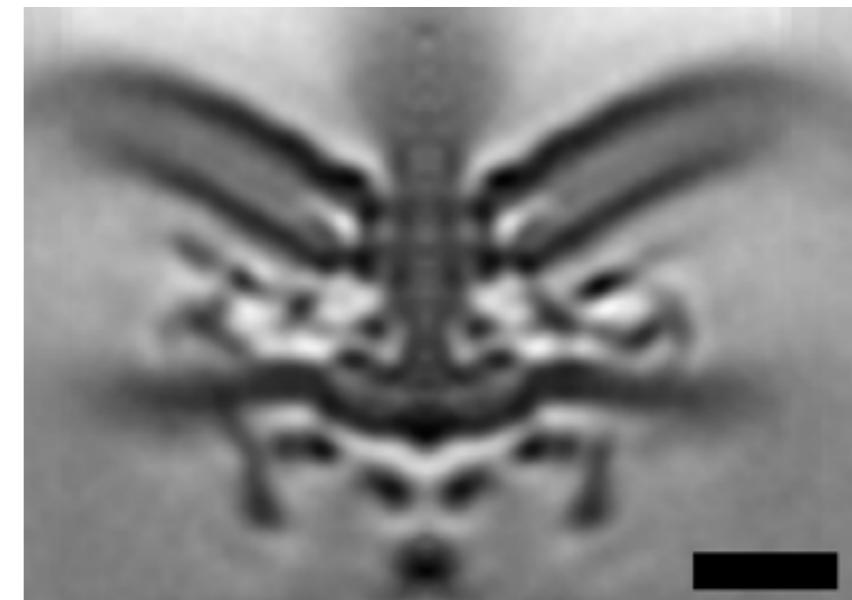
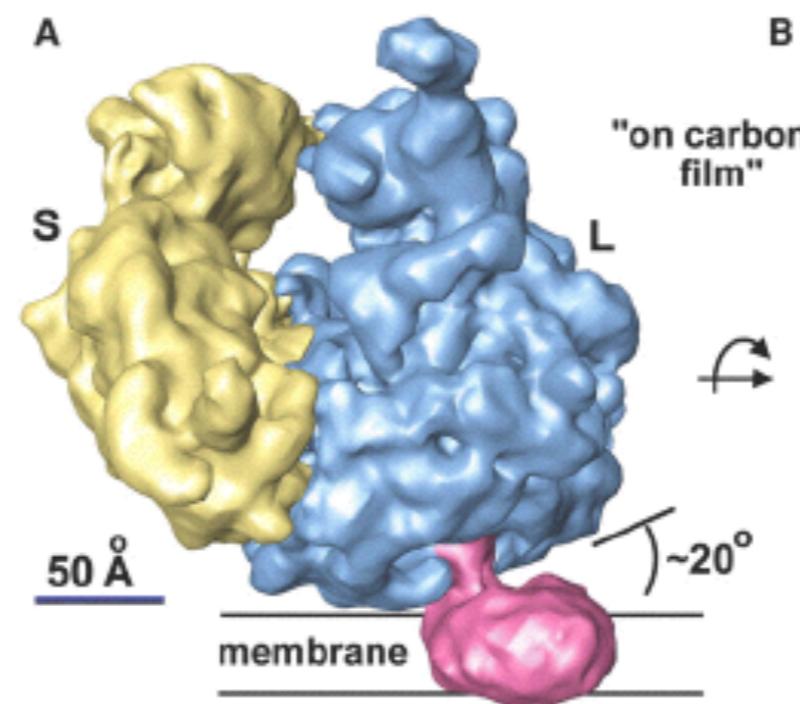
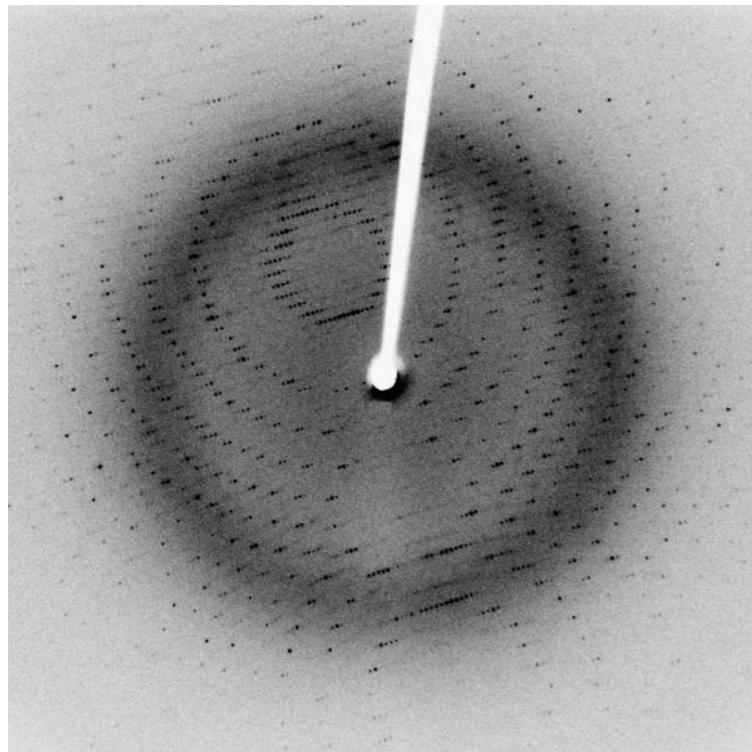
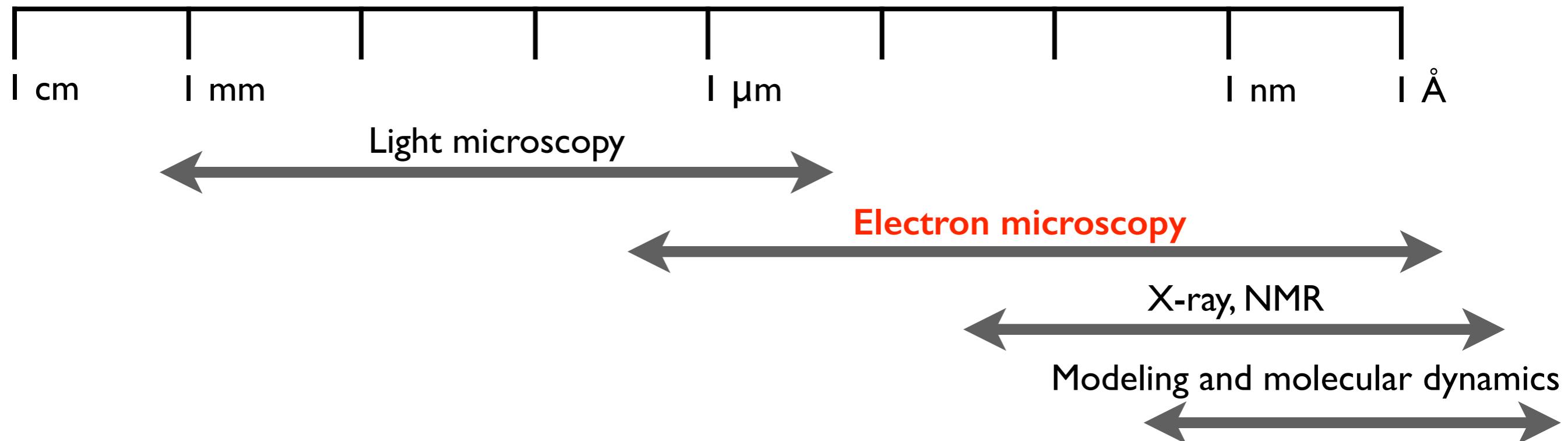
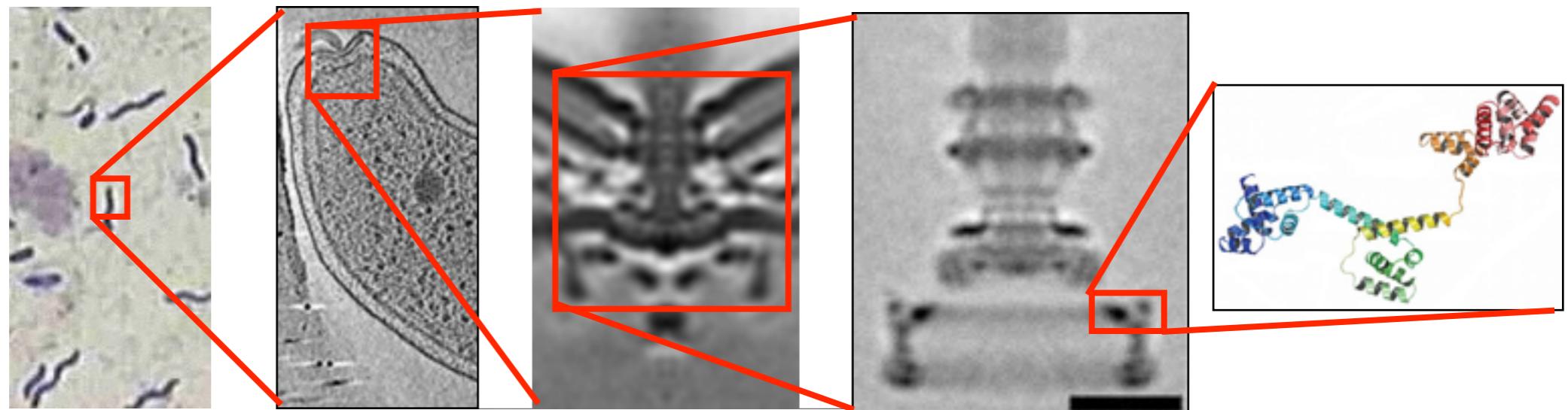


Introduction to structural biology techniques



James C. Gumbart
Georgia Institute of Technology

Structural biology continuum



resolution of the resulting image is limited by the wavelength of light used

$$d = \frac{\lambda}{2(n \sin \theta)}$$
 Abbe diffraction limit

Four radiation types

	Advantages	Disadvantages
<i>Visible light</i>	Low sample damage Easily focused Visible by eye	Long wavelengths
<i>X-rays</i>	Small wavelength (Angstroms) Good penetration	Hard to focus Damage sample
<i>Electrons</i>	Small wavelength (pm!) Can be focused	Poor penetration Damage sample
<i>Neutrons</i>	Low sample damage Small wavelength (pm)	How to produce? How to focus?

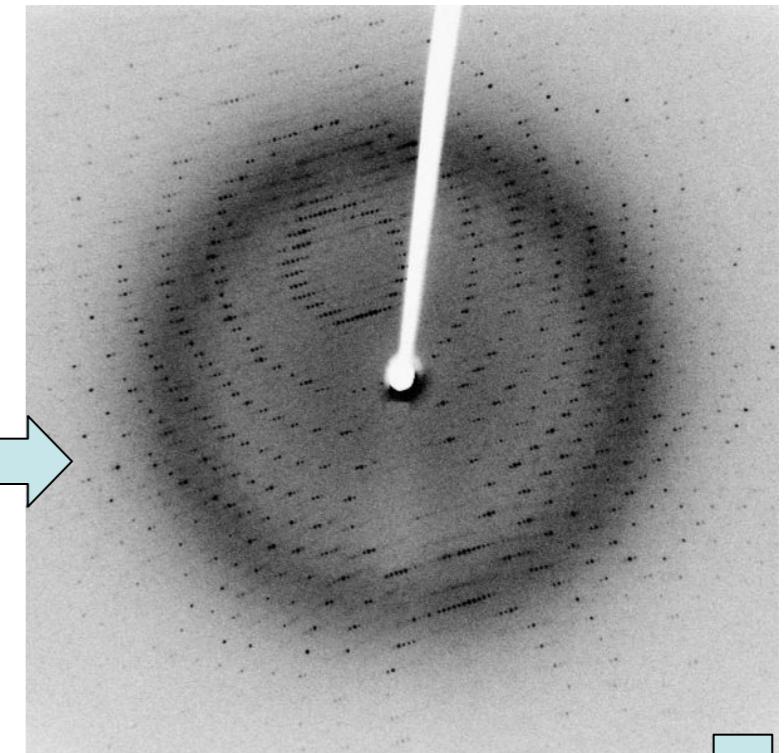
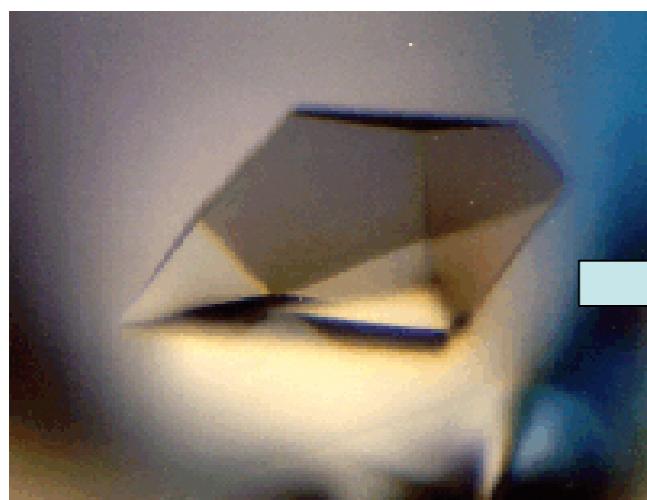


de Broglie, defends thesis in 1924, wins Nobel Prize in 1929

$$\text{de Broglie wavelength: } \lambda = -\frac{h}{p}$$

10 keV electron \rightarrow 0.01 nm wavelength

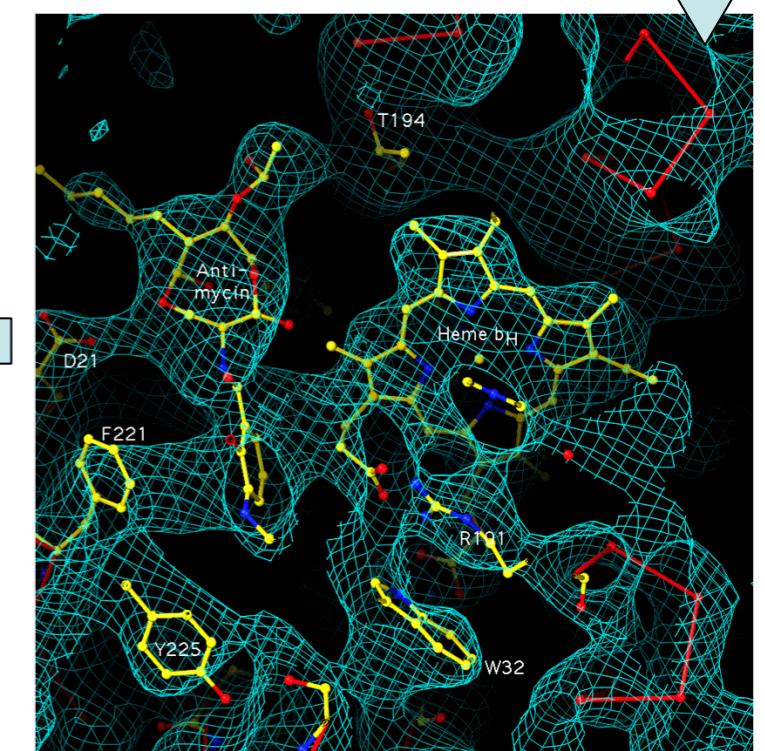
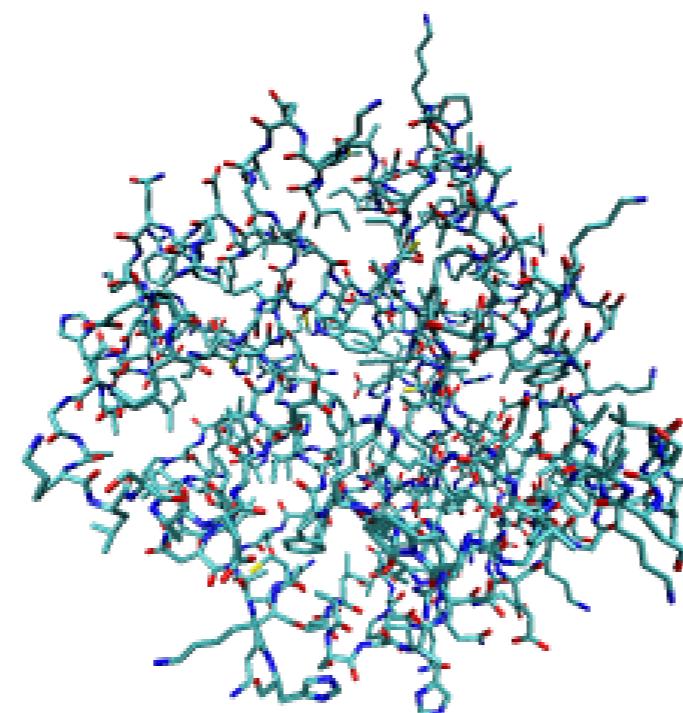
X-ray crystallography



best resolution
produced by X-rays,
which have
wavelengths on the
scale of Ångstroms

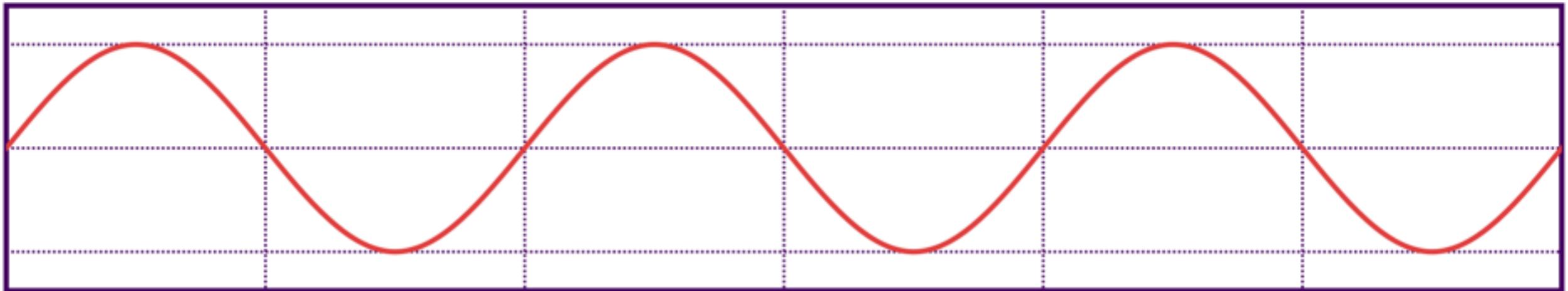
(inverse) Fourier
transform

$$f(\mathbf{r}) = \int \frac{d\mathbf{q}}{(2\pi)^3} F(\mathbf{q}) e^{i\mathbf{q}\cdot\mathbf{r}}$$

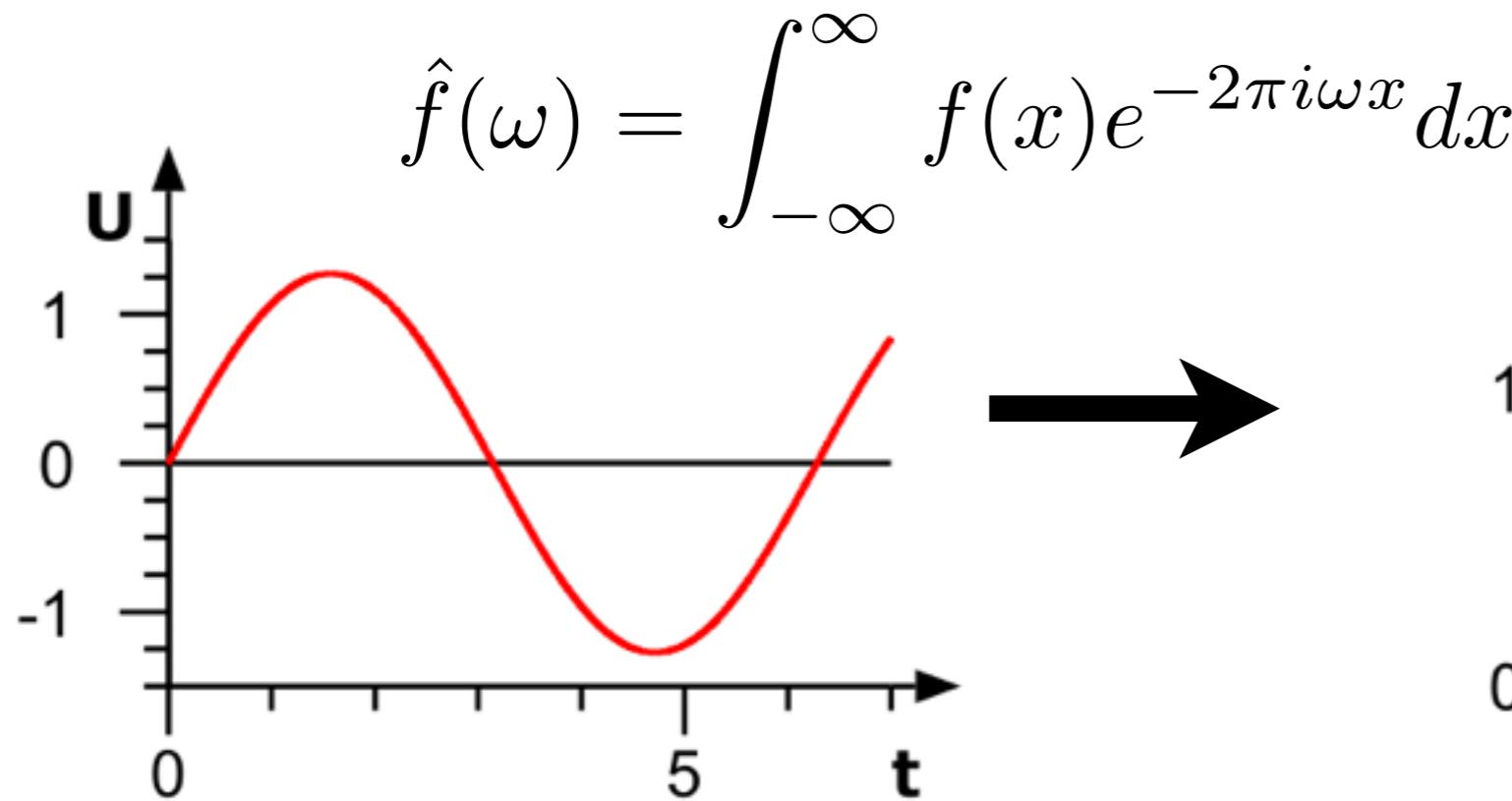


Fourier transforms

properties defining a sine wave:
amplitude, wavelength (or frequency), phase shift, and direction



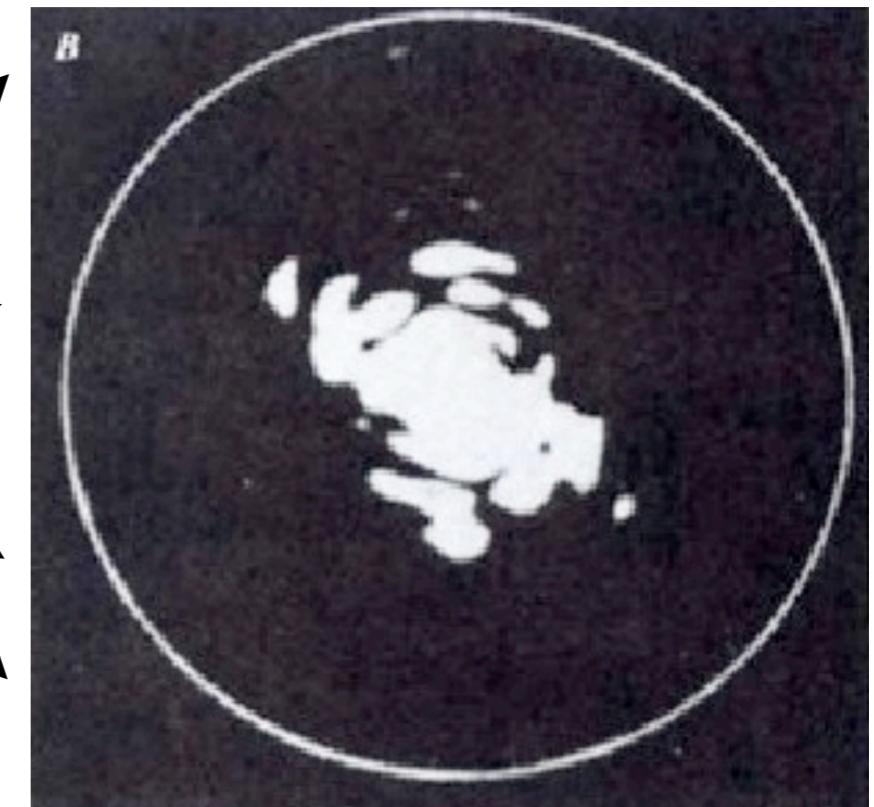
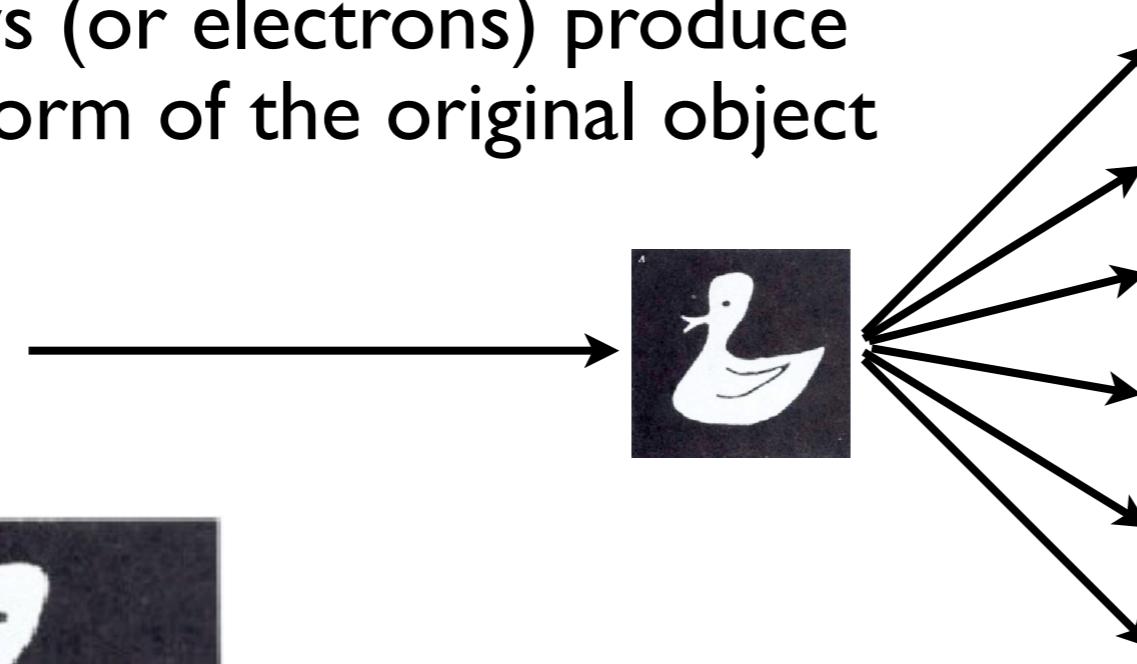
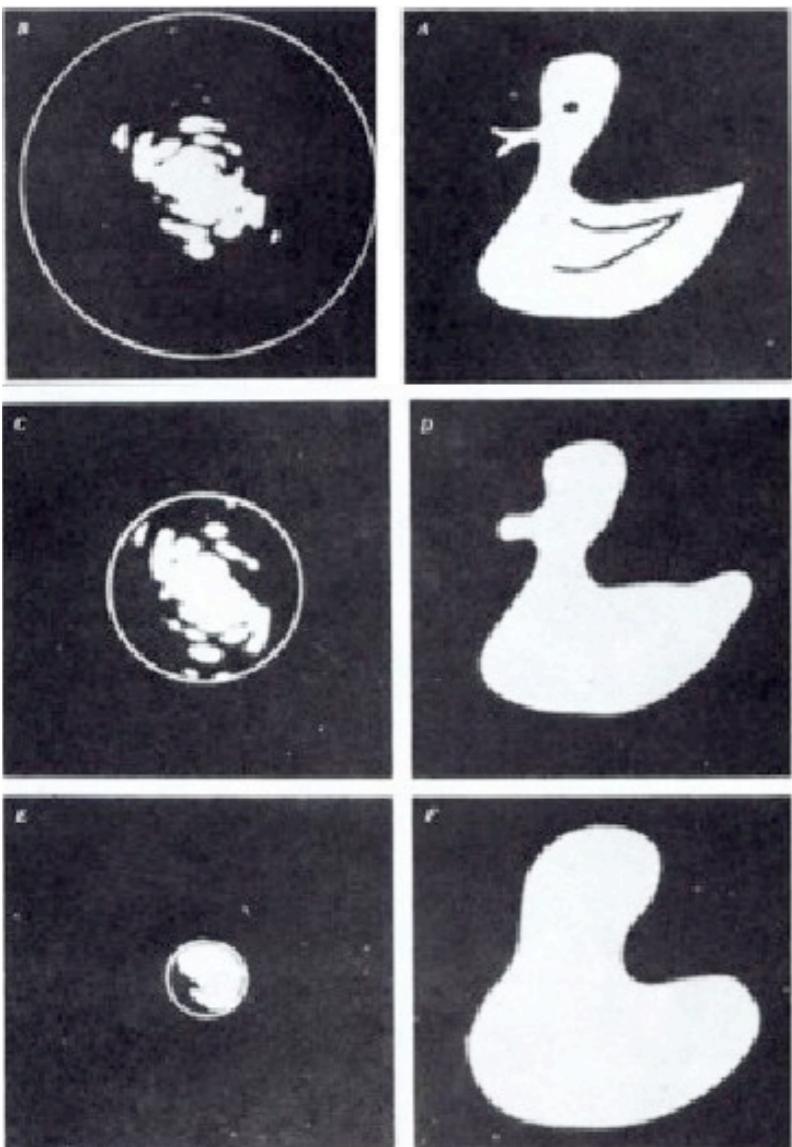
Waves can be represented in frequency (“reciprocal”) space



Phase information not depicted here to keep things simple -- but we do store it!! (as complex numbers)

diffraction patterns

diffracted X-rays (or electrons) produce a Fourier transform of the original object

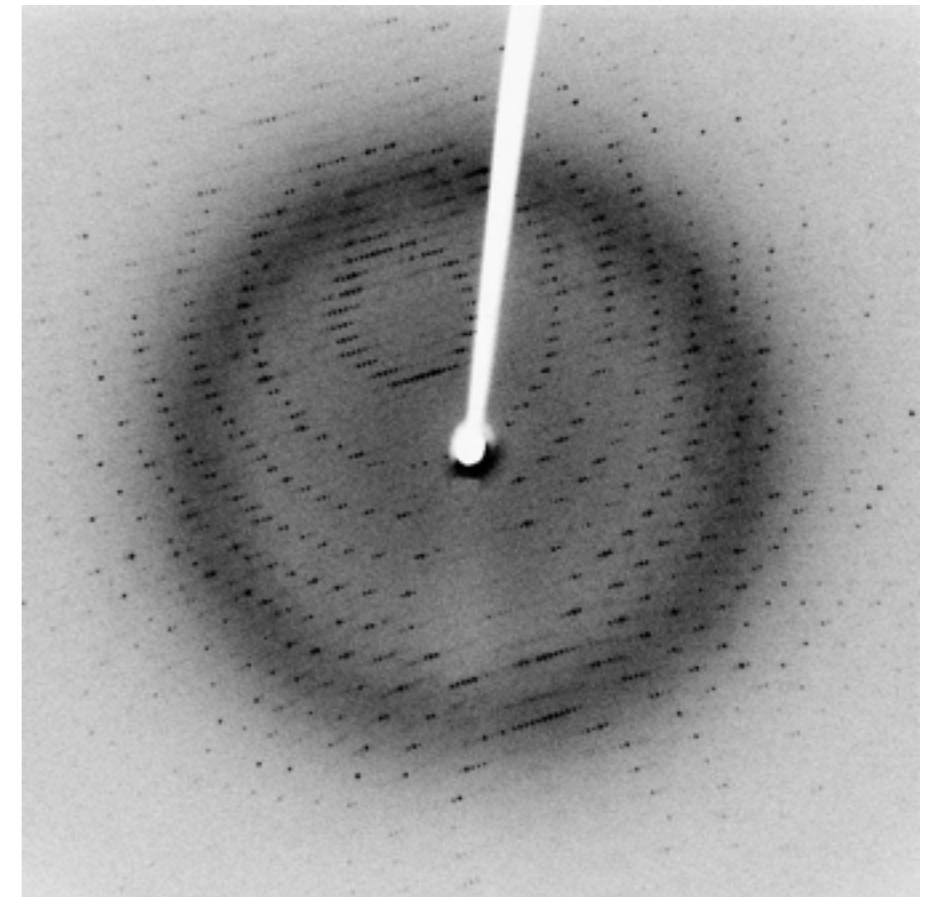
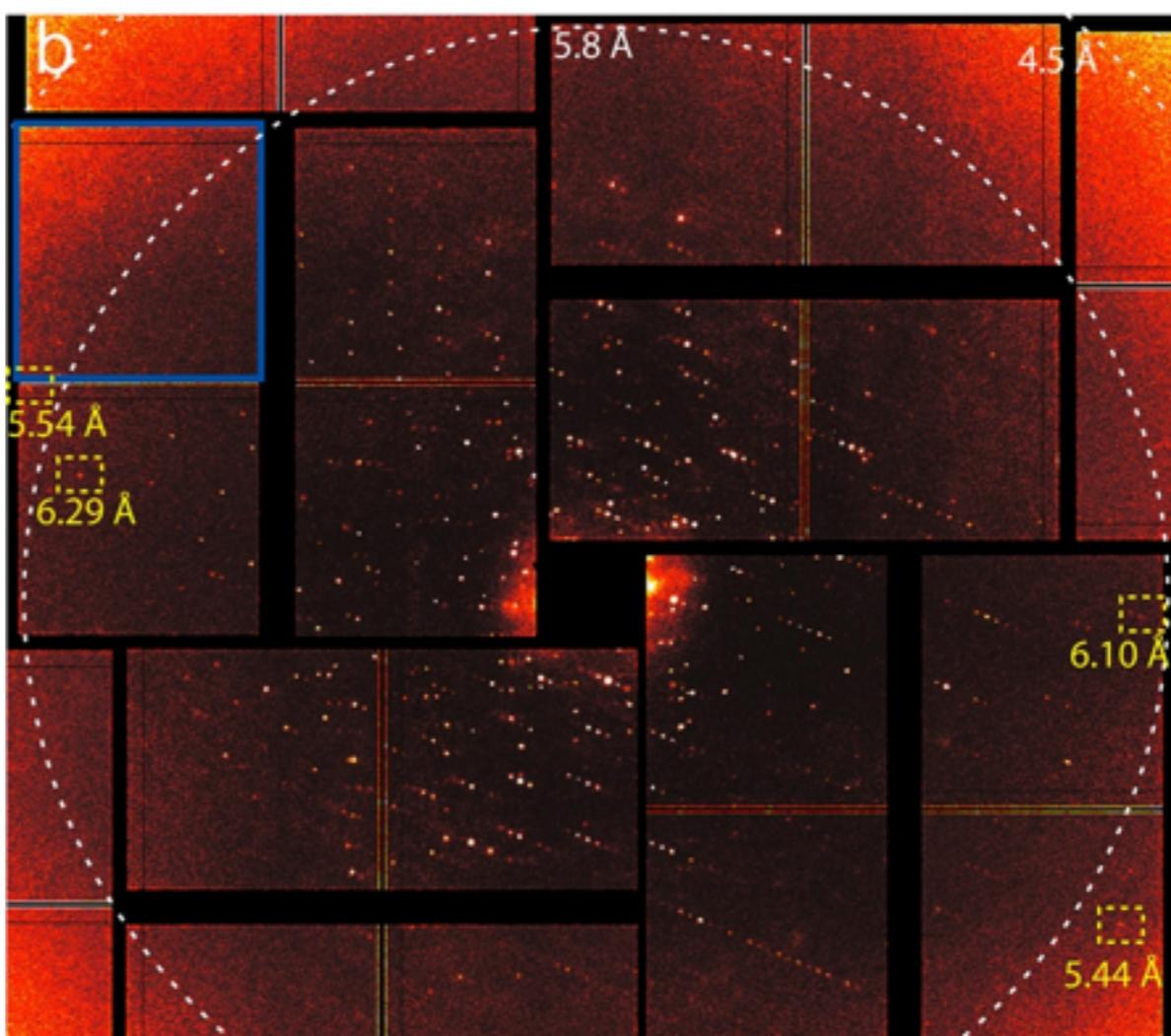
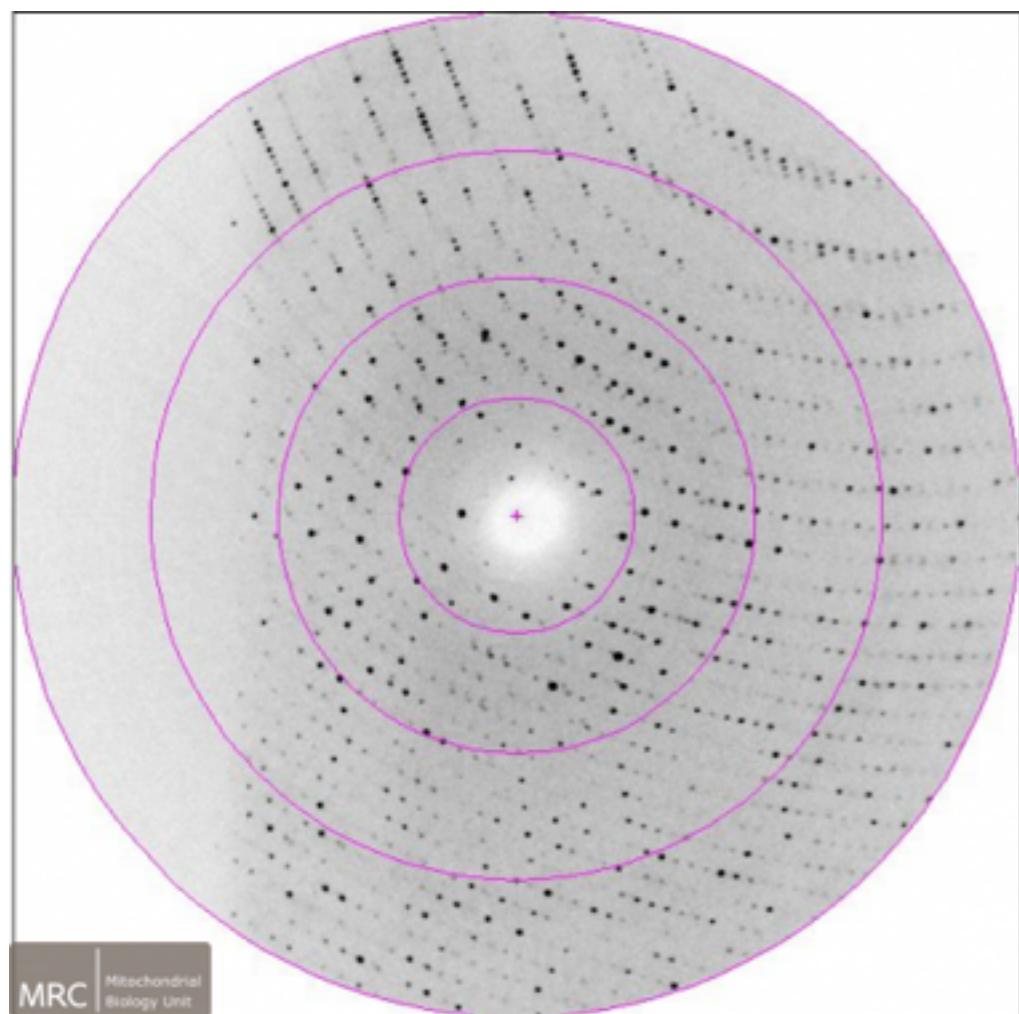


*intensity of diffracted photons
(but not phases!)*

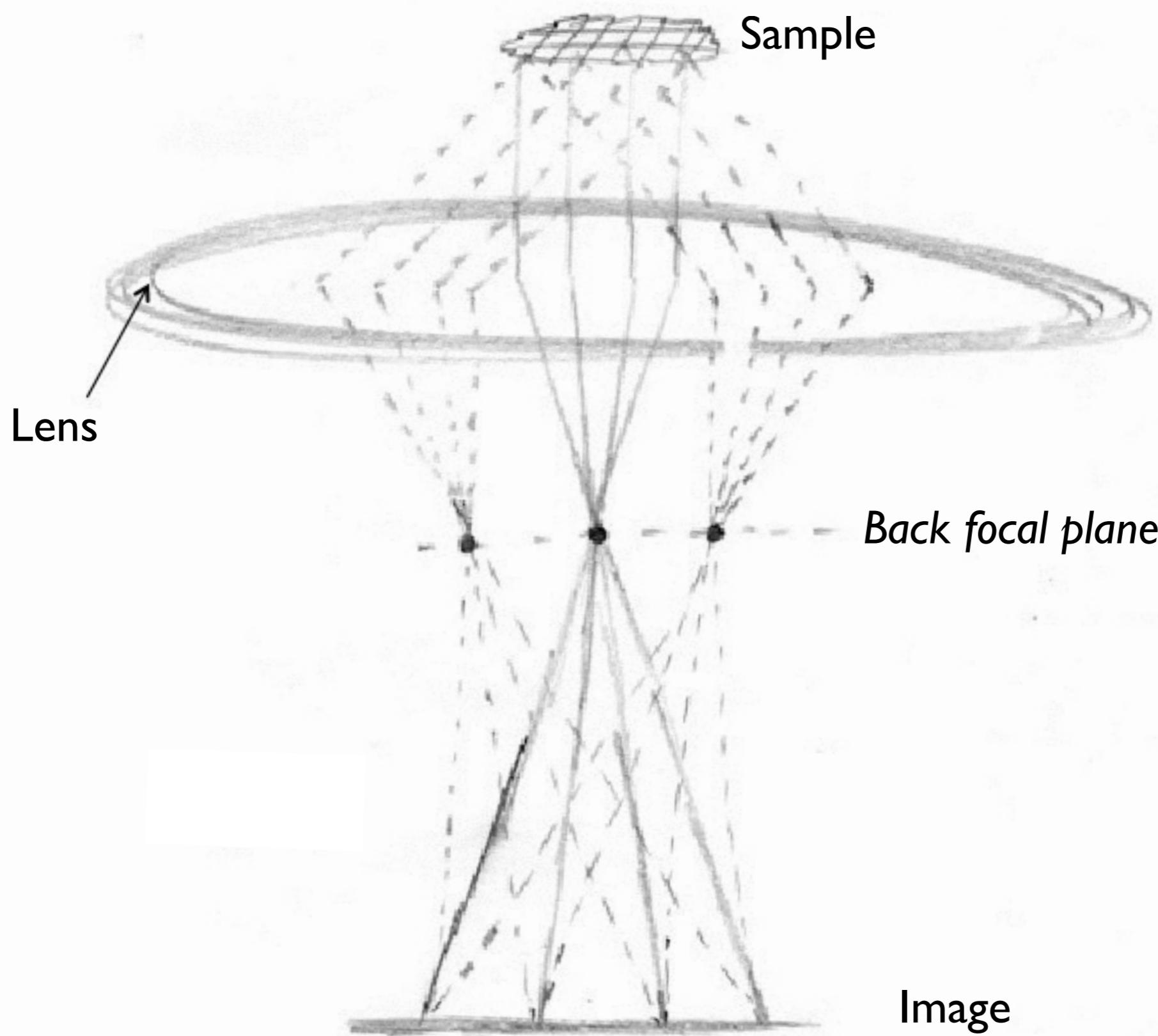
High “frequency” components contribute the details, and appear furthest from the origin

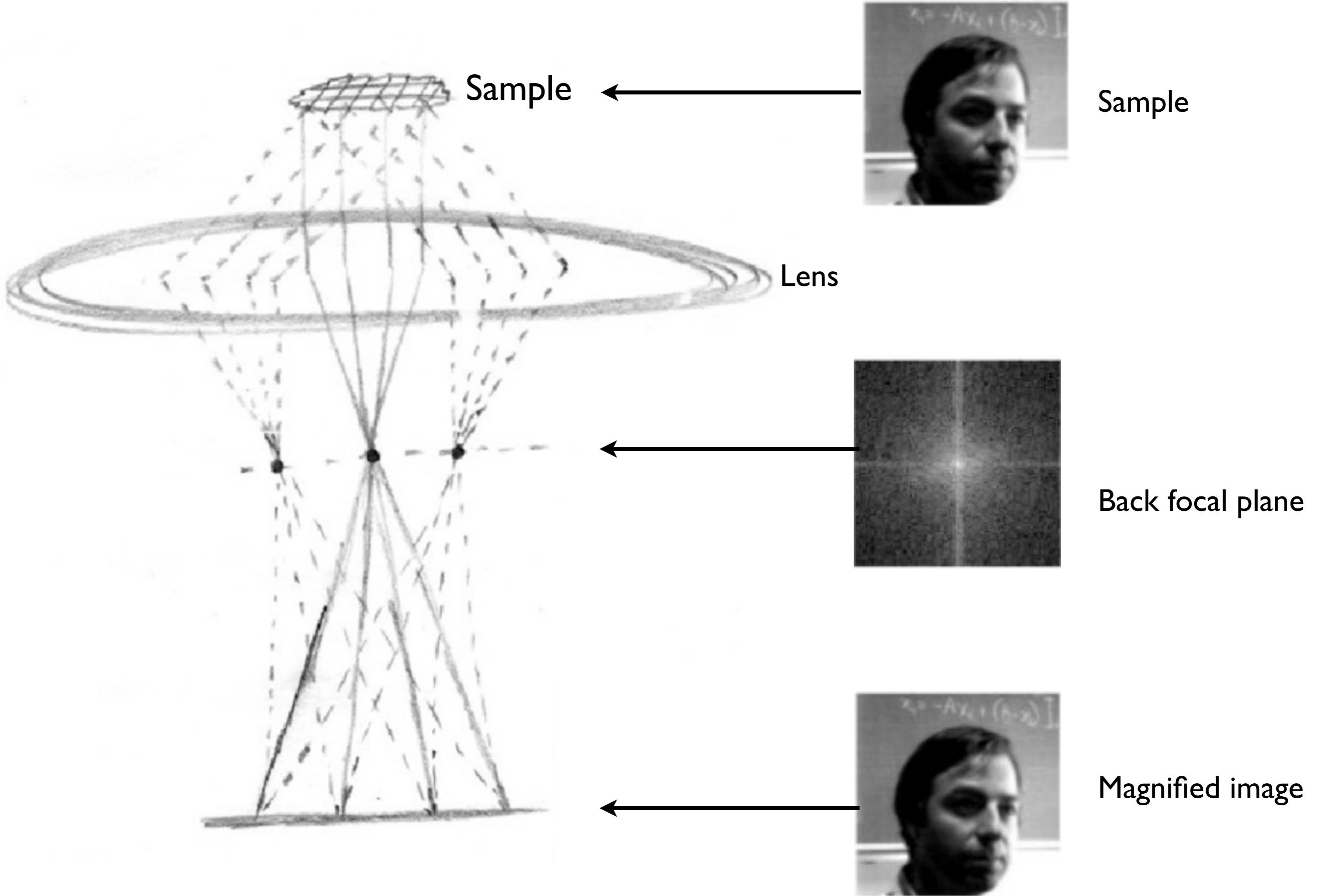
diffraction patterns

resolution determined by presence of data
far from origin

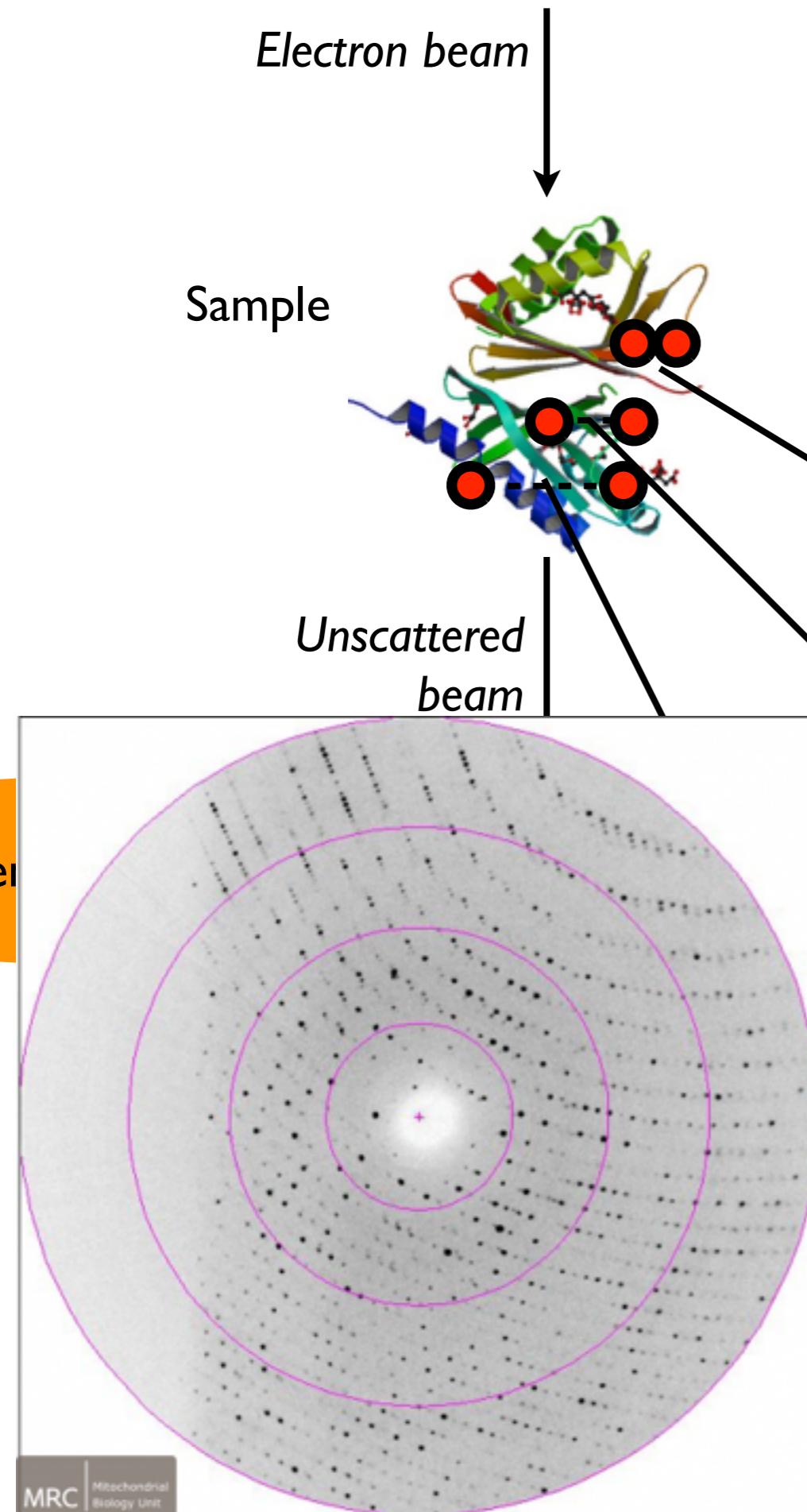


Before inverting reciprocal space back into an image, the diffraction pattern (i.e. Fourier transform) is focused at the **back focal plane**:





reconstituting the image



normally, use a lens to refocus rays onto the sensor, *but...*

there are no X-ray lenses!!!

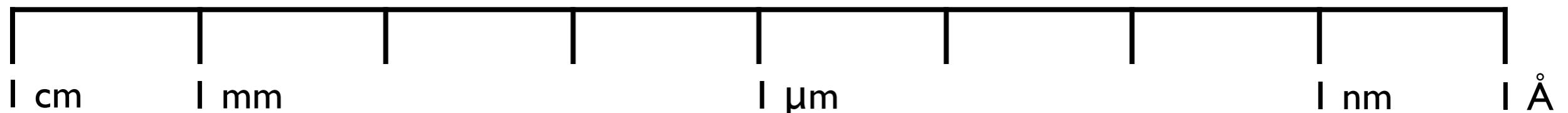
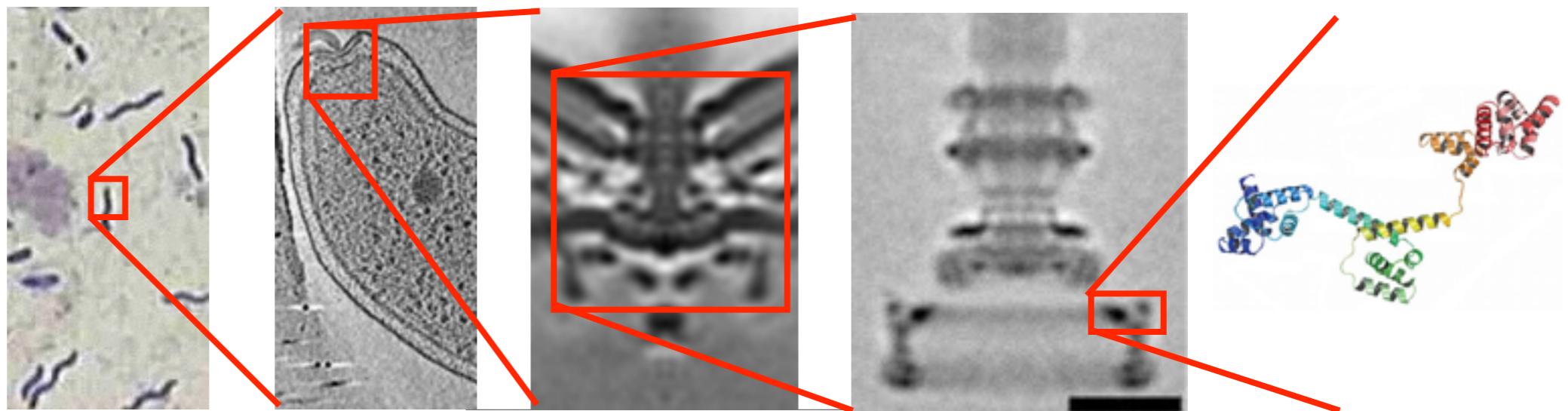
(Low spatial frequency data) \longleftrightarrow (High spatial frequency data)

i.e., diffraction = Fourier transform

so we only have the diffraction pattern,
which encodes intensities, but not phases

this is the so-called “phase problem”

Structural biology continuum



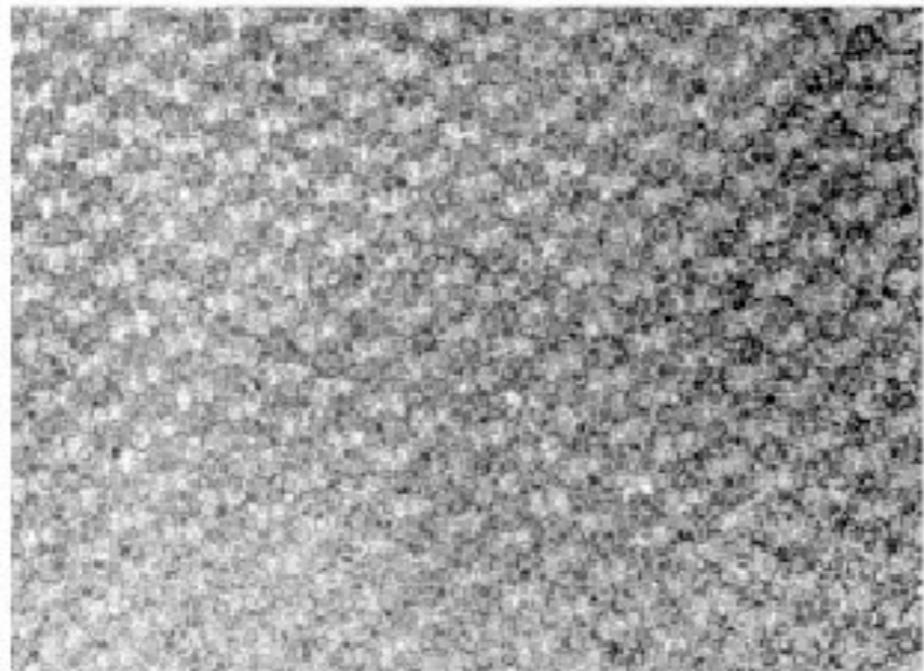
“Electron microscopy”

Electron cryo-tomography

Single particle analysis

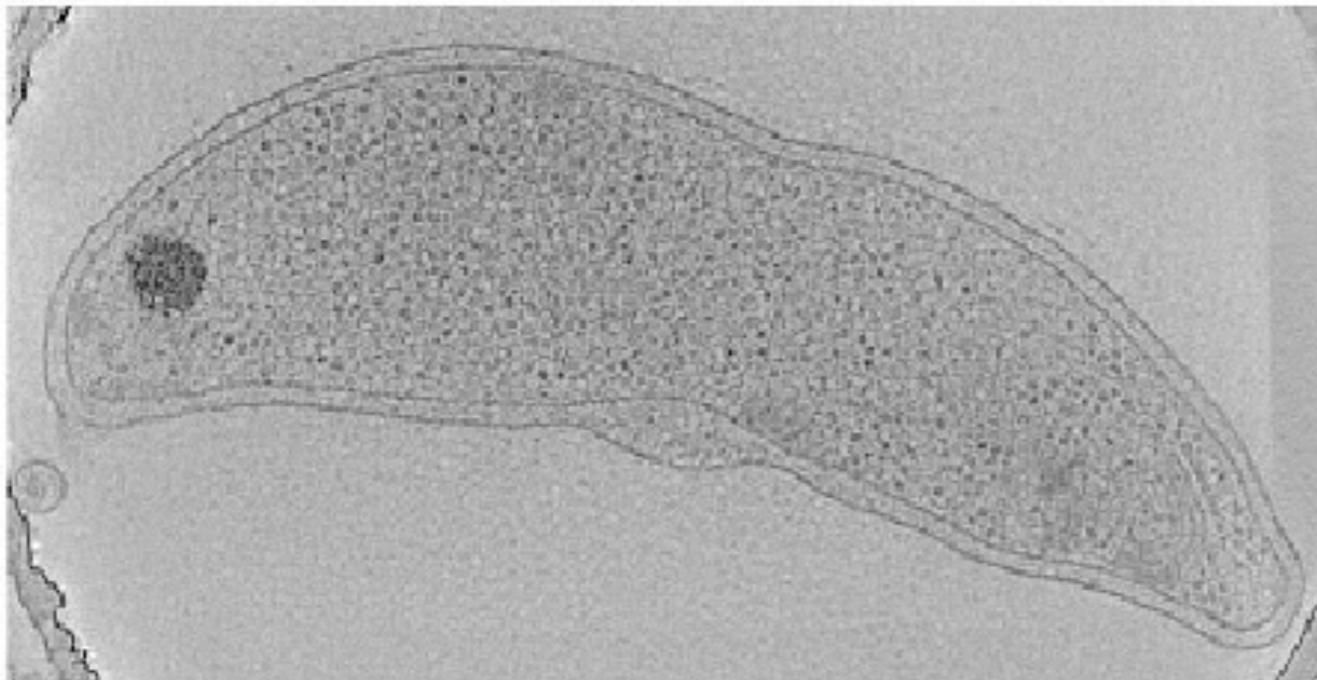
2-D Electron crystallography

Rough guide to “cryo-EM”:

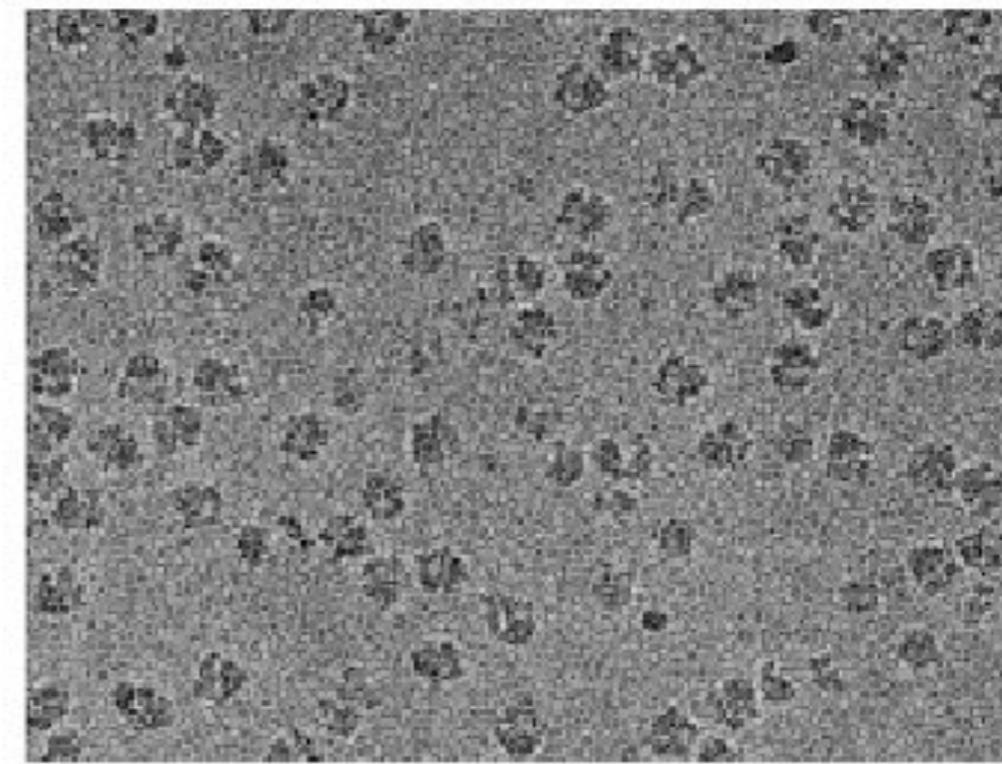


2D electron crystallography

Electron cryo-tomography

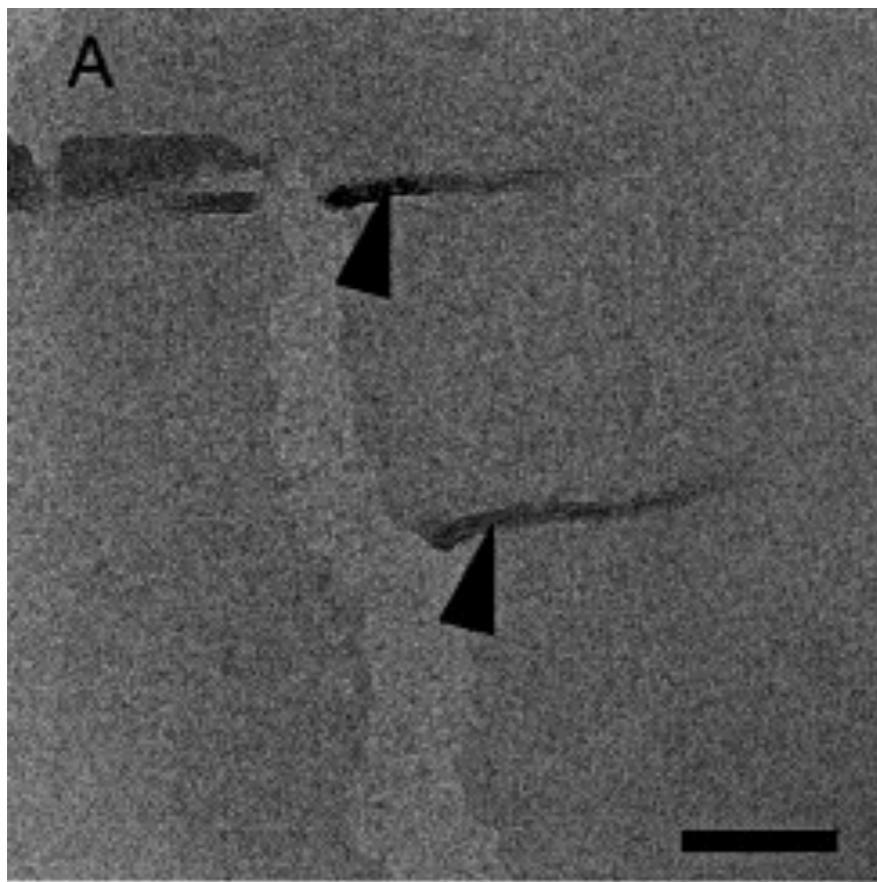


Three flavors:



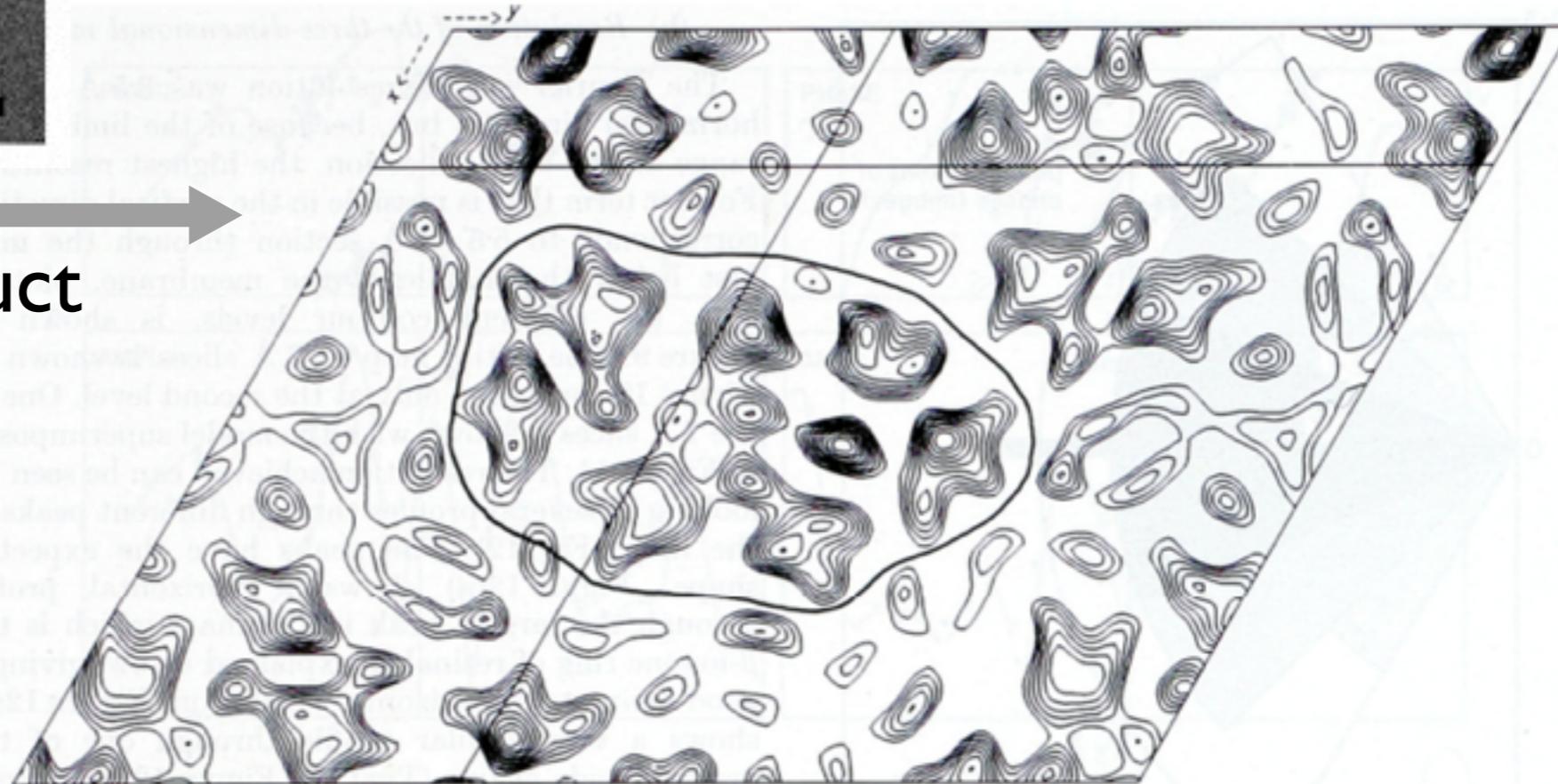
Single particle analysis

2-D electron crystallography



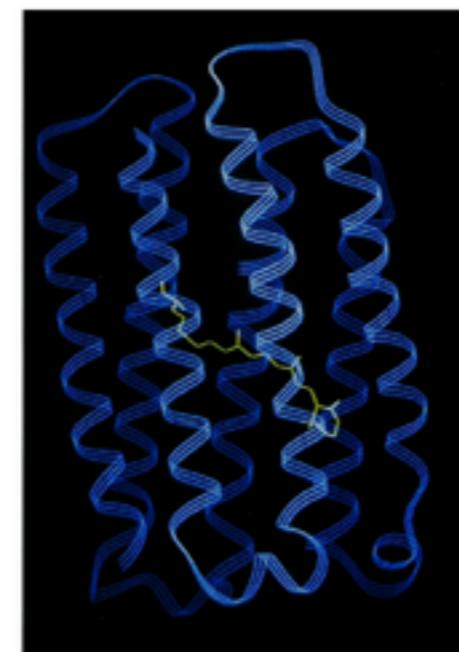
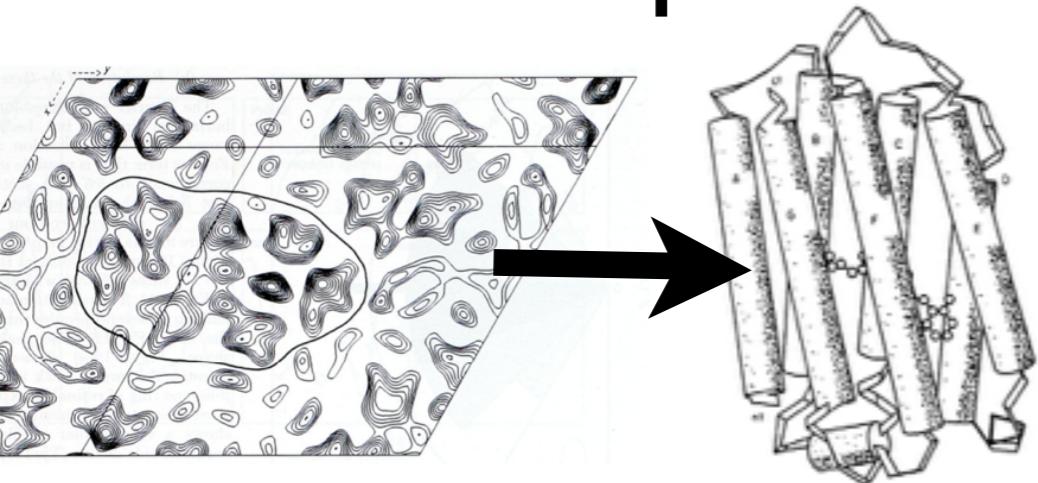
→ Reconstruct

useful because phases
aren't irretrievably lost
works better with smaller
crystals than X-rays, but
must be thin



Example structures

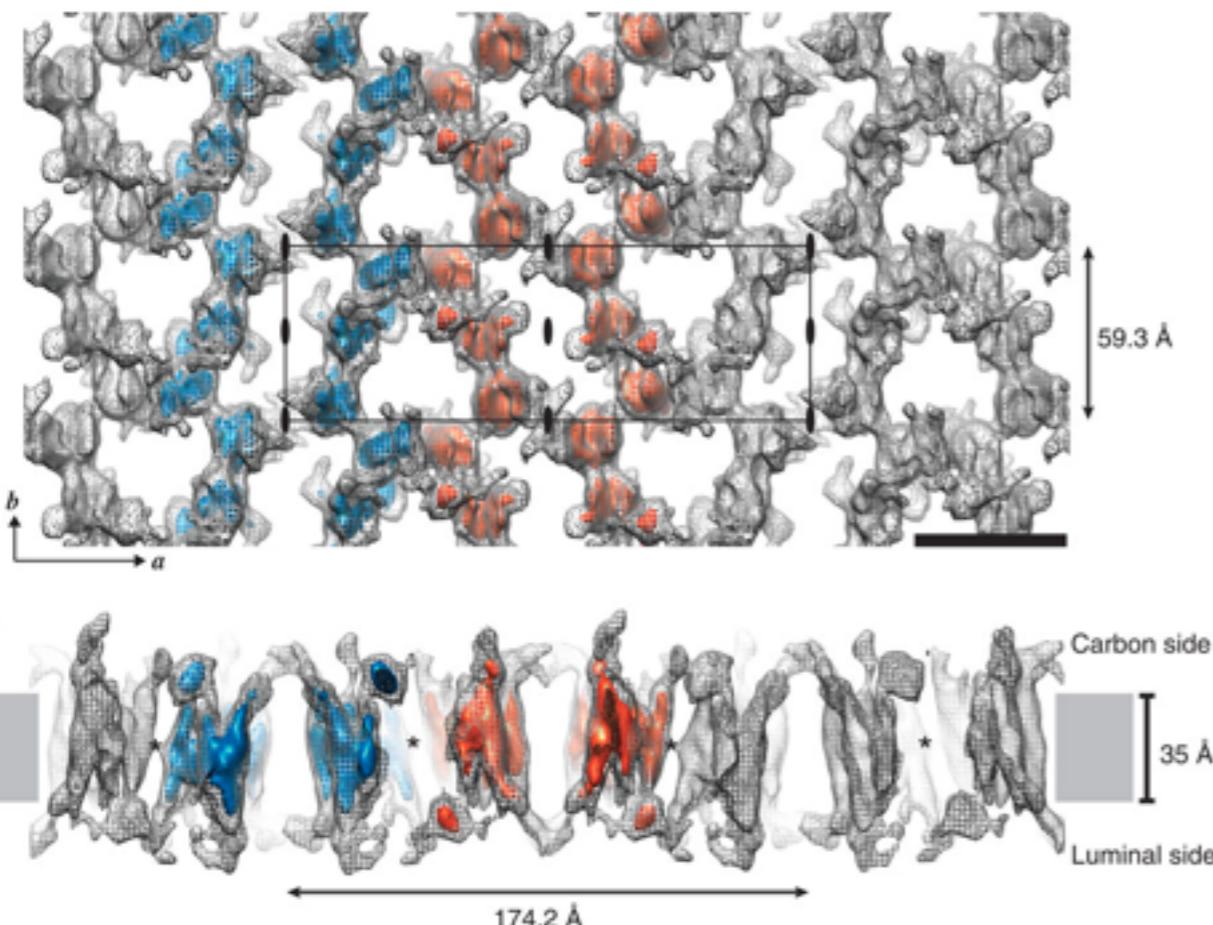
Bacteriorhodopsin



Henderson et al., 1990

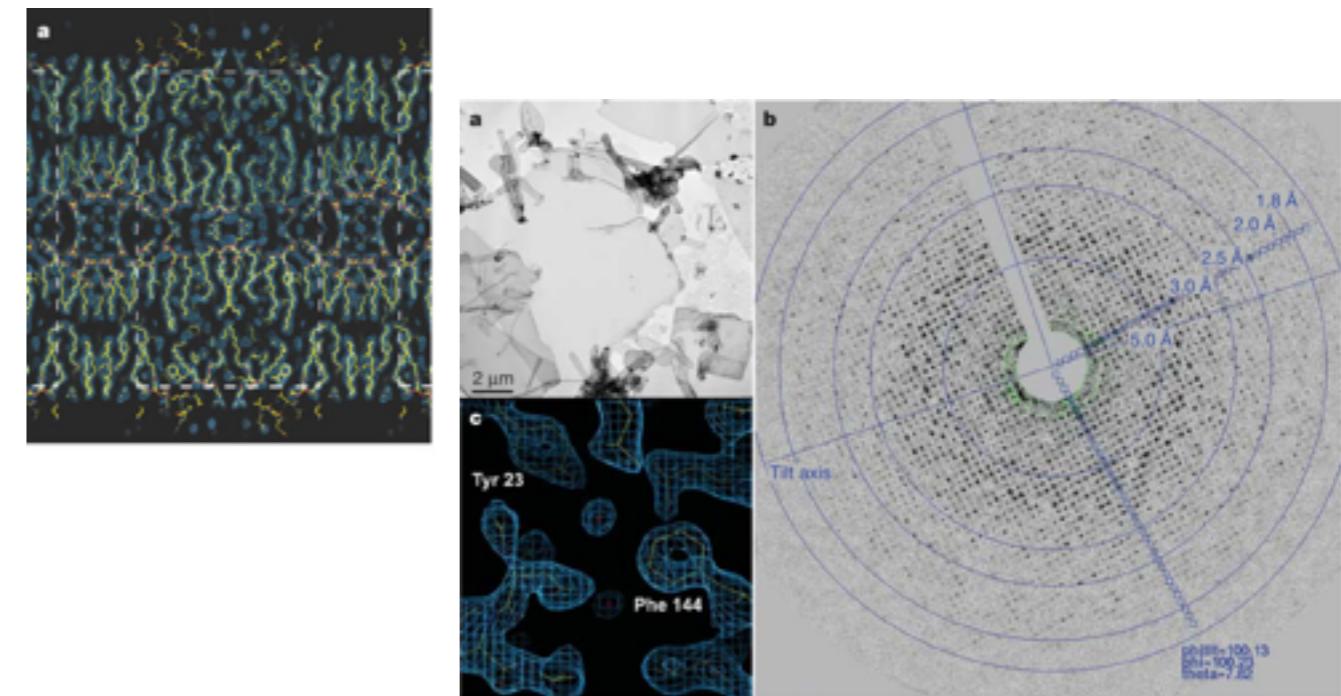
First ever electron crystallography structure, to 3.5 Å.

IP39 (~10 Å)



Suzuki et al. (2013) Nat. Comm. 4:1766.

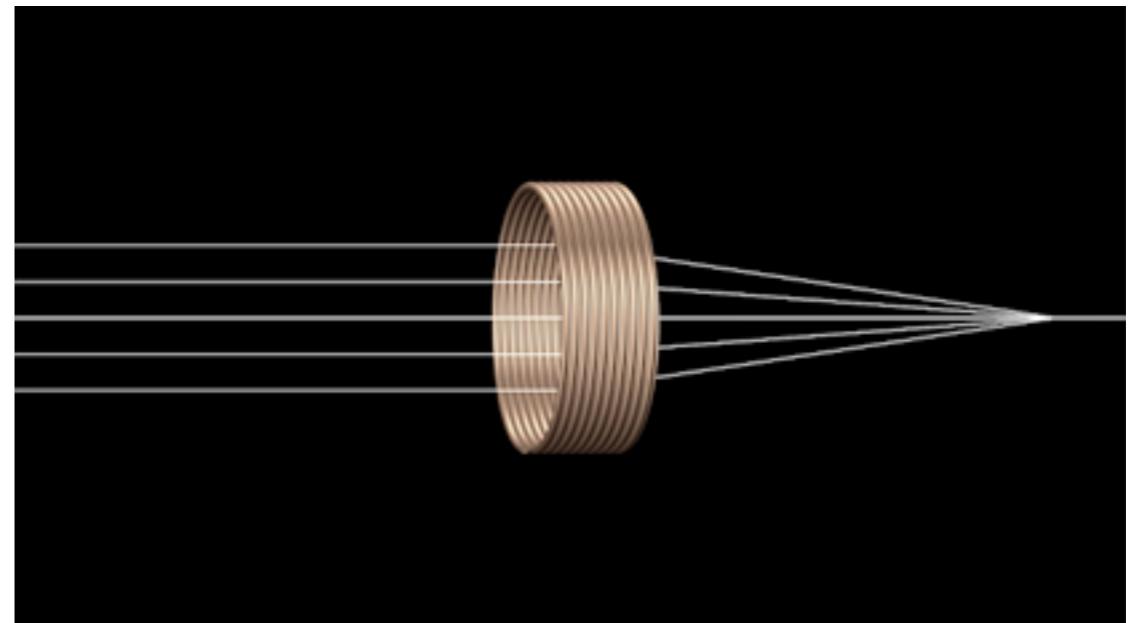
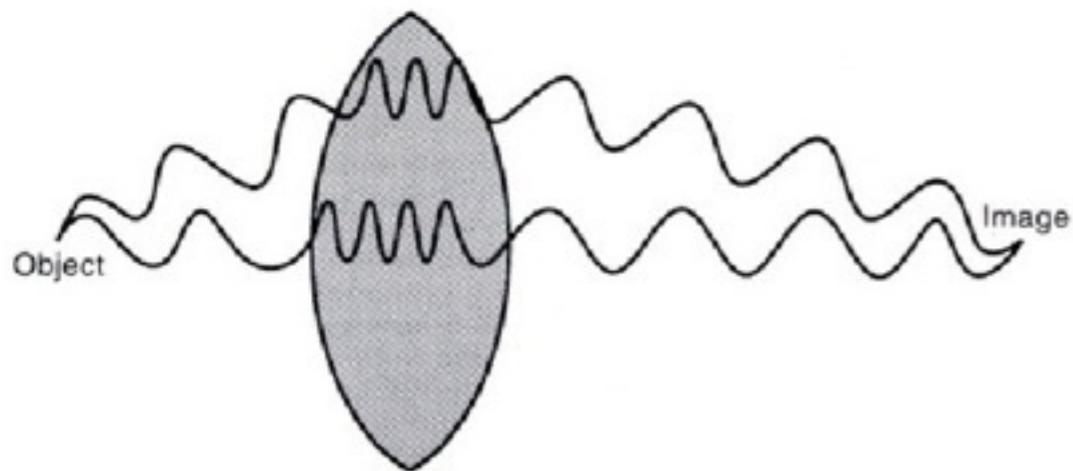
Aquaporin 0 (1.9 Å)



Gonen et al., Nature (2005) 438:633

electron lenses

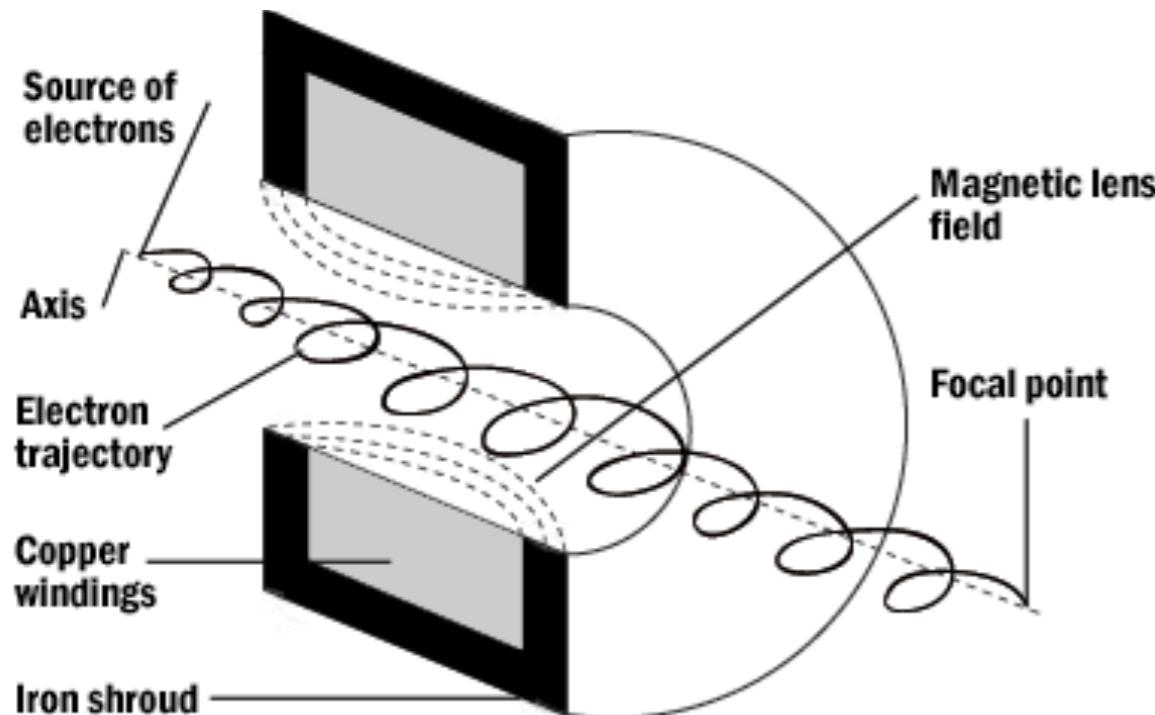
Lenses “focus” divergent (diffracted) rays, allow production of image (including magnification)



<http://www.first-tonomura-pj.net/e/commentary/mechanism/index.html>

For electrons, the “lens” is actually a magnetic field

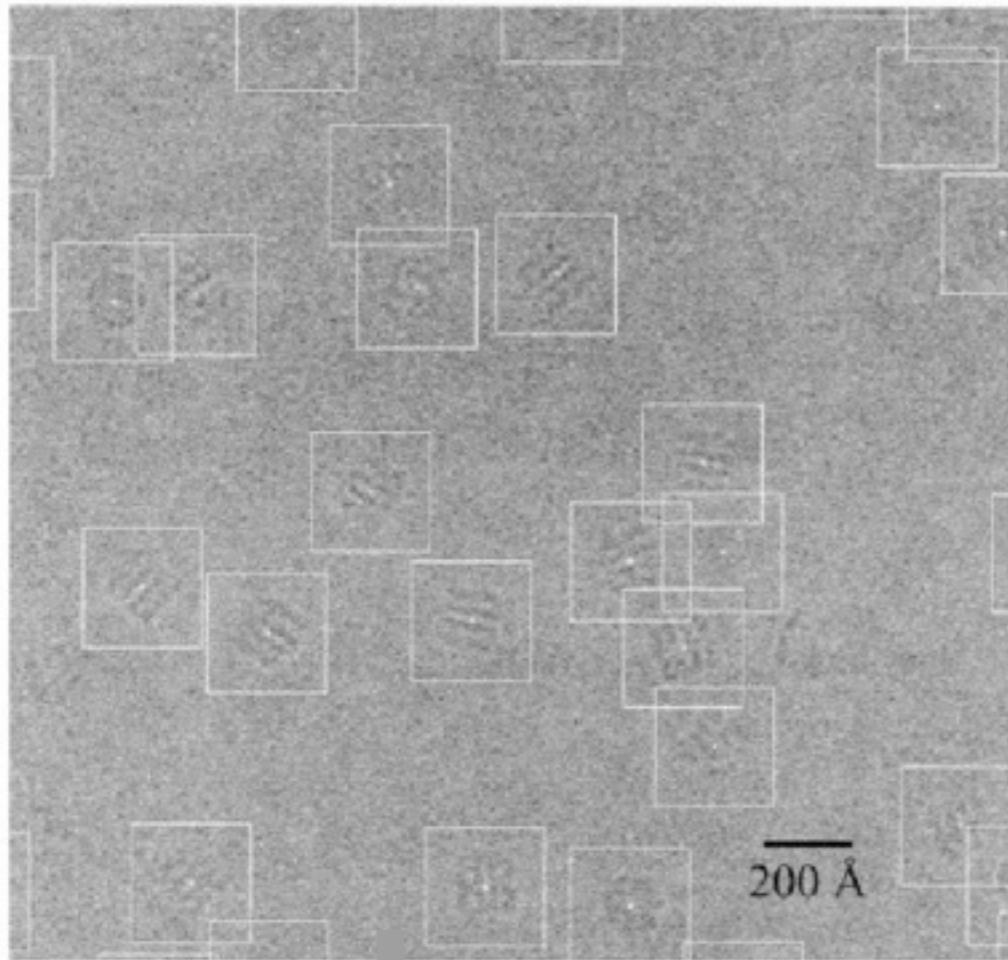
$$\mathbf{F} = -e (\mathbf{v} \times \mathbf{B})$$



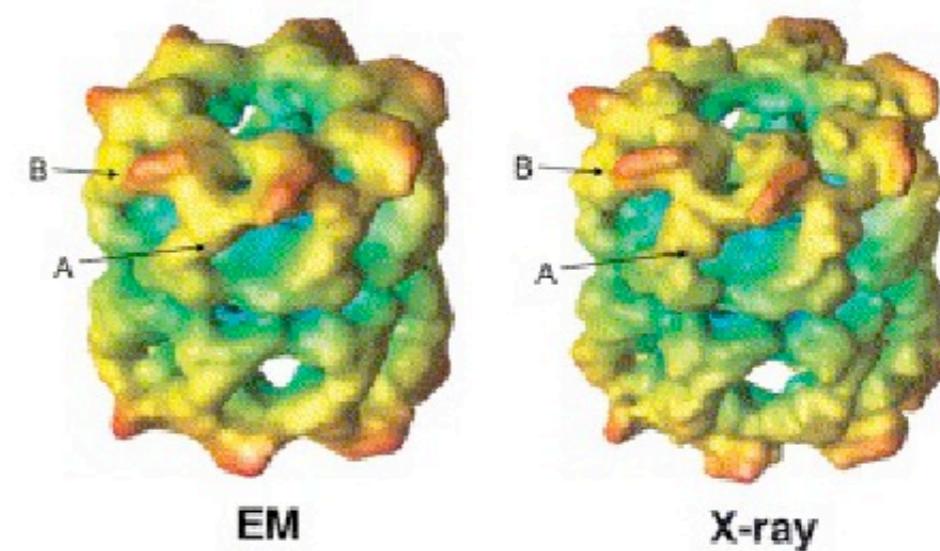
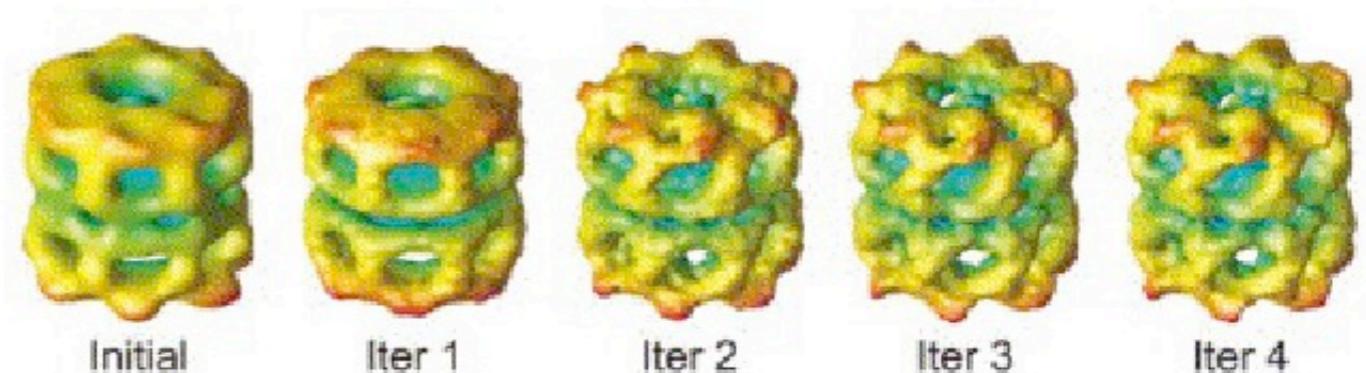
spiraling effect required to focus beam, but introduces unavoidable artifacts

Single particle analysis (cryo-EM)

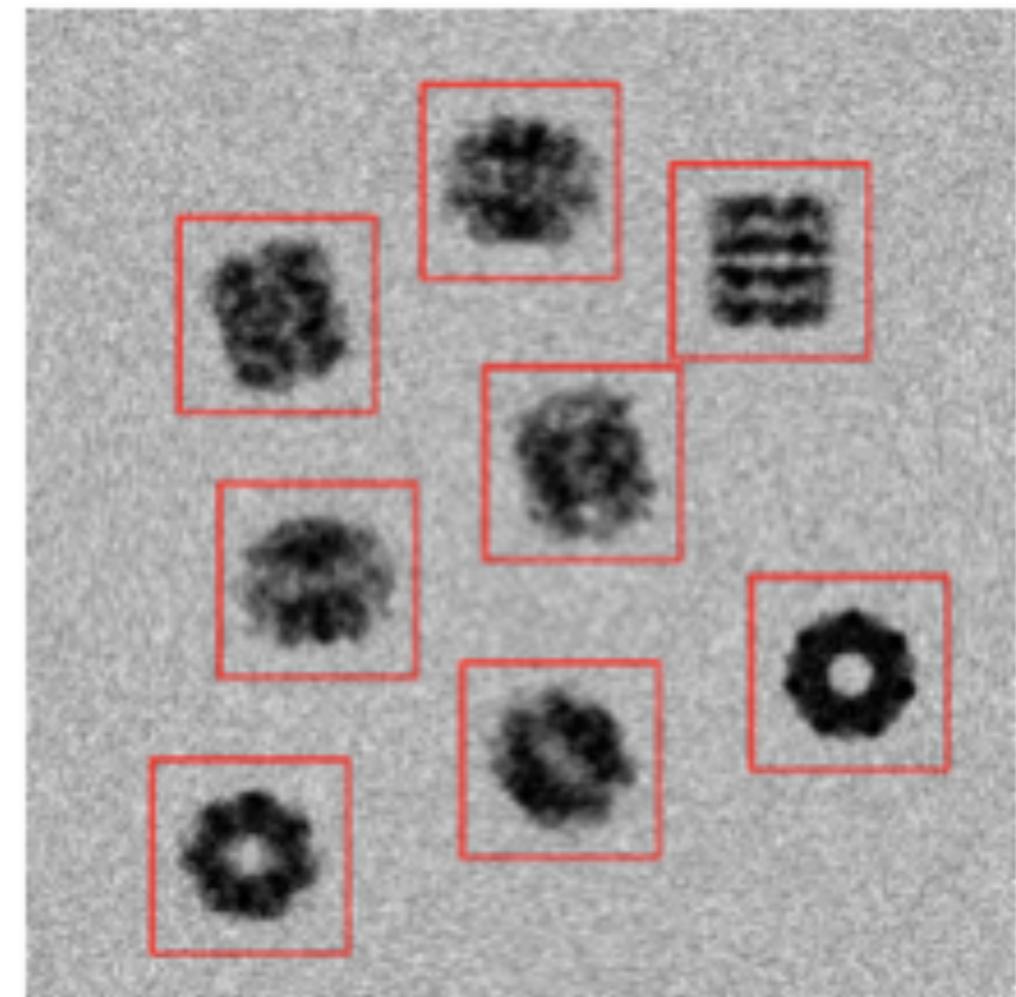
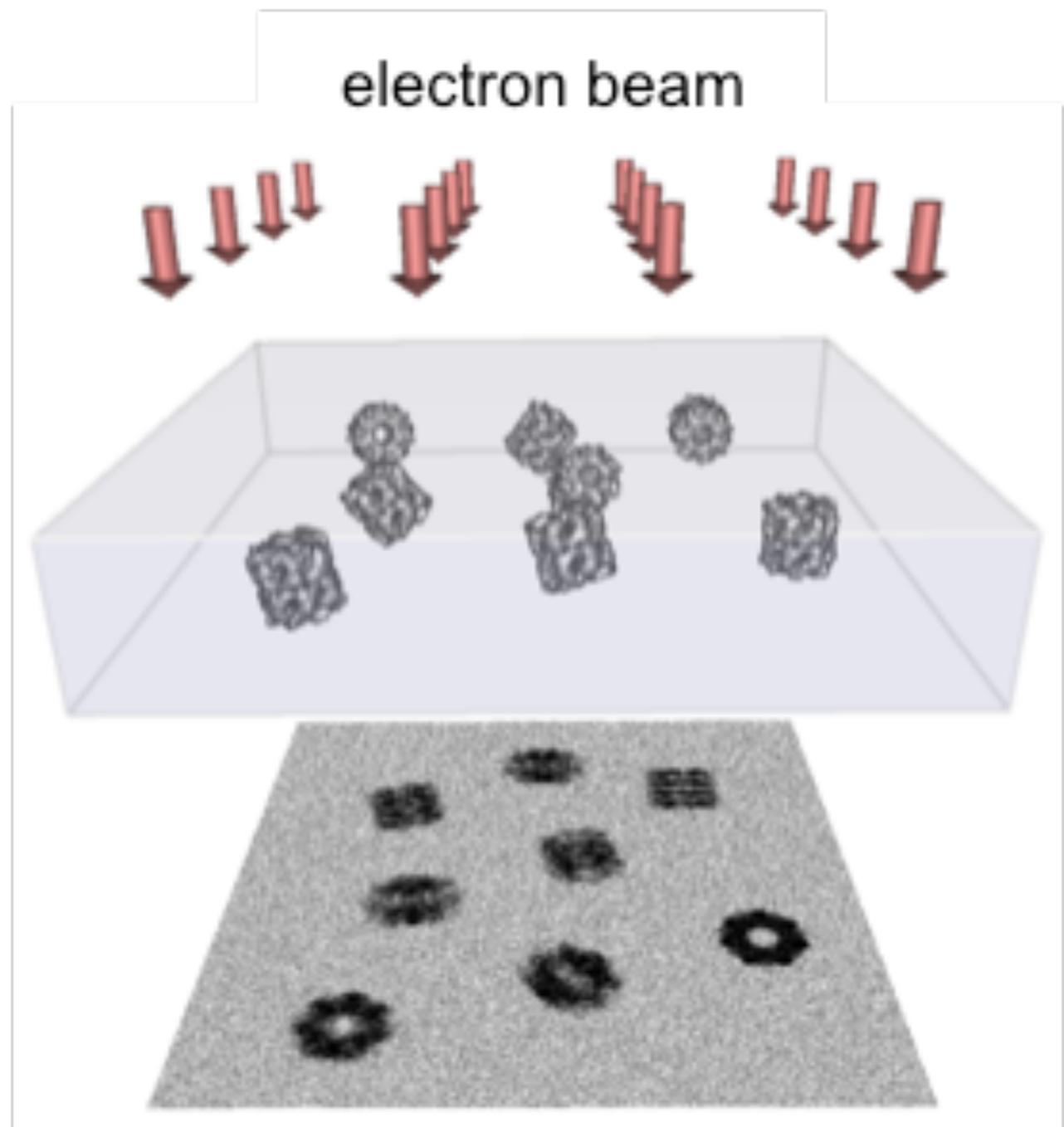
100 000's of ("identical") 2-D particles



Align and average



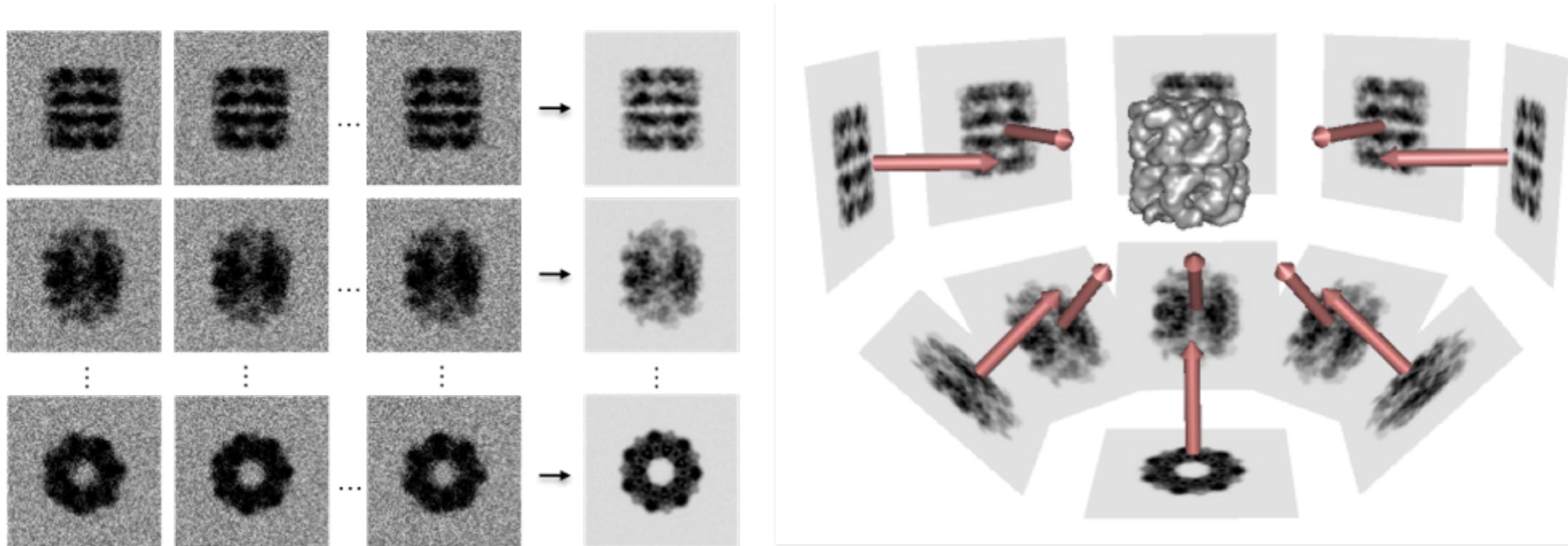
sorting the data



<http://people.csail.mit.edu/gdp/cryoem.html>

2D images are aligned and sorted computationally into classes representing homogeneous particles and perspectives

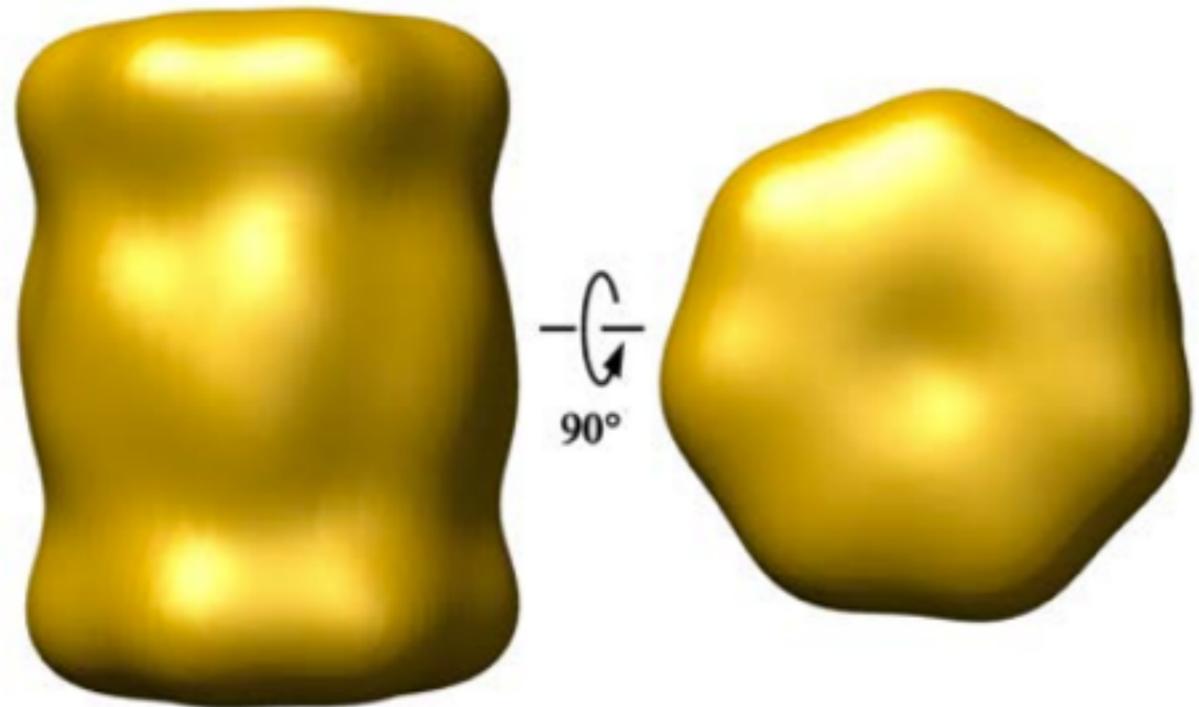
Class averages



<http://people.csail.mit.edu/gdp/cryoem.html>

classes are then averaged and back-projected to produce 3D density map

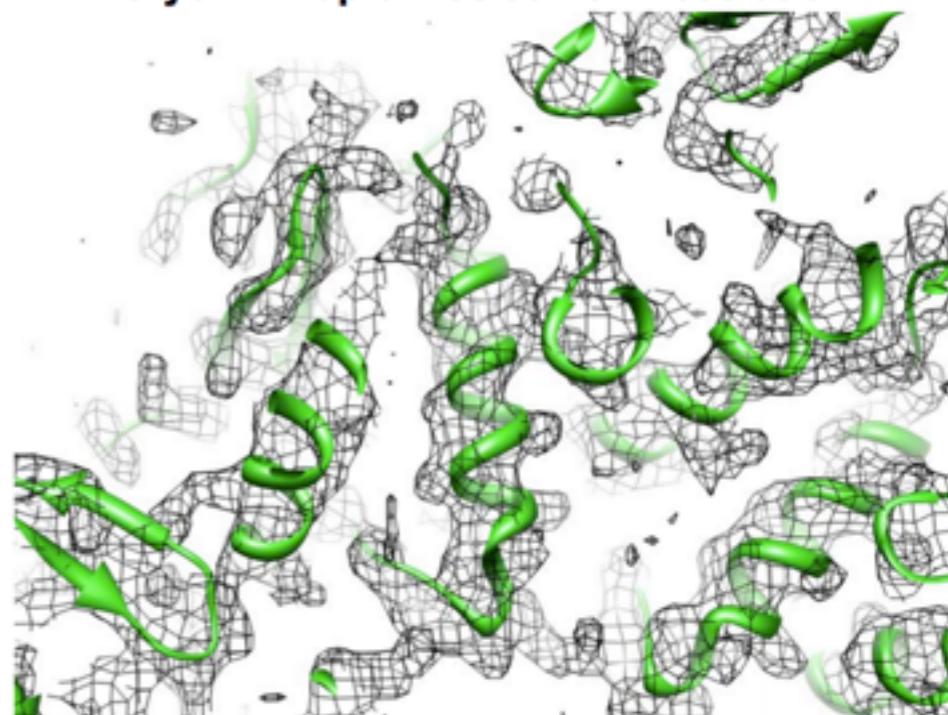
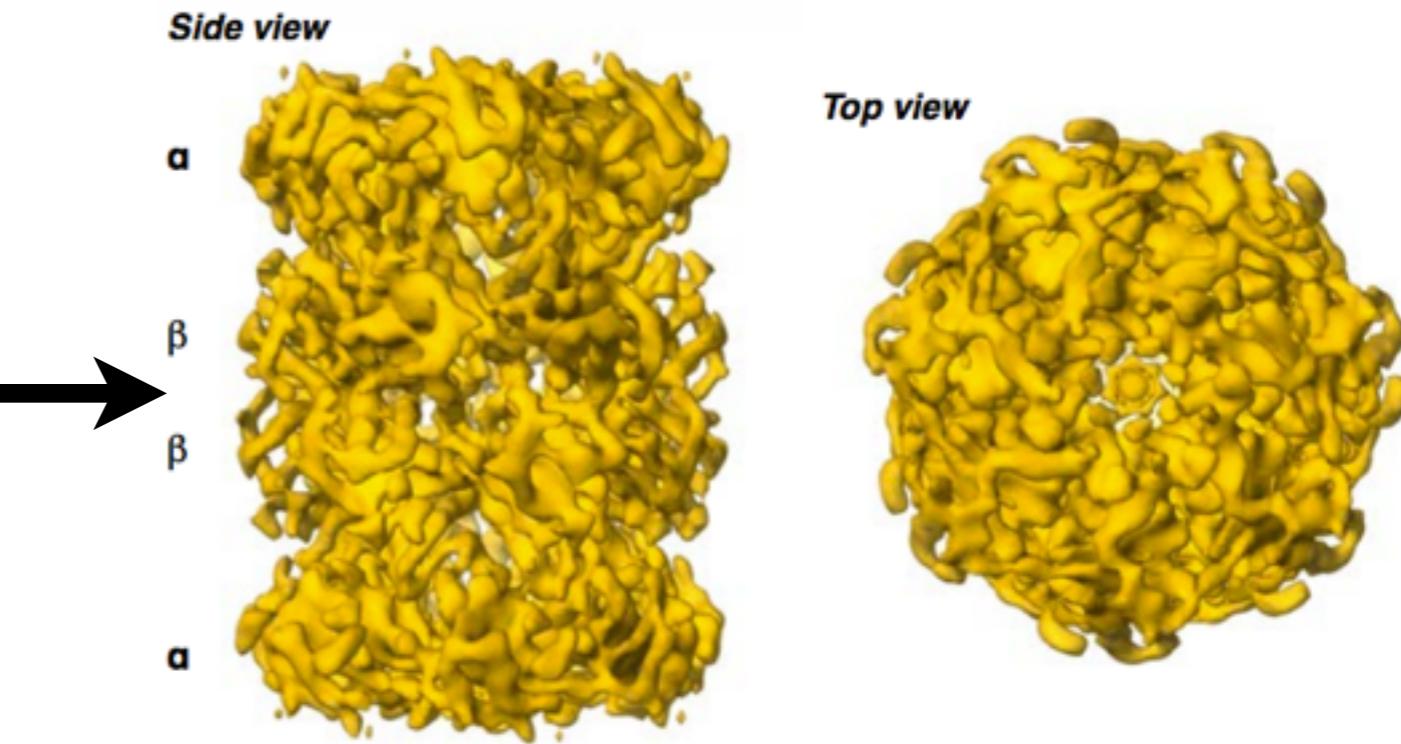
iterative refinement



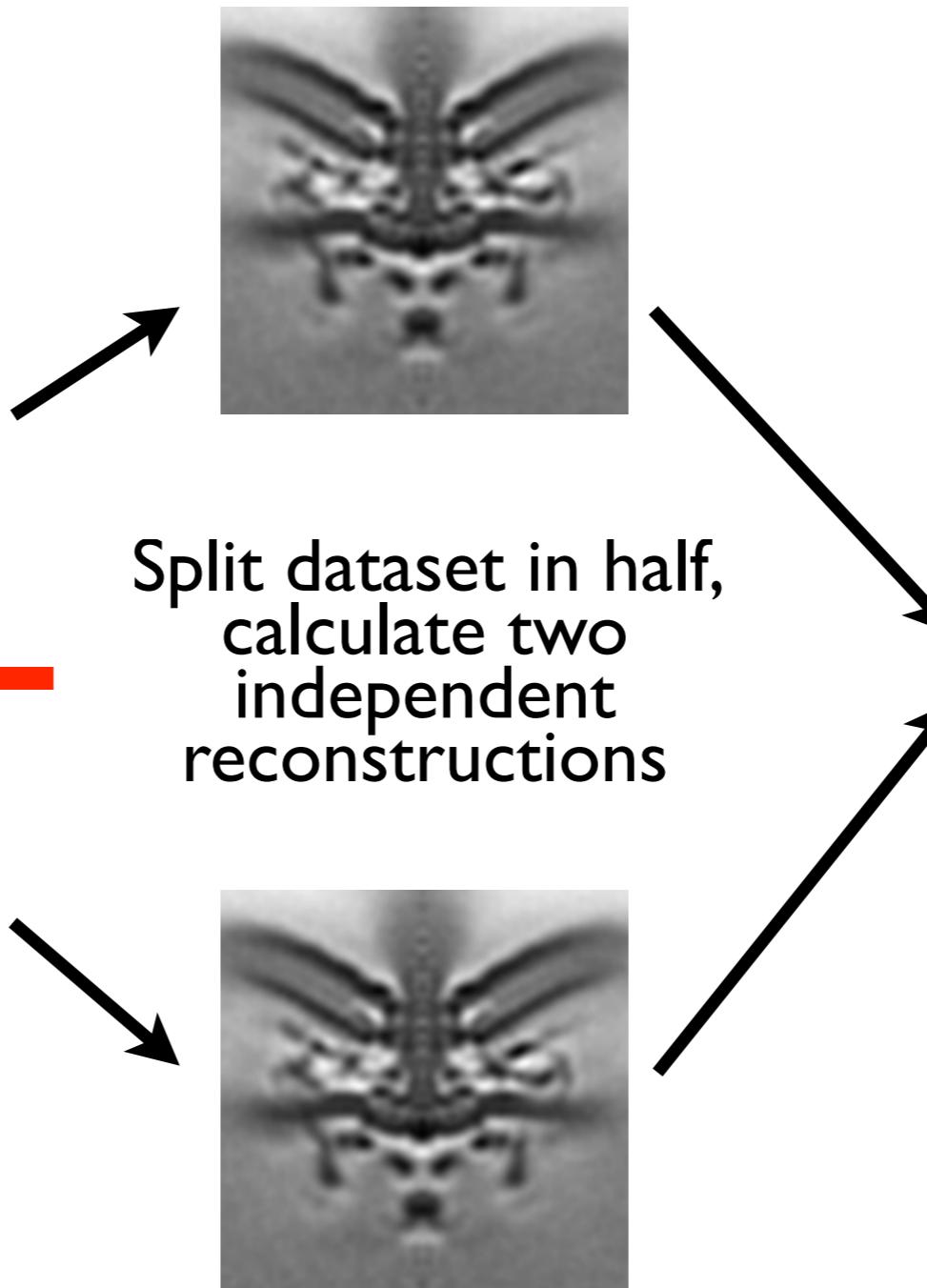
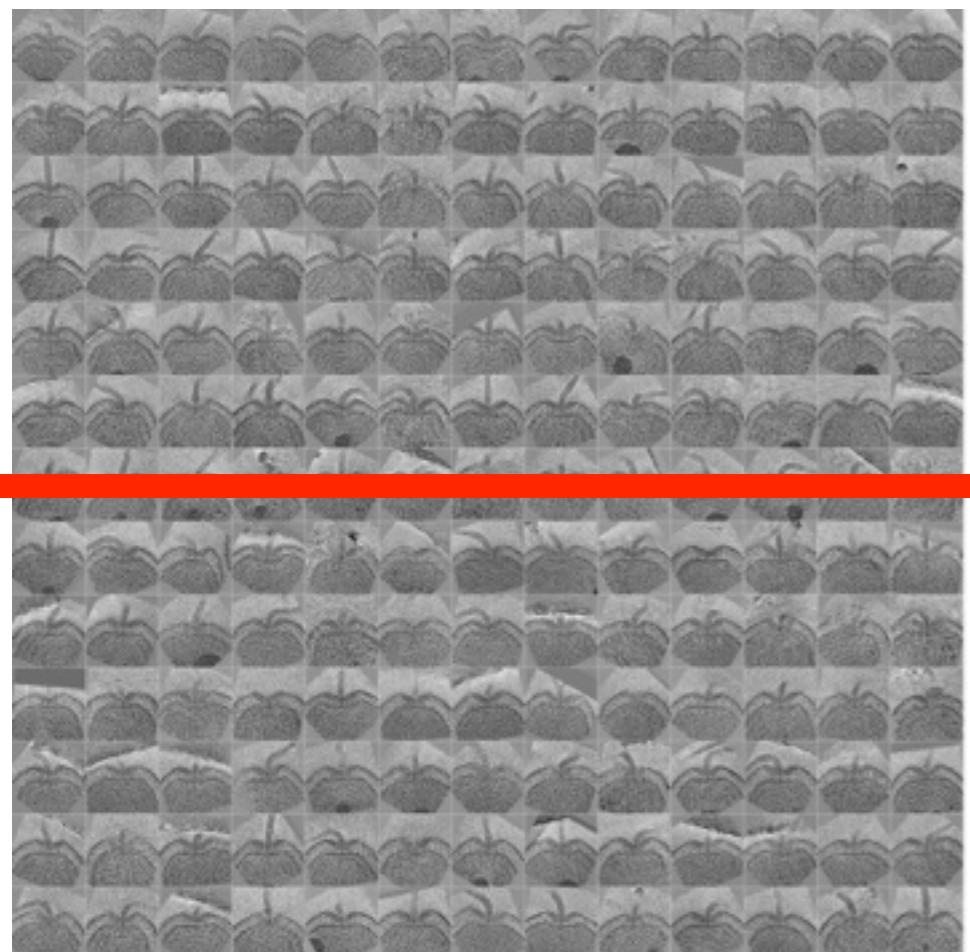
*cryo-EM map of the proteosome
(iteration 1)*

back projection is iterative - need the model for
projection matching with class averages

maps can have resolutions ranging from near-
atomic ($<5\text{ \AA}$) to 2-3 nm



map resolution



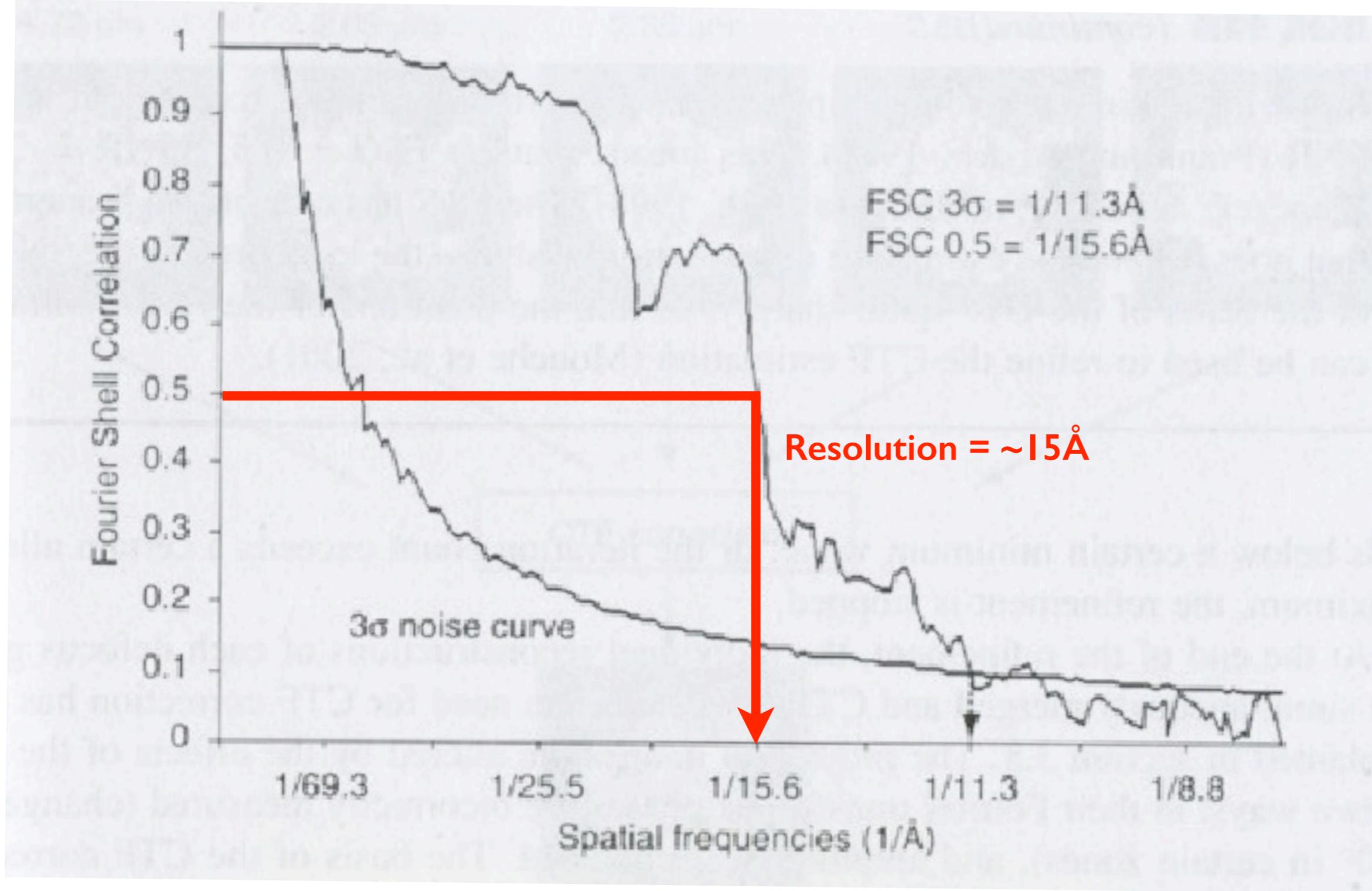
Align two
structures, flip
into reciprocal
space (i.e., 3D FT),
and calculate
correlation co-
efficients between
bands of spatial
frequency

Fourier shell correlation:

$$FSC(r) = \frac{\sum_{r_i \in r} F_1(r_i) \cdot F_2(r_i)^*}{\sqrt[2]{\sum_{r_i \in r} |F_1(r_i)|^2 \cdot \sum_{r_i \in r} |F_2(r_i)|^2}}$$

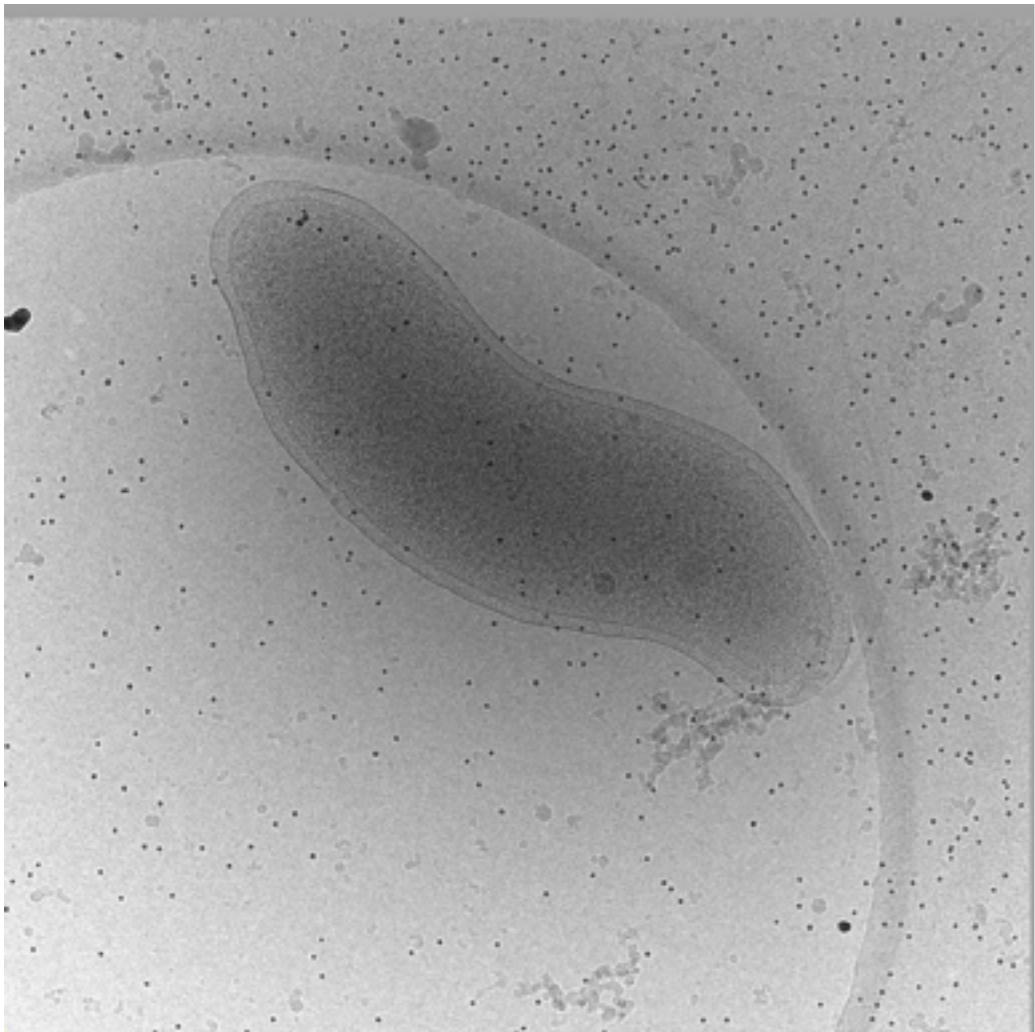
map resolution

FSC between two halves of the data set



Electron cryo-tomography

~100 2D images



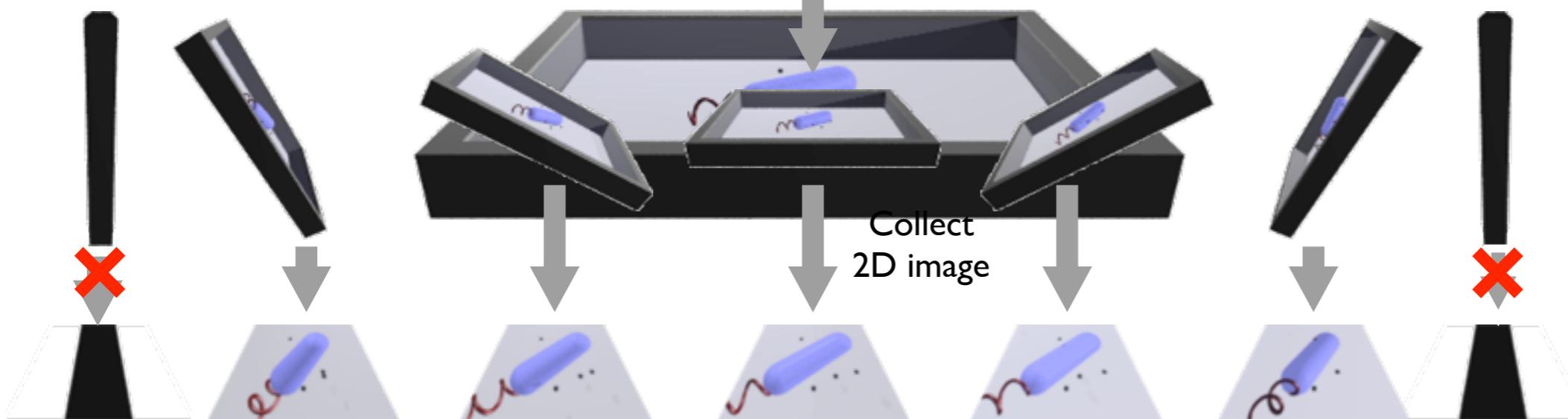
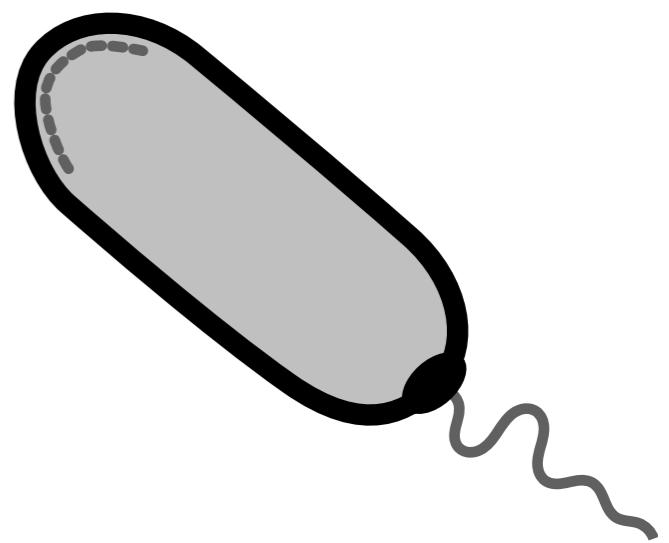
3D tomogram



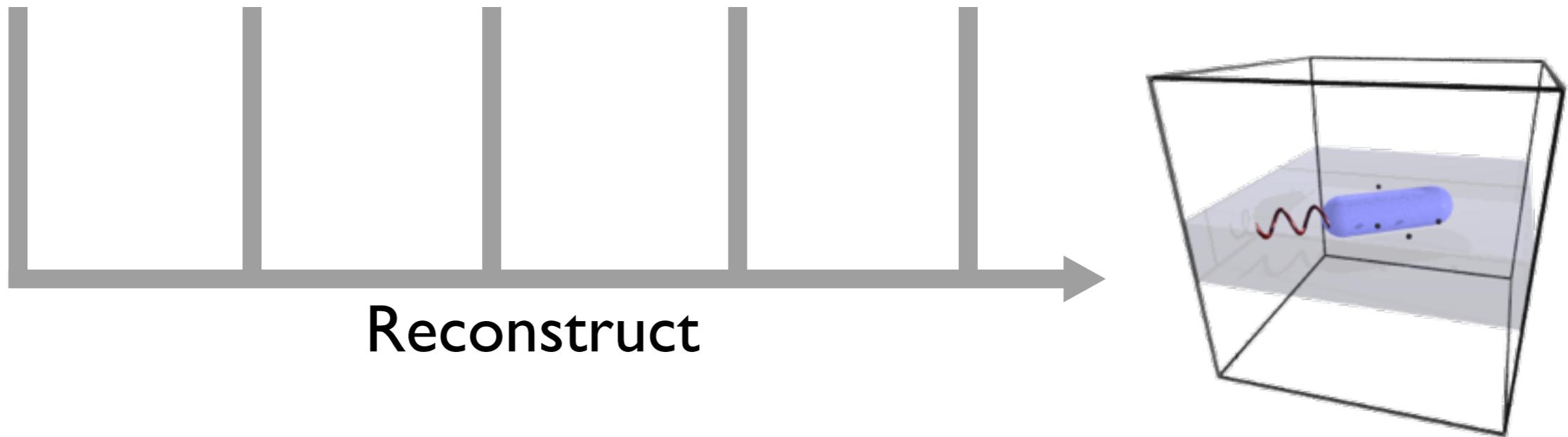
Reconstruct

Principle of tomography

Flash freeze

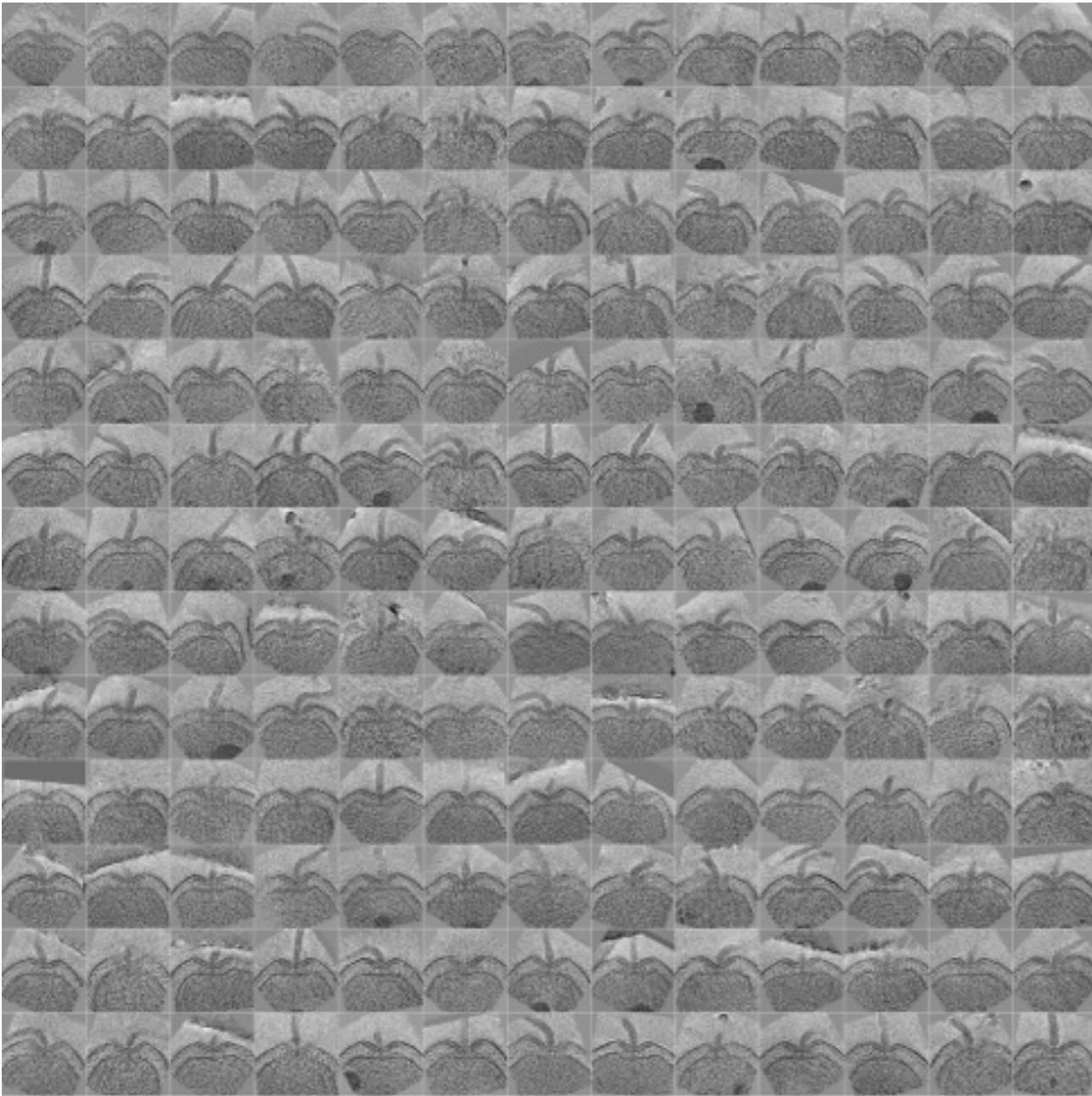


Reconstruct

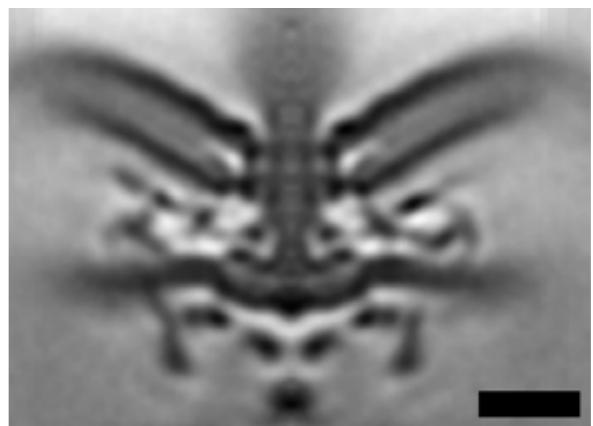
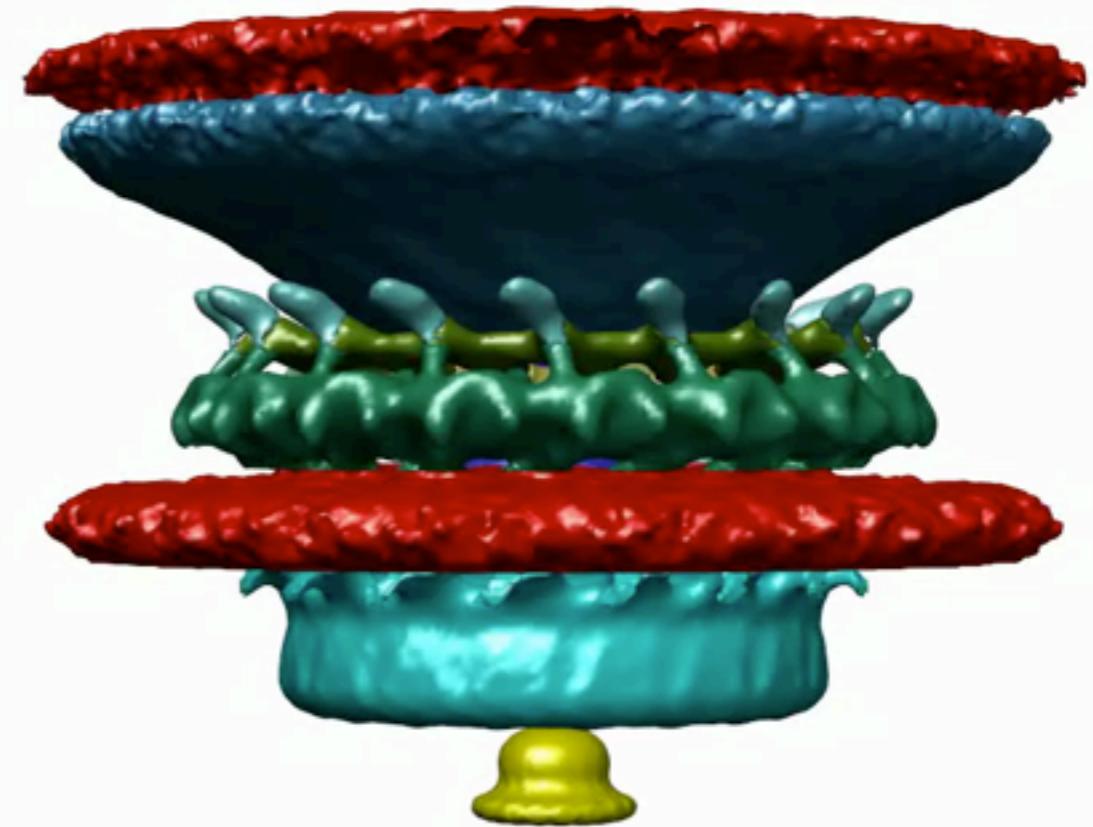


Subtomogram averaging

100's of ("identical") 3-D particles



Align and average



Identifying cellular features

