	Aquaporin 4 (WCH4) (Mercurial...	222	8e-58	G		
gi 47116232 sp O923J4 AQP4_DIPME	Aquaporin 4	219	4e-57			
gi 1703358 sp P55064 AQP5_HUMAN	Aquaporin 5	219	5e-57	G		
gi 2506859 sp P55087 AQP4_HUMAN	Aquaporin 4 (WCH4) (Mercuri...	218	2e-56	G		
gi 7387547 sp O9WTY4 AQP5_MOUSE	Aquaporin 5	218	2e-56			
gi 7387545 sp O77750 AQP4_BOVIN	Aquaporin 4 (WCH4) (Mercuri...	217	3e-56			
gi 47117859 sp P55088 AQP4_MOUSE	Aquaporin 4 (WCH4) (Mercur...	216	4e-56	G		
gi 1351968 sp P47864 AQP5_RAT	Aquaporin 5	215	8e-56	G		
gi 32469581 sp O9NHW7 AQP_AEDAE	Aquaporin AQP _{AE.a}	201	1e-51			
gi 32469580 sp O25074 AQP_HAEIE	Aquaporin (Water channel 1)...	192	5e-49			
gi 2497939 sp Q13520 AQP6_HUMAN	Aquaporin 6 (Aquaporin-2 li...	192	9e-49	G		
gi 47115531 sp O9WTY0 AQP6_RAT	Aquaporin 6	191	2e-48	G		
gi 21431896 sp P43287 PI22_ARATH	Aquaporin PIP2.2 (Plasma m...	189	5e-48	G		
gi 32469582 sp O9V5Z7 AQP_DROME	Aquaporin	188	1e-47	G		
gi 1175013 sp P43286 PI21_ARATH	Aquaporin PIP2.1 (Plasma me...	187	2e-47	G		
gi 47115796 sp O8C4A0 AQP6_MOUSE	Aquaporin 6	185	1e-46	G		
gi 267136 sp P30302 PI23_ARATH	Aquaporin PIP2.3 (Plasma mem...	184	1e-46	G		
gi 32363439 sp O9ZV07 PI26_ARATH	Probable aquaporin PIP2.6 ...	184	1e-46	Snooz Pro X		

Final Result: Sequence Alignment - Approximate

□>gi|46395801|sp|Q88F17|AQPZ_PSEPK G Aquaporin Z
Length = 230

Score = 119 bits (299), Expect = 6e-27
Identities = 70/186 (37%), Positives = 105/186 (56%), Gaps = 12/186 (6%)

Query: 53 VSLAFGLSIATLAQSVGHISGAHLNPAVTLGLLLSCQISVLRAIMYIIAQCVGAIIVATAI 112
 V+ AFGL++ T+A ++GHISG HLNPAV+ GL++ + + Y+IAQ +GAI+A +
Sbjct: 40 VAFAFGLTVLTMAFAIGHISGCHLNPAVSFGLVVGGRFPAKELLPYVIAQVIGAILAAGV 99

Query: 113 LSGITSSLP--DNSLGL--NALAP----GVNSGQGLGIEIIIGTLQLVLCVLATTDRRRD 164
 + I S + S GL N A G G G E++ T ++ ++ TD R
Sbjct: 100 IYLIASGKAGFELSAGLASNGYADHSPGGYTLGAGFVSEVVMTAMFLVVIMGATDARAP- 158

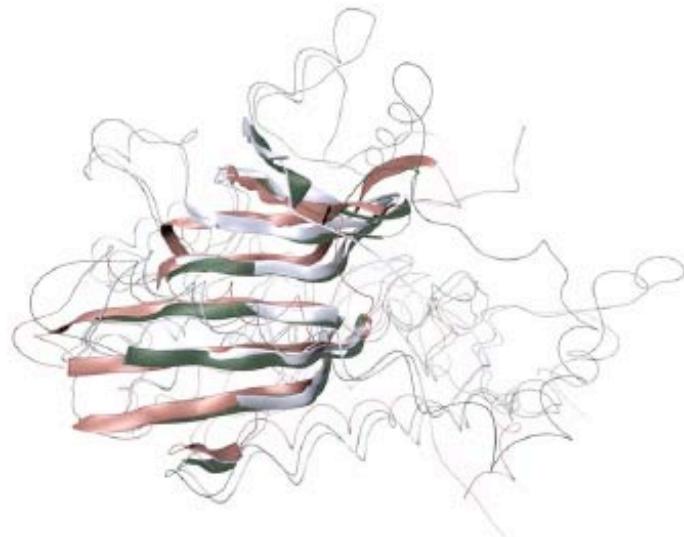
Query: 165 LGGSGPLAIGFSVALGHLLAIDYTGCINPARSGSSVITHNF--QDHWIFWVGPFIGAA 222
 G P+AIG ++ L HL++I T +NPARS G ++ + Q W+FWV P IGAA
Sbjct: 159 -AGFAPIAIGLALTЛИHLISIPVTNTSVNPARSTGPALFVGGWALQQLWLFWVAPLIGAA 217

Query: 223 LAVLIY 228
 + +Y
Sbjct: 218 IGGALY 223

University of Illinois at Urbana-Champaign
Luthey-Schulten Group
Theoretical and Computational Biophysics Group
Summer School 2004 - University of Western Australia, Perth

Sequence Alignment Algorithms

*Tutorial for the
material of this
lecture available*



Rommie Amaro

Felix Autenrieth

Brijeet Dhaliwal

Barry Isralewitz

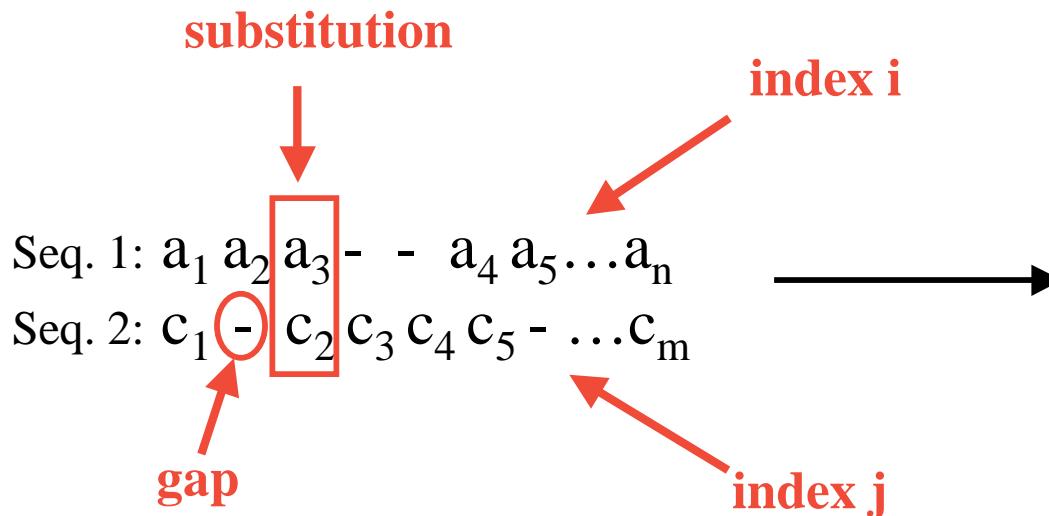
Zaida Luthey-Schulten

Anurag Sethi

Taras Pogorelov

June 2004

Sequence Alignment & Dynamic Programming



number of possible alignments

$$= \binom{2n}{n} = 2^{2n} (\sqrt{n\pi})^{-1}$$

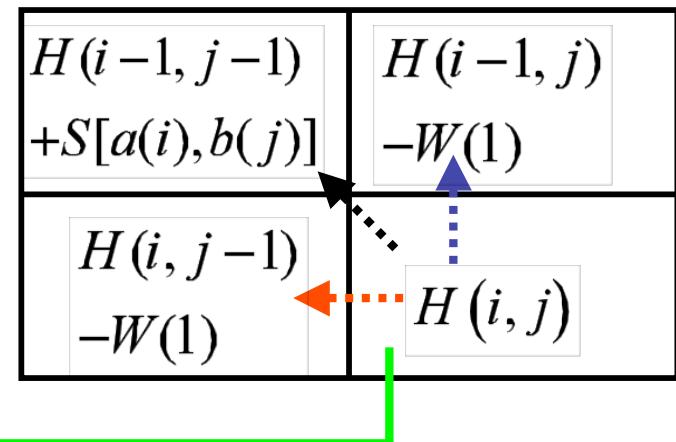
Smith-Waterman alignment algorithm

objective function

$$H(i, j) = \text{MAX} \begin{cases} H(i-1, j-1) + S[a(i), b(j)] \\ H(i, j-k) - W(k), \\ H(i-m, j) - W(m), 0 \end{cases}$$

substitution matrix

gap penalty



traceback defined
through choice of
maximum

Blosum 40 Substitution Matrix

AA not resolved

A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V	B	Z	X	
5	-2	-1	-1	-2	0	-1	1	-2	-1	-2	-1	-1	-3	-2	1	0	-3	-2	0	-1	-1	0	A
-2	9	0	-1	-3	2	-1	-3	0	-3	-2	3	-1	-2	-3	-1	-2	-2	-1	-2	-1	0	-1	R
-1	0	8	2	-2	1	-1	0	1	-2	-3	0	-2	-3	-2	1	0	-4	-2	-3	4	0	-1	N
-1	-1	2	9	-2	-1	2	-2	0	-4	-3	0	-3	-4	-2	0	-1	-5	-3	-3	6	1	-1	D
-2	-3	-2	-2	16	-4	-2	-3	-4	-4	-2	-3	-3	-2	-5	-1	-1	-6	-4	-2	-2	-3	-2	C
0	2	1	-1	-4	8	2	-2	0	-3	-2	1	-1	-4	-2	1	-1	-1	-1	-3	0	4	-1	Q
-1	-1	-1	2	-2	2	7	-3	0	-4	-2	1	-2	-3	0	0	-1	-2	-2	-3	1	5	-1	E
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0	-2	-3	-3	-2	-3	-3	-4	-4	4	2	-2	1	0	-3	-1	1	-3	-1	5	-3	-3	-1	V
-1	-1	4	6	-2	0	1	-1	0	-3	-3	0	-3	-3	-2	0	0	-4	-3	-3	5	2	-1	B
-1	0	0	1	-3	4	5	-2	0	-4	-2	1	-2	-4	-1	0	-1	-2	-2	-3	2	5	-1	Z
0	-1	-1	-1	-2	-1	-1	-1	-1	-1	-1	-1	0	-1	-2	0	0	-2	-1	-1	-1	-1	-1	X

Amino Acid Three Letter and One Letter Code

Amino acid	Three letter code	One letter code
alanine	ala	A
arginine	arg	R
asparagine	asn	N
aspartic acid	asp	D
asparagine or aspartic acid	asx	B
cysteine	cys	C
glutamic acid	glu	E
glutamine	gln	Q
glutamine or glutamic acid	glx	Z
glycine	gly	G
histidine	his	H
isoleucine	ile	I
leucine	leu	L
lysine	lys	K
methionine	met	M
phenylalanine	phe	F
proline	pro	P
serine	ser	S
threonine	thr	T
tryptophan	try	W
tyrosine	tyr	Y
valine	val	V

Sequence Alignment & Dynamic Programming

Seq. 1: $a_1 a_2 a_3 \dots a_4 a_5 \dots a_n$
 Seq. 2: $c_1 \dots c_2 c_3 c_4 c_5 \dots c_m$



number of possible alignments:

$$= \binom{2n}{n} = 2^{2n} (\sqrt{n\pi})^{-1}$$

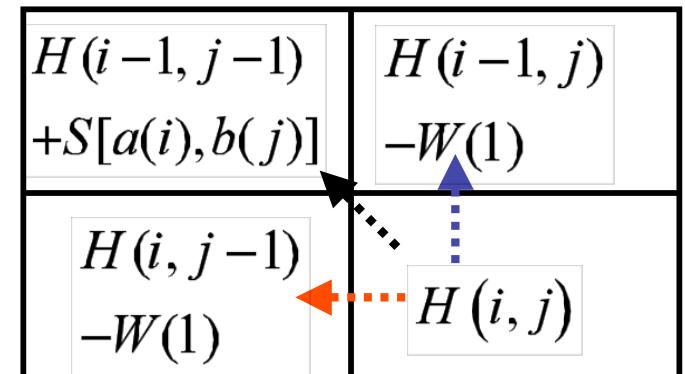
Needleman-Wunsch alignment algorithm

$$H(i, j) = \text{MAX} \begin{cases} H(i-1, j-1) + S[a(i), b(j)] \\ H(i, j-k) - W(k), \\ H(i-m, j) - W(m) \end{cases}$$

S : substitution matrix

A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V	B	Z	X	
5	-2	-1	-1	-2	0	-1	1	-2	-1	-2	-1	-3	-2	-1	0	-3	-2	0	-1	-1	0	A	
-2	9	0	-1	-3	2	-1	-3	0	-3	-2	3	-1	-2	-3	-1	-2	-2	-1	-2	-1	0	-1	R
-1	0	8	2	-2	1	-1	0	1	-2	-3	0	-2	-3	-2	1	0	-4	-2	-3	4	0	-1	N
-1	-1	2	9	-2	-1	2	-2	0	-4	-3	0	-3	-4	-2	0	-1	-5	-3	-3	6	1	-1	D
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0	2	1	-1	-4	8	2	-2	0	-3	-2	1	-1	-4	-2	1	-1	-1	-1	-3	0	4	-1	Q
-1	-1	1	2	-2	2	7	-3	0	-4	-2	1	-2	-3	0	0	-1	-2	-2	-3	1	5	-1	E
1	-3	0	-2	-3	-2	-3	8	-2	-4	-4	-2	-2	-3	-1	0	-2	-2	-3	-4	-1	-2	-1	G
-2	0	1	0	-4	0	0	-2	13	-3	-2	-1	1	-2	-2	-1	-2	-5	2	-4	0	0	-1	H
-1	-3	-2	-4	-4	-3	-4	-4	-3	6	2	-3	1	1	-2	-2	-1	-3	0	4	-3	-4	-1	I
-2	-2	-3	-3	-2	-2	-4	-2	2	6	-2	3	2	-4	-3	-1	-1	0	2	-3	-2	-1	L	
-1	3	0	0	-3	1	1	-2	-1	-3	-2	6	-1	-3	-1	0	0	-2	-1	-2	0	1	-1	K
-1	-1	-2	-3	-3	-1	-2	-2	1	1	3	-1	7	0	-2	-2	-1	-2	1	1	-3	-2	0	M
-3	-2	-3	-4	-2	-4	-3	-3	-2	1	2	-3	0	9	-4	-2	-1	1	4	0	-3	-4	-1	F
-2	-3	-2	-2	-5	-2	0	-1	-2	-2	-4	-1	-2	-4	11	-1	0	-4	-3	-3	-2	-1	-2	P
1	-1	1	0	-1	1	0	0	-1	-2	-3	0	-2	-2	-1	5	2	-5	-2	-1	0	0	0	S
0	-2	0	-1	-1	-1	-2	-1	-1	0	-1	-1	0	2	6	-4	-1	1	0	-1	0	T		
-3	-2	-4	-5	-6	-1	-2	-2	-5	-3	-1	-2	-2	1	-4	-5	-4	19	3	-3	-4	-2	-2	W
-2	-1	-2	-3	-4	-1	-2	-3	2	0	0	-1	1	4	-3	-2	-1	3	9	-1	-3	-2	-1	Y
0	-2	-3	-3	-2	-3	-3	-4	-4	4	2	-2	1	0	-3	-1	1	-3	-1	5	-3	-3	-1	V
-1	-1	4	6	-2	0	1	-1	0	-3	-3	0	-3	-3	-2	0	0	-4	-3	-3	5	2	-1	B
-1	0	0	1	-3	4	5	-2	0	-4	-2	1	-2	-4	-1	0	-1	-2	-2	-3	2	5	-1	Z
0	-1	-1	-1	-2	-1	-1	-1	-1	-1	-1	0	-1	-2	0	0	-2	-1	-1	-1	-1	-1	-1	X

gap penalty $W = -6$



Score Matrix H: Traceback

Needleman-Wunsch Global Alignment

Similarity Values

	M	G	K	P
M	5	-3	-1	-2
G	-3	6	-2	-2
P	-2	-2	-1	7
K	-1	-2	5	-1
K	-1	-2	5	-1
P	-2	-2	-1	7

Initialization of Gap Penalties

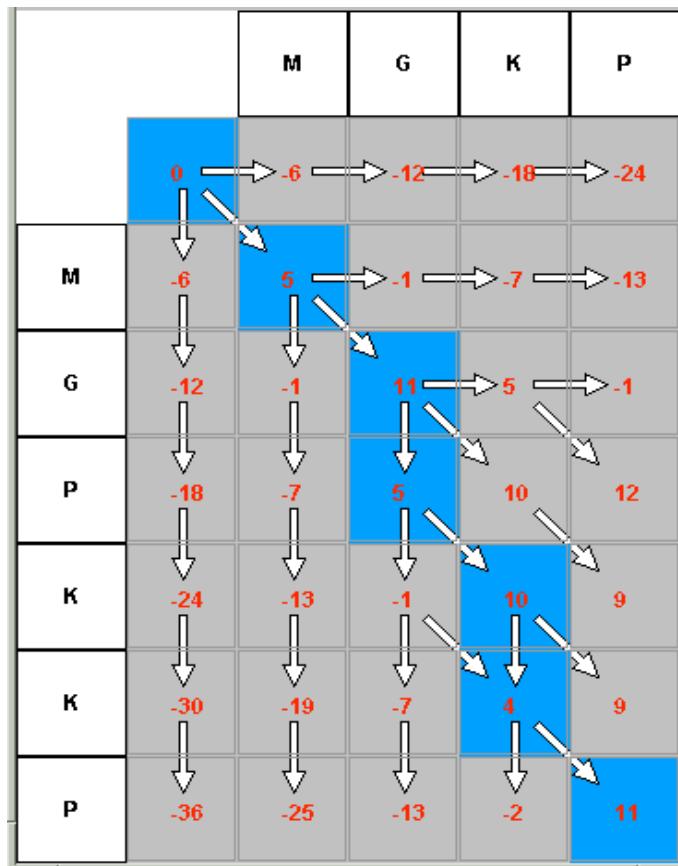
	M	G	K	P	
M	0	-6	-12	-18	-24
G	-6	5	-3	-1	-2
P	-12	-3	6	-2	-2
K	-18	-2	-2	-1	7
K	-24	-1	-2	5	-1
P	-30	-1	-2	5	-1
P	-36	-2	-2	-1	7

Filling out the Score Matrix H

	M	G	K	P
M	0 → -6 → -12 → -18 → -24	-6	5 → -1 → -7 → -13	
G	-12	-1 → 11	-2	-2
P	-18	-2	-1	7
K	-24	-1	-2	5
K	-30	-1	-2	5
P	-36	-2	-2	-1

	M	G	K	P
M	0 → -6 → -12 → -18 → -24	-6	5 → -1 → -7 → -13	
G	-12	-1 → 11	11 → 5 → -1	-1
P	-18	-7	5 → 10 → 12	12
K	-24	-13	-1 → 10 → 9	9
K	-30	-19	-7 → 4 → 9	9
P	-36	-25	-13 → -2	11

Traceback and Alignment



The Alignment

M	G	-	K	-	P
:	:		:		:
M	G	P	K	K	P

Traceback (blue) from optimal score

Protein Structure Prediction

1-D protein sequence

SISSIRVKSKRIQLG...

Homology Modeling/ FR

$$E = E_{match} + E_{gap}$$

Target Sequence

SISSRVKSKRIQLGLNQAE LAQKV-----GTTQ...
QFANEFKVRRRIKLGYTQ---TNVGEALAAVHGS...

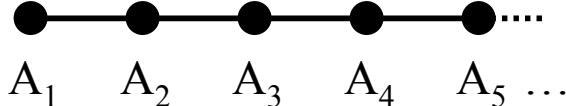
Known structure(s)

3-D protein structure

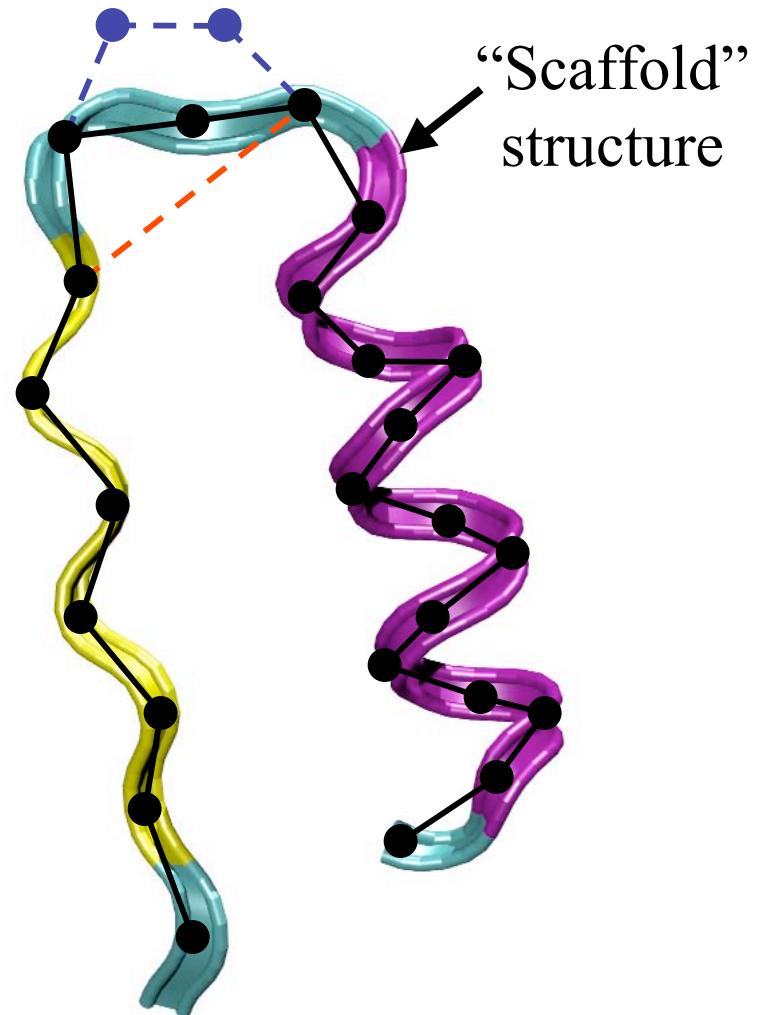


Sequence-Structure Alignment

Target sequence



Alignment between
target(s) and scaffold(s)



1. Energy Based Threading*

$$H = E_{contact} + E_{profile} + E_{H-bonds} + E_{gap}$$

$$E_{profile} = \sum_i^n \gamma^{(p)}(A_i, SS_i, SA_i)$$

$$E_{contact} = \sum_{i,j} \sum_{k=1}^2 \gamma_k^{(ct)}(A_i, A_j) * U(r_k - r_{ij})$$

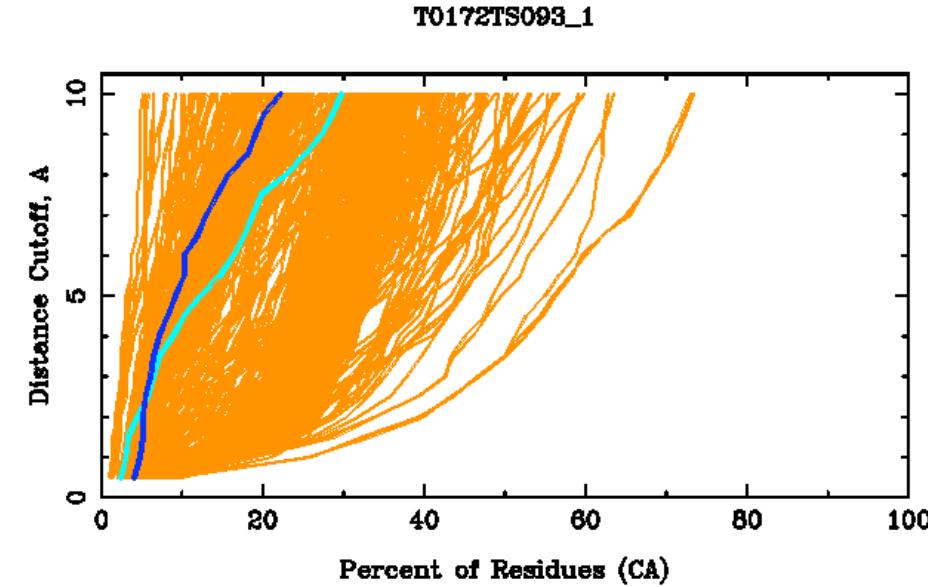
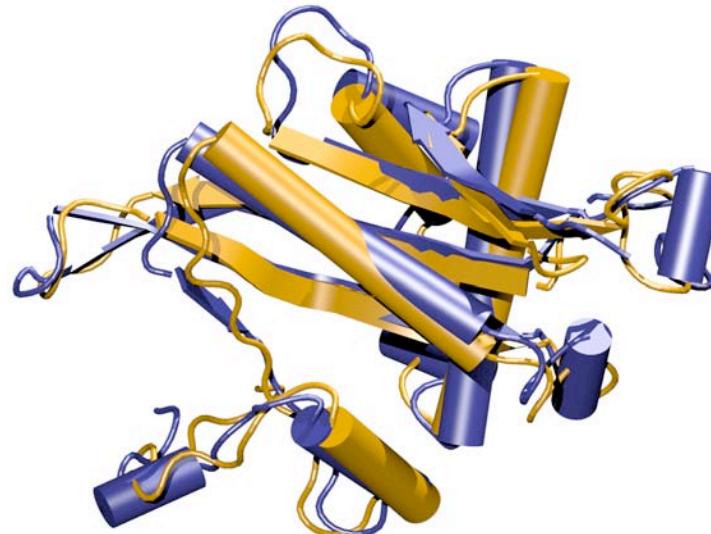
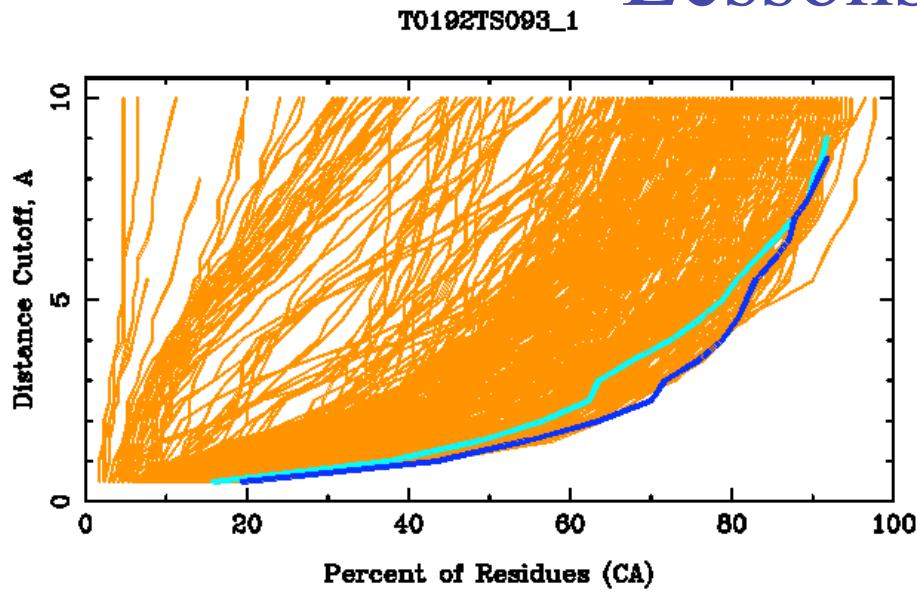
2. Sequence – Structure Profile Alignments

Clustal, Hidden Markov (HMMER, PSSM)
with position dependent gap penalties

*R. Goldstein, Z. Luthey-Schulten, P. Wolynes (1992, PNAS), K. Koretke et.al. (1996, Proteins)

CM/Fold Recognition Results from CASP5

Lessons Learned



The prediction is never better than the scaffold.

Threading Energy Function and Profiles need improvement.

Structural Profiles

1. Structure more conserved than sequences!!! Similar structures at the Family and Superfamily levels.
Add more structural information
2. Which structures and sequences to include? Evolution, QR redundancy

Structural Domains

Structural Classification of Proteins



Protein: Aspartyl-tRNA synthetase (AspRS) from *Escherichia coli*

Lineage:

1. Root: [scop](#)
2. Class: [All beta proteins](#)
3. Fold: [OB-fold](#)
barrel, closed or partly opened n=5, S=10 or S=8; greek-key
4. Superfamily: [Nucleic acid-binding proteins](#)
5. Family: [Anticodon-binding domain](#)
barrel, closed; n=5, S=10
6. Protein: Aspartyl-tRNA synthetase (AspRS)
this is N-terminal domain in prokaryotic enzymes and the first "visible" domain in eukaryotic enzymes
7. Species: [Escherichia coli](#)

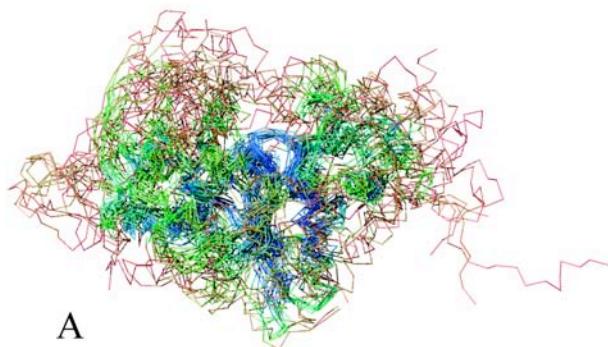
PDB Entry Domains:

1. [1c0a](#)
1. [region a:1-106](#)
2. [1i12](#)
complexed with 1mg, 5mc, 5mu, amo, h2u, psu, so4
 1. [region a:1-106](#)
 2. [region b:1001-1106](#)
3. [1eqr](#)
complexed with mg
 1. [region a:1-106](#)
 2. [region b:1-106](#)
 3. [region c:1-106](#)

Profile - Multiple Structural Alignments

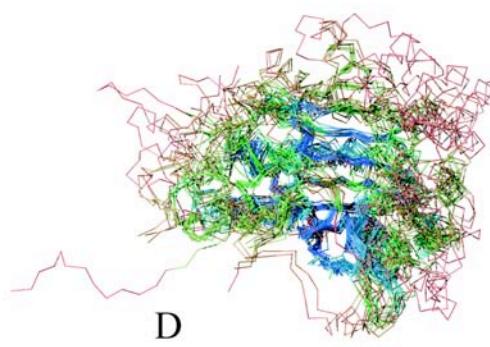
Representative Profile of AARS Family

Class I

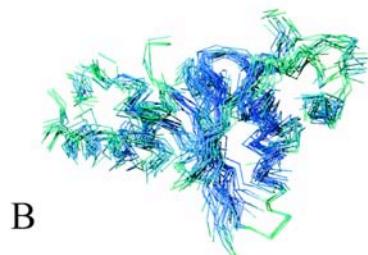


A

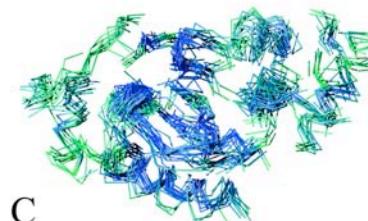
Class II



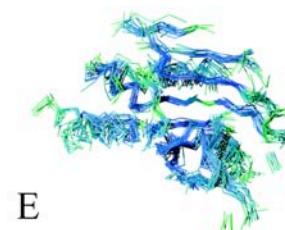
D



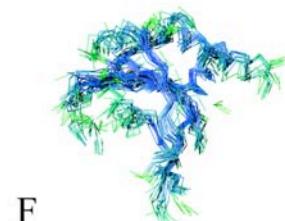
B



C



E



F

STAMP - Multiple Structural Alignments

1. Initial Alignment Inputs

- Multiple Sequence alignment
- Ridged Body “Scan”

2. Refine Initial Alignment & Produce Multiple Structural Alignment

$$P_{ij} = \left\{ e^{-d_{ij}^2/2E_1} \right\} \left\{ e^{-s_{ij}^2/2E_2} \right\}$$

probability that residue i on structure A is equivalent to residue j on structure B.

d_{ij} -- distance between i & j

s_{ij} -- conformational similarity; function of rms bewteen i-1, i, i+1 and j-1, j, j+1.

- Dynamic Programming (Smith-Waterman) through P matrix gives optimal set of equivalent residues.
- This set is used to re-superpose the two chains. Then iterate until alignment score is unchanged.
- This procedure is performed for all pairs.

Multiple Structural Alignments

STAMP – cont'd

2. Refine Initial Alignment & Produce Multiple Structural Alignment

Alignment score:

$$S_C = \frac{S_p}{L_p} \frac{L_p - i_A}{L_A} \frac{L_p - i_B}{L_B}$$

$$S_p = \sum_{aln.\ path} P_{ij}$$

L_p, L_A, L_B -- length of alignment, sequence A, sequence B

i_A, i_B -- length of gaps in A and B.

Multiple Alignment:

- Create a dendrogram using the alignment score.
- Successively align groups of proteins (from branch tips to root).
- When 2 or more sequences are in a group,
then average coordinates are used.

Variation in Secondary Structure STAMP Output



Stamp Output/Clustal Format

SerRS-T_thermophilus	VGGEEANREIKR VGGPPEFSFP--P--LDHVALMEKNGWWEPRISQVSGSRSYALKGDLA
ThrRS-E_coli	-----R--DHRKIGKQLDLY-HMQ-EE-APGMVFWHNDGW
ProRS-T_thermophilus	-----KGLTPQSQDFSEWYLEVIQKAELAD-YG--P-VRGTIVVRPYGY
ProRS-M_thermoautotrophicus	-----EFSEWFHNILEEAEIIDQRY--P-VKGMHVWMPHGF
space	-----
SerRS-T_thermophilus	--SGGG-EEEEEES----SS-----HHHHHHHHHT-B-TTHHHHH-SS---B-THHH
ThrRS-E_coli	-----HHHHHHHHHTT-E-E---TT-STT--EE-HHHH
ProRS-T_thermophilus	-----HHHHHHHHHHHHHHHHHTTSEE-E---S-STT-EEE-HHHH
ProRS-M_thermoautotrophicus	-----HHHHHHHHHHHHHTT-EE----S-STT--EE-HHHH
SerRS-T_thermophilus	LYELALLRFAMDFMARRGFLPMTLPSYAREK-AFLG-TGHFPAYRDQVWAIA-----E--
ThrRS-E_coli	TIFRELEV FVRSKLKEYQYQEVKGPFMMDRV-LWEKT-GHWDNYKDAMFTTS---S-EN
ProRS-T_thermophilus	AIWENIQVQLDRMFKETGHQNAFPLFIPMSFL-----FSPELAVVTHAGGELE
ProRS-M_thermoautotrophicus	MIRKNTLKILRRILD-RDHEEVLFPLLVPED-E-LAKEAIHVKGFEDEVYVWVTHGGLSKLQ
space	-----
SerRS-T_thermophilus	HHHHHHHHHHHHHHHTT-EEEE--SEEEHH-HHHH-HT-TTTGGGS-B-T----T--
ThrRS-E_coli	HHHHHHHHHHHHHHHTT-EE---SEEEHH-HHHTT-THHHHGGG--EEE---E-TT
ProRS-T_thermophilus	HHHHHHHHHHHHHHHTT-EE---SEESTT-----TT--EEEE-SSSEEE
ProRS-M_thermoautotrophicus	HHHHHHHHHHHHHTT-TT-EE---SEEEHHH-HTTSHHHHHHTTTT--EEEEETTEEEE
SerRS-T_thermophilus	TDLYLTGTAEVVLNALHSGEILPYEALPLRYAGYAPAFRSEA--GSFGKDVRLMRVH-Q
ThrRS-E_coli	REYC I KPMNC PGHVQ IFNQ GLKS YRDL P L RMAE FG SCHR--NEPS--G-S LHGL MRV R-G
ProRS-T_thermophilus	EPLA VRPT SET VIGYMWSK WIRS WRDL P QLLN QWG NVVRW--E---M-RTRPFLRTSE-
ProRS-M_thermoautotrophicus	RKLALRPTSETV MYP MFAL WVR SHT DLP MRFY QVV NTF RY-ET---K-HTRPL IRV REI
space	-----
SerRS-T_thermophilus	SSEEE-S-T HHHHHHHHTT-EEEGGG-SEEEEEEEEEE-----S-SSTTTTTTS-S-E
ThrRS-E_coli	EEEEEE-S-S HHHHHHHHTS--BTTT-SEEEEEE--EEE-----G-G-G-BTTTB-S-E
ProRS-T_thermophilus	EEEEEE-S-S HHHHHHHHHHHH--BGGG-EEEEEEEEE-----S-S-BTTTB-SE-
ProRS-M_thermoautotrophicus	EEEEEE-S S HHHHHHHHHHHH--BTTT-EEEEEEEEE-----S-BTTTB-SEE

From multiple structure alignment compute position probabilities for amino acids and gaps!!!!

PSSM-based approach

I. Construction of Profile

	1	2	3	4	5
Sequence 1	-	B	B	-	C
Sequence 2	C	C	-	-	C
Sequence 3	C	B	C	C	B

Multiple Sequence Alignment



Position Specific Amino Acid Probabilities

j	1	2	3	4	5
P(C ^j)	1	0.33	0.5	1	0.67
P(B ^j)	0	0.67	0.5	0	0.33

Position specific score for aligning i^{th} residue of S to j^{th} position of profile

$$Sc(S_i^j) = \log(P(S_i^j)/P(S_i^{rnd}))$$

II Database search

Align every sequence in the database to the profile using Dynamic Programming algorithm.

Sequence represented by $S(S_1, S_2, \dots, S_{n_{res}})$

Progressive alignment score = $H(i,j)$

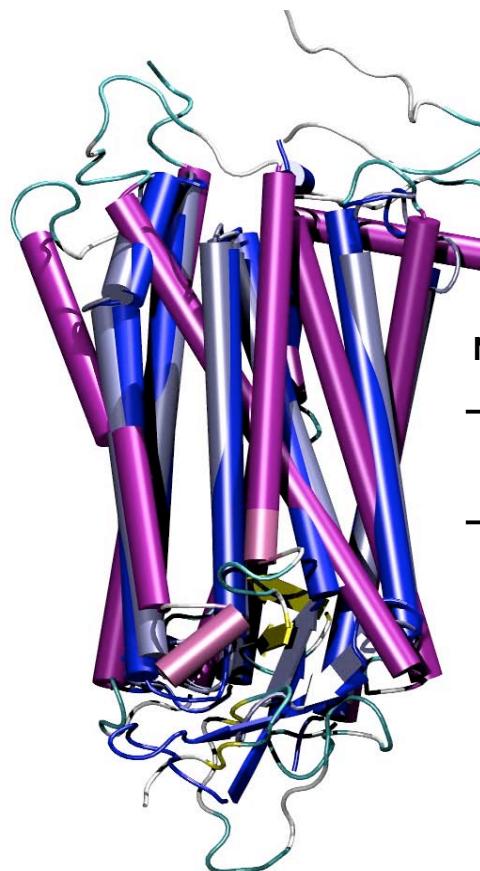
$$H(0,0) = 0, H(i,0) = i \times \delta, H(0,j) = j \times \delta.$$

$$H(i,j) = \max \begin{cases} H(i-1, j-1) + Sc(S_i^j) \\ H(i-1, j) + \delta \\ H(i, j-1) + \delta \end{cases}$$

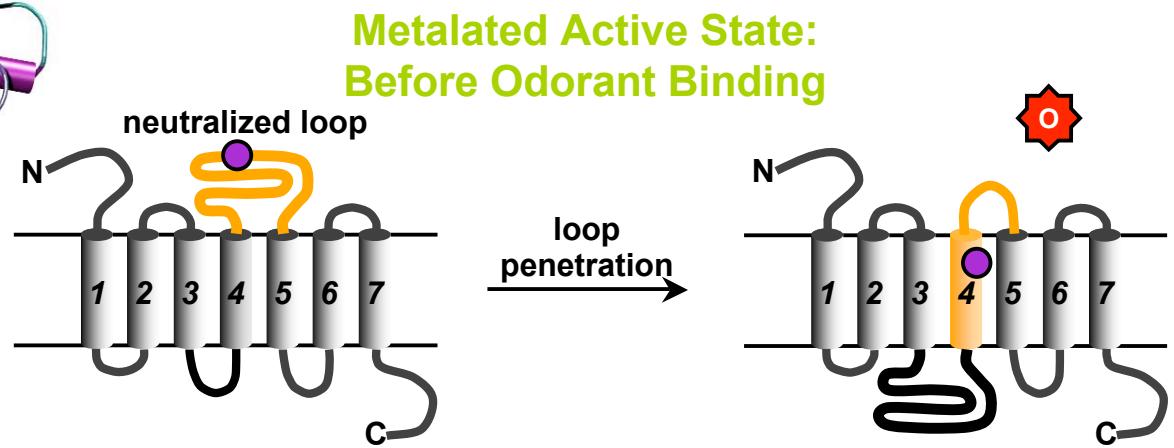
for $j=1,2,\dots,m_{aln}$ and $i=1,2,\dots,N_{res}$

Traceback gives the optimal alignment of the sequence S to profile.

Hidden Markov Models of Transmembrane Proteins



Bacteriorhodopsin/Rhodopsins



Olfactory Receptor/Bovine Rhodopsin

J. Wang, Z. Luthey-Schulten, K. Suslick (2003) *PNAS* **100**(6):3035-9

Stamp Profile

d1l9ha_3	MNGTEGPNFYVPPSNKTGVVRSPFEAPQYYLAEPWQFSMLAAYMFEL	GFP	UNFLTLYVTVQH																
d1e12a	-----R-ENALLS	SLW	NVALAG																
d1jgja_1	-----MVGL	LFW	GA	G	GT	TLAFA	AGR	D	AG										
d1l9ha_3	KKLRTPLNYIL	NLA	SADLFM	FG	X	TTTLYTSLHG	YFV	-F	-----	GPTGCNL									
d1e12a	PG	---	RPRPLINGATE	WIPLES	I	SSYLG	L	---	S	-G	TVGMD	EMPAGHALA	EMVR	--SQWG					
d1jgja_1	S	---	GERRY	STL	GISG	AA	V	YAV	A	---	L	--G	GWVP	-----	E	RT	--VFVP		
d1l9ha_3	EGFFATTCGGE	A	W-SL	-	LA	TERY	YVV	VCKPMSNFR	FGENHA	M	G	FTWV	WA	CA	APPLVGW				
d1e12a	RY	TWAL	TP	-I	LA	-LG	LL	-A	-----	D	-----	D	GS	FTVIAAD	E	C	TG	--LA	
d1jgja_1	RY	DWIL	TP	-I	YF	-LG	LL	-A	-----	G	-----	G	DSREF	IIVIT	NTV	U	M	AG	--FA
d1l9ha_3	SRYIPEGMQCSCGIDYY	-	PHEETNNE	FVIYM	FVVH	I	PLIV	FF-CY	-	QLVFTVKE	AAAAT								
d1e12a	A	-----	M	--TT	AL	--	FR	NA	F	SCA	-FP	Y	LSALVTDW	-ASA	S	-----			
d1jgja_1	A	-----	M	--VP	-----	ER	AL	Y	NGAV	-A	FIG	Y	YLVGPM	-TESA	S	-----			
d1l9ha_3	TQKAEEKETR	EV	VI	V	AF	ICMLP	AGVAF	-Y	-IFTHQG	D	-FGPIFM	I	PAF	AK-T	AVYNP				
d1e12a	--SA	--GTAE	DTL	R	LT	VVL	WLG	PIVWA	GVE	--G	--AL	Q	VGAT	WAYSVLD	FAKYV	F			
d1jgja_1	--QRSSG	K	S	-----	RLRN	LT	VVL	MA	IPF	WL	GPP	--G	--AL	I	PTVDVALIV	LD	V	KVGFD	
d1l9ha_3	V	I	Y	I	M	-	MNKQFRNCMV	TTLCCGKNPLGD	ST	--TVSK	TET	SQV	-APA	-----					
d1e12a	F	ULLR	W	AN	-----	NERT	-----	VAV	-----										
d1jgja_1	F	HALDA	AA	-----															

Clustal Profile-Profile Alignment

```

dil9ha_3      MNGTEGPNFYVPPFSNKTGVVRSPFEAPQYYLAEPWQFSMLAAYMFLLI  GFPINNLTLY
die12a      -----R-ENALLS  SWNLALAGL-LFVWAGR
dijgja_1      ---VGL-LFWLAIGMLGTLAFAGR
IAT9__BACTERIO  XA[T]TGRPEW[WL]GTALIC[GTL]C[V]

dil9ha_3      VTVQHKKLRPLNYILLNLADLFM[FG]TTLYTSLHGY[V-F
die12a      T-[R]PG---RPRLLGAT[PL]-SSYLGLL---S-GLTGMEMPAGHALA
dijgja_1      D--AGS---GERYYVTLGIGSIAA[AYA]A----L-C[GWVP]
IAT9__BACTERIO  GMG[SDP]---DA[FYAYITTEPAIAFTVYL][LLG]----[GLT]VPGF

dil9ha_3      --GPTGCNLEGGFFATLGGEAW-SL-[LAIERYVVVCKPMSNFRGENHA]MG[GFT
die12a      ENVR-SOWRY[TWAL]TP-[LLA-LG]L-A-----D-----DG[GFTV
dijgja_1      -ERT-[VPRY]DW[LTTPL]-YF-LG]L-A-----G-----DSREFIV
IAT9__BACTERIO  -GEQNP[V]VERYADVFTTPLL[LDLALLID-----ADQG[LA

dil9ha_3      WVMACAAPPVGVWSRYIPEGMQCSCGIDYY-[PHEETNNE]FVIYMFVVHFI[PLIV
die12a      I[AD]GMCVTVG-LA[A]-----M-TT[L-L]RGAFAISCA-FF[LSAL
dijgja_1      ITL[TVV]LAG-FAGA-----M-VP-[I]ER[AL]GAV-AFIG-YVYL
IAT9__BACTERIO  [ADGIM]GTG-LVGA-----LTKVYS[R]EV[LA]ISTA-AM[Y]LYVL

dil9ha_3      FF-CYG-QLVFTVKEAAAATTQKAKEKVTR[V]VIAF[C]LPIAGVAF-Y-IFTHQG
die12a      VTDL-AASA-S-----SA-GTAEFDTLRVLTVVL[LY]P[VW]AGVE-G-
dijgja_1      VGPM-TESA-S-----QRSSG[K]S[RLRNLTVVL[AI]PF[WI]GPP-G-
IAT9__BACTERIO  FFG[TSK]E-----SMRPEVASTFK[LRN]TVVL[S]P[VW]GSE-G

dil9ha_3      [D-FGP]IFMT[PAFFAK-[AVVN[P]Y-N-[NKQFRNCMVTTLCGKPNLGDST--TVS
die12a      AL[Q]VGAT[V]A[SVLDVFAKYVF[F]LLRV[AN]-----NERT-
dijgja_1      AL-[P]T[VALI]YLD[VTKVGF]G[ALDA-AA]-----
IAT9__BACTERIO  AG[VPLN]T[IL]VLDV[AKVKG]GL[LLRSRAIFG]-----EAEAP

dil9ha_3      KTETSQV-APA
die12a      -----VAV-
dijgja_1      -----
IAT9__BACTERIO  EPSADGAAATS

```

Sethi and Luthey-Schulten, 2003

Refine Structure Prediction with Modeller 6.2



Sethi and Luthey-Schulten, UIUC 2003

Modeller 6.2 A. Sali, et al.

Comparative Modeling Tools in SwissProt - SwissModel

Databases	Tools and software packages
<ul style="list-style-type: none">• Swiss-Prot and TrEMBL - Protein knowledgebase• PROSITE - Protein families and domains• SWISS-2DPAGE - Two-dimensional polyacrylamide gel electrophoresis• ENZYME - Enzyme nomenclature• SWISS-3DIMAGE - 3D images of proteins and other biological macromolecules• SWISS-MODEL Repository - Automatically generated protein models• GermOnLine - Knowledgebase on germ cell differentiation• Ashbya Genome Database• Links to many other molecular biology databases	<ul style="list-style-type: none">• Proteomics and sequence analysis tools<ul style="list-style-type: none">◦ Proteomics [Aldente (PMF)  , PeptideMass, ...]◦ DNA -> Protein [Translate]◦ Similarity searches [BLAST]◦ Pattern and profile searches [ScanProsite]◦ Post-translational modification and topology prediction◦ Primary structure analysis [ProtParam, pI/MW, ProtScale]◦ Secondary and tertiary structure prediction [SWISS-MODEL, Swiss-PdbViewer]◦ Alignment [T-COFFEE, SIM]◦ Biological text analysis• ImageMaster / Melanie - Software for 2-D PAGE analysis• MSight - Mass Spectrometry Imager• Roche Applied Science's Biochemical Pathways

Structure Prediction Resources - on line

http://cgat.ukm.my/spores/Predictory/structure_prediction.html

Fold Recognition / Secondary Structure Prediction	
WWW Servers	
3D-PSSM	A Fast, Web-based Method for Protein Fold Recognition using 1D and 3D Sequence Profiles coupled with Secondary Structure and Solvation Potential Information. Biomolecular Modelling Group, Imperial Cancer Research Fund, UK
BCM PSSP	Protein secondary structure prediction, Baylor College of Medicine, USA.
bioinbgu	Fold-recognition services based on Sequence-Derived Properties - Computer Science Dept., Ben Gurion University, Israel
CODA	A combined algorithm for predicting protein loops. CODA can predict fragments of length 3-8 using the consensus methodology. Biochemistry Dept. Cambridge, UK
CONSENSUS SECONDARY STRUCTURE	Submits input sequence to multiple servers for consensus
NNPREDICT	Protein secondary structure prediction. Dept of Cellular & Molecular Pharmacology, UCSF, USA
PREDATOR	Protein secondary structure prediction from single sequence or a set of sequences, EMBL-Heidelberg, Germany
Pred2ary	Secondary structure and class prediction server, Cohen Lab, Dept of Cellular & Molecular Pharmacology, UCSF, USA
PredictProtein	PredictProtein is a service for sequence analysis, and structure prediction. Mirrors - America, Asia, Australia, Europe
PROF	B. Rost : PROFfile based neural network prediction
PROF	R.D. King : Cascaded multiple classifiers for protein secondary structure prediction. - Neural Networks - Bayesian classifiers - Linear discrimination - Quadratic discrimination, Computational Biology Group, Univ. of Wales, Aberystwyth, UK.
PSCAN	A combined sequence structure profile fold recognition method - alignment of 2 sequences.
PSI Pred /Gen Threader	Protein structure prediction server (V2.0) using PSIPRED - a highly accurate secondary structure prediction method, GenTHREADER - a new sequence profile based fold recognition method & MEMSAT2 - a widely used transmembrane topology prediction method, David Jones et al, Brunel Univ. UK
RPFOLD	This is a simple method based on amino acid properties.
SAM-T99/T98	Hidden Markov Models applications, Computational Biology, UCSC, USA
SAWTED	SAWTED stands for Structure Assignment With Text Description. It is a method to improve the coverage of the detection of remote homologues of known structure by sequence searches (e.g. PSI-BLAST) and fold recognition programs.
ssPsi	A fold recognition/homology modelling server that uses predicted secondary structure and evolutionary information.
UCLA-DOE	Protein fold recognition by threading. UCLA-DOE, USA

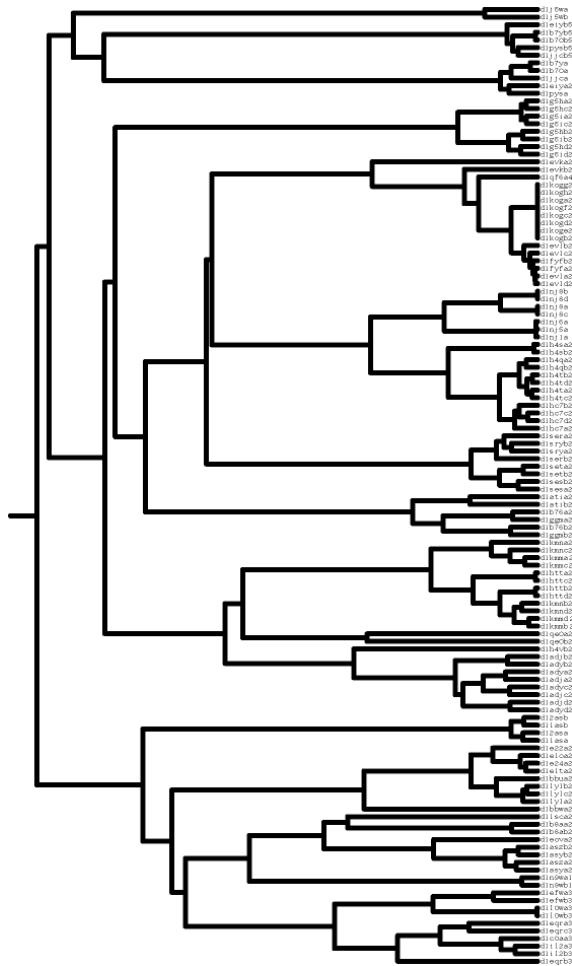
Cont'd - Web Resources

<i>Ab - Initio Methods</i>	
WWW Servers	
ELAN-PROT	Uses an elastic net combinatorial optimization to determine the lowest-energy conformation for a residue-residue energy function. This energy function incorporates information from secondary structure prediction methods, and also adds a term for any known non-local residue contacts. Side-chain detail is presently being added to the protein model. Side chains will be added to the predicted C_a trace by adding a full backbone and then using SCWRL.
Isites	Sequences are converted to sequence profiles using PSI-BLAST. Fragments of structure are predicted using the I-sites Library, which also produces a moveset for the next step. Rosetta uses the I-sites fragments to do a Monte Carlo Fragment Insertion conformational search for pieces of length 36-50. These pieces are spliced together using a genetic algorithm, to create the coordinates for the complete sequence.
PETRA	An ab-initio protein fragment prediction method, Biochemistry Dept., Cambridge, UK
Model Building	
WWW Servers	
AL2TS	Translates sequence-structure alignment into tertiary structure. PredictionCenter, Lawrence Livermore Natl. Lab.
Software / Programs	
Homology	Builds models from manual alignment and assignment of SCRs, loops and side chains (rotamers).
MODELLER	MODELLER-4: Homology protein structure modelling by satisfaction of spatial restraints, Andrej Sali Lab, Rockefeller University, USA.

Non-redundant Representative Sets of Structures

Too much information

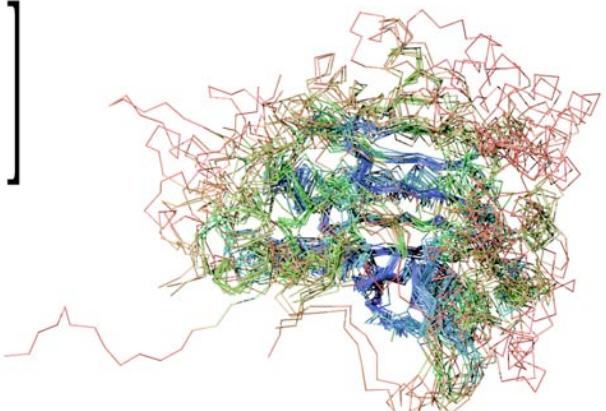
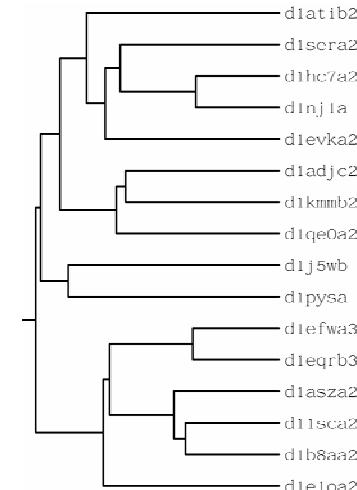
129 Structures



Multidimensional QR factorization of alignment matrix, A .

$$A = \left[\begin{array}{c} d=4 \\ G \\ Z \\ Y \\ X \\ l_{aln} \\ k_{proteins} \end{array} \right]$$

Economy of information 16 representatives



P. O'Donoghue and Z. Luthey-Schulten (2003) *MMBR* **67**:550-571.

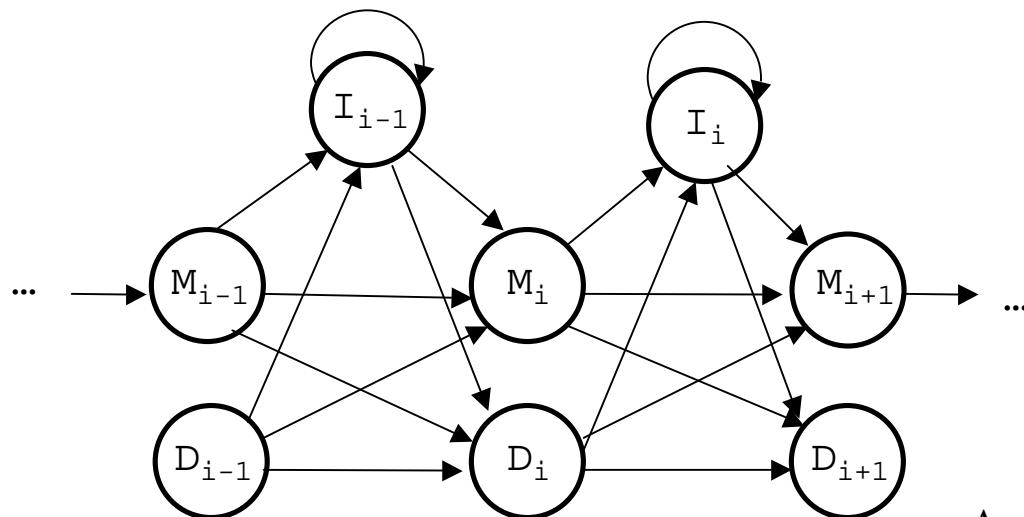
P. O'Donoghue and Z. Luthey-Schulten (2004) *J. Mol. Biol.*, in press.

HMM-based approach

	1	2	3	4	5
Sequence 1	-	B	B	-	C
Sequence 2	C	C	-	-	C
Sequence 3	C	B	C	C	B
State	M_1	M_2	M_3	I_3	M_4

State transition Probabilities (ST)

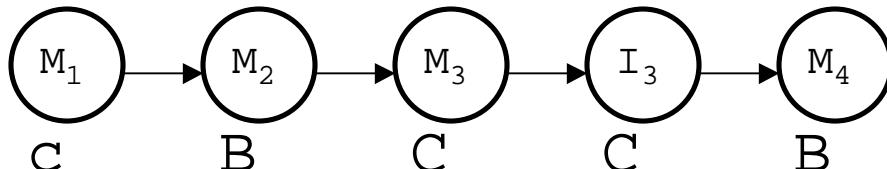
i	$M_i \rightarrow M_{i+1}$	$M_i \rightarrow D_{i+1}$	$M_i \rightarrow I_i$
1	1	0	0
2	0.67	0.33	0
3	0.5	0	0.5



Position specific amino acid Probabilities

i	$C(M_i)$	$B(M_i)$
1	1	0
2	0.33	0.67
3	0.5	0.5
4	0.67	0.33

State Path of Sequence 3



Amino acid probabilities at insert states is equal to the background probability of occurrence of the corresponding amino acid.

$$P(C|I) = 7/11 = 0.64$$

$$P(B|I) = 4/11 = 0.36$$

Leads to affine gap penalty.

$$P(-|D) = 1.$$

Generation of HMM Profile

Goal: To select right model and assign match states to selected columns in MSA.

The **model (M)** is constructed so that it generates MSA with the *highest probability*.

The **probability** of finding a **single aligned sequence A** (A_1, A_2, \dots, A_N) is:

$$P(A|\pi, M) = \prod_{i=1}^N P(A_i(\pi_i)) \quad P(\pi|M) = \prod_{i=1}^{N-1} P(\pi_i \rightarrow \pi_{i+1})$$

$$\begin{aligned} P(A, \pi|M) &= \prod_{i=0}^{N-1} P(\pi_i \rightarrow \pi_{i+1}) P(A_{i+1}(\pi_{i+1})) \\ &= P(A_{0 \rightarrow i}, \pi_{0 \rightarrow i}|M) P(A_{i+1 \rightarrow j}, \pi_{i+1 \rightarrow j}|M) P(A_{j+1 \rightarrow N}, \pi_{j+1 \rightarrow N}|M) \end{aligned}$$

The **probability** of obtaining the **MSA** from the profile is:

$$\begin{aligned} P(MSA, \pi|M) &= \prod_{k=1}^{N_{seq}} P(A^k, \pi^k|M) \quad \text{where } A^k \text{ represents the } k^{\text{th}} \text{ aligned sequence.} \\ &= \prod_{k=1}^{N_{seq}} P(A_{0 \rightarrow i}^k, \pi_{0 \rightarrow i}^k|M) \times P(A_{i+1 \rightarrow j}^k, \pi_{i+1 \rightarrow j}^k|M) \times P(A_{j+1 \rightarrow N}^k, \pi_{j+1 \rightarrow N}^k|M) \end{aligned}$$

The **profile** is constructed using dynamic programming.

$$\log P_j = \max_{0 \leq i \leq j-1} \log P_{ij} = \max_{0 \leq i \leq j-1} (\log P_i + ST_{ij} + AM_j + AI_{ij})$$

P_j = Highest probability of obtaining MSA till j^{th} column such that j is a match state.

P_{ij} = Highest probability of obtaining MSA such that j is a match state and i is the previous match state.
where ST_{ij} represents the probabilities of all state transitions.

AI_{ij} the probability of all amino acids in insert states between i^{th} and j^{th} columns.

AM_j represents the probabilities of all amino acids in j^{th} column.

HMM-based approach

New sequence aligned using dynamic programming.

$$H_j^M(i) = \log\left(\frac{aa_{M_j}(x_i)}{aa^{rnd}(x_i)}\right) + \max \begin{cases} H_{j-1}^M(i-1) + \log(ST_{M_{j-1}M_j}) \\ H_{j-1}^I(i-1) + \log(ST_{I_{j-1}M_j}) \\ H_{j-1}^D(i-1) + \log(ST_{D_{j-1}M_j}) \end{cases}$$

$$H_j^I(i) = \log\left(\frac{aa_{I_j}(x_i)}{aa^{rnd}(x_i)}\right) + \max \begin{cases} H_j^M(i-1) + \log(ST_{M_jI_j}) \\ H_j^I(i-1) + \log(ST_{I_jI_j}) \\ H_j^D(i-1) + \log(ST_{D_jI_j}) \end{cases}$$

$$H_j^D(i) = \max \begin{cases} H_{j-1}^M(i) + \log(ST_{M_{j-1}D_j}) \\ H_{j-1}^I(i) + \log(ST_{I_{j-1}D_j}) \\ H_{j-1}^D(i) + \log(ST_{D_{j-1}D_j}) \end{cases}$$



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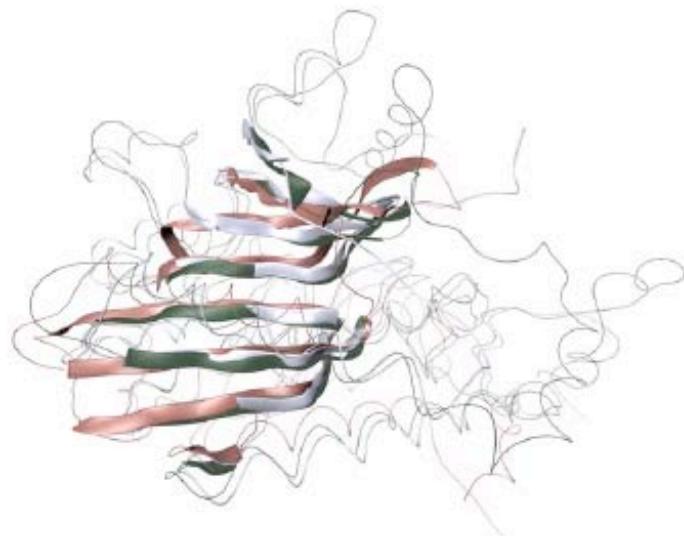
Now: or

University of Illinois at Urbana-Champaign
Luthey-Schulten Group
Theoretical and Computational Biophysics Group
Summer School 2004 - University of Western Australia, Perth

Sequence Alignment Algorithms

*Tutorial for the
material of this
lecture available at*

<http://www.ks.uiuc.edu/Training/Tutorials/>



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Zaida Luthey-Schulten

Anurag Sethi

Taras Pogorelov

June 2004