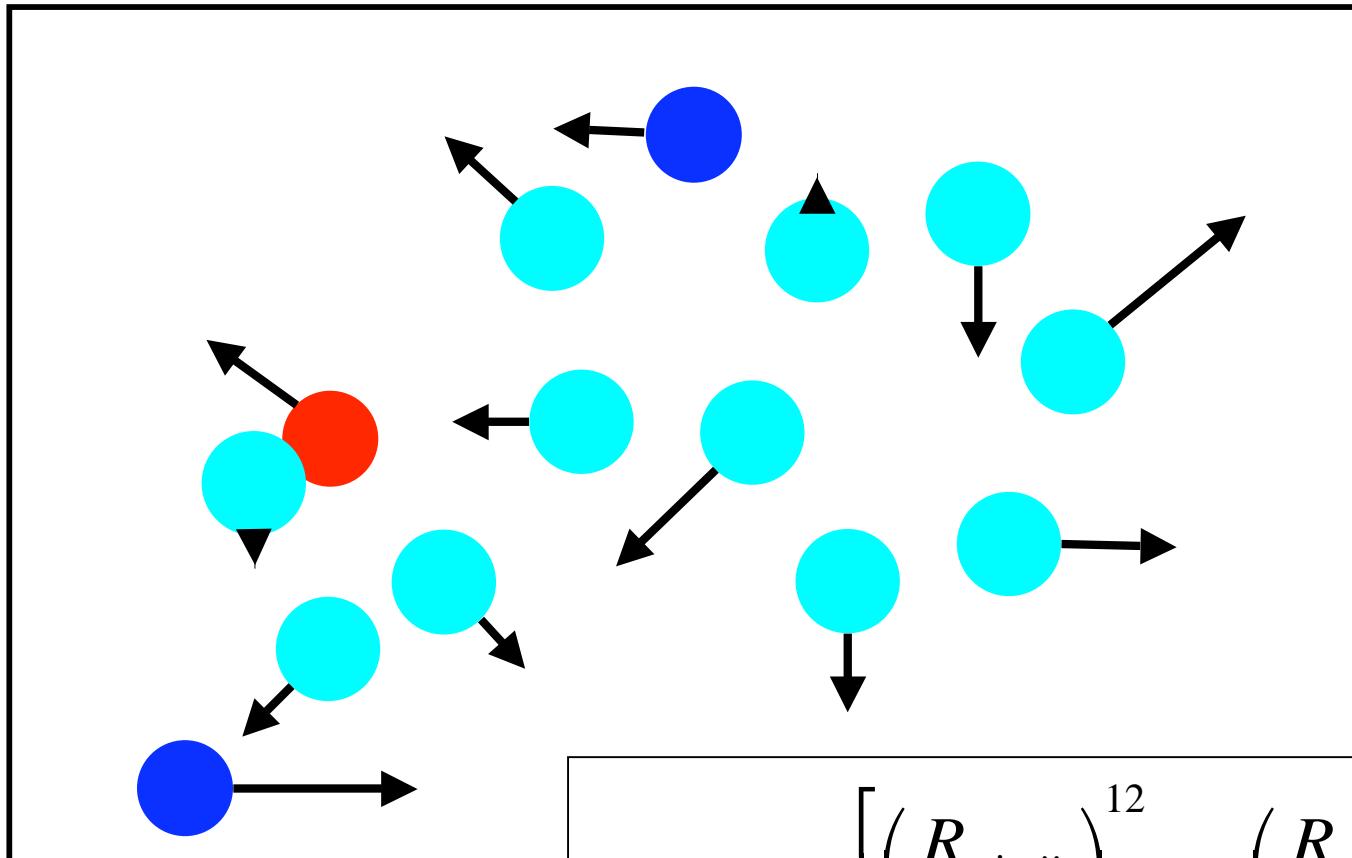


Force Fields for MD simulations

- Topology/parameter files
- Where do the numbers an MD code uses come from?
- How to make topology files for ligands, cofactors, special amino acids, ...
- How to obtain/develop missing parameters.

Classical Molecular Dynamics



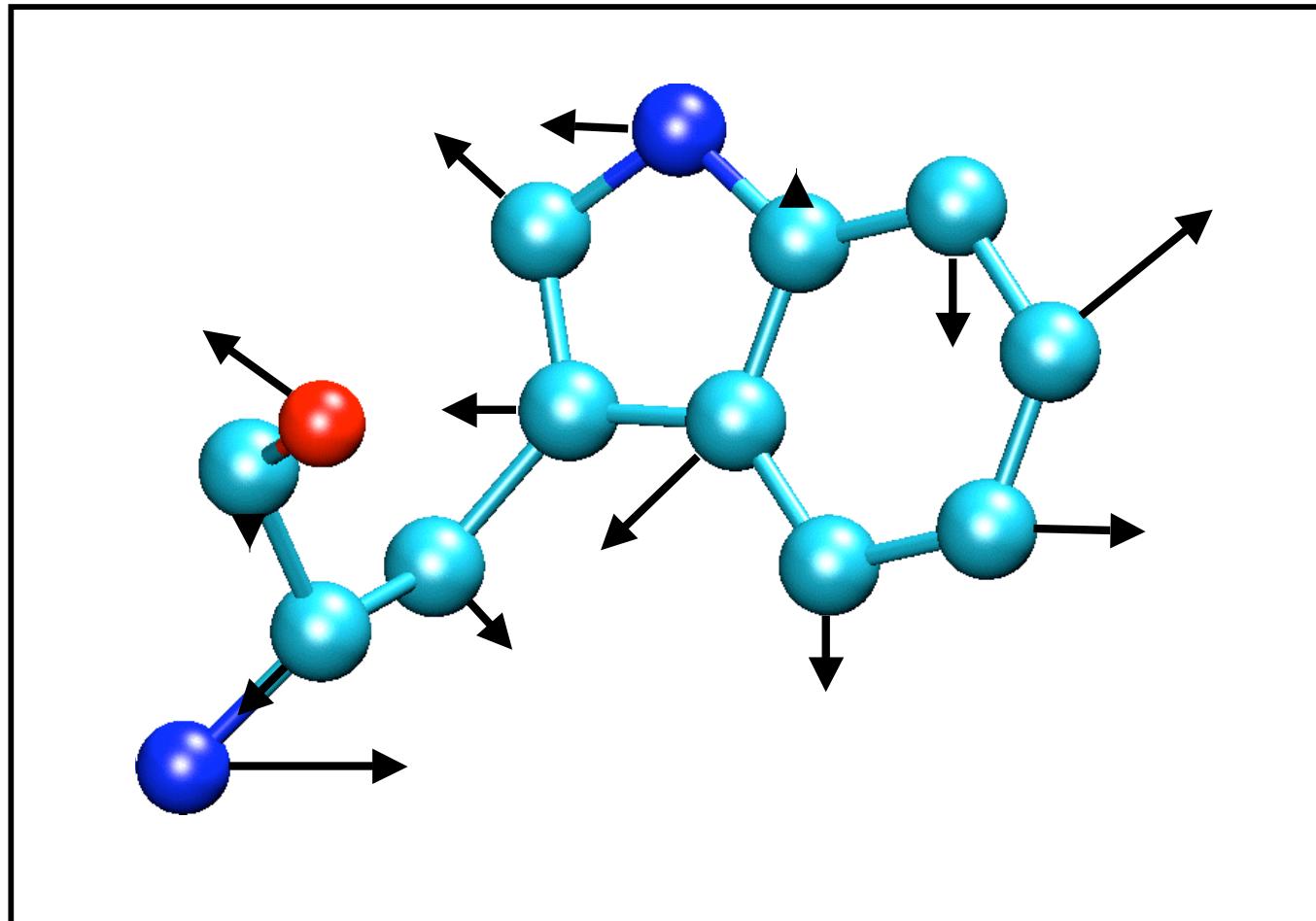
$$U(r) = \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}}$$

Coulomb interaction

$$U(r) = \epsilon_{ij} \left[\left(\frac{R_{\min,ij}}{r_{ij}} \right)^{12} - 2 \left(\frac{R_{\min,ij}}{r_{ij}} \right)^6 \right]$$

van der Waals interaction

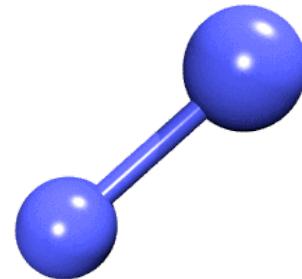
Classical Molecular Dynamics



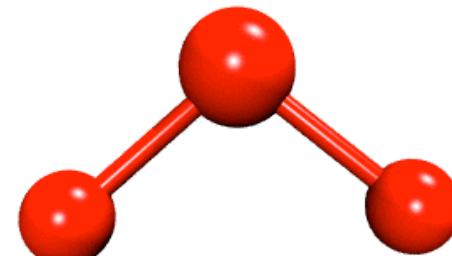
Bond definitions, atom types, atom names, parameters,

Energy Terms Described in the CHARMM Force Field

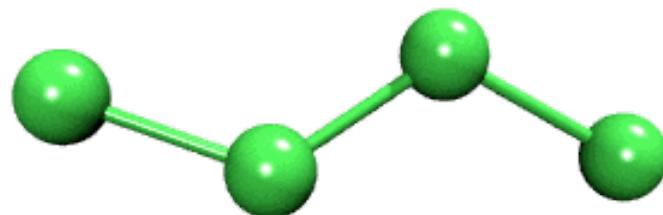
Bond



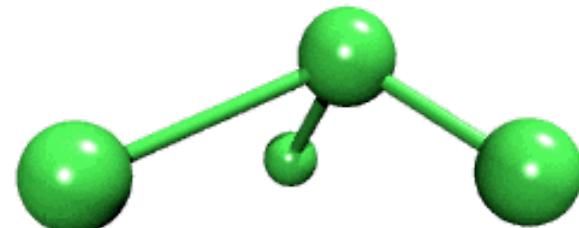
Angle



Dihedral



Improper



The Potential Energy Function

$$U(\vec{R}) = \underbrace{\sum_{bonds} k_i^{bond} (r_i - r_0)^2}_{U_{bond}} + \underbrace{\sum_{angles} k_i^{angle} (\theta_i - \theta_0)^2}_{U_{angle}} + \underbrace{\sum_{dihedrals} k_i^{dihed} [1 + \cos(n_i \phi_i + \delta_i)]}_{U_{dihedral}} + \underbrace{\sum_i \sum_{j \neq i} 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \sum_i \sum_{j \neq i} \frac{q_i q_j}{\epsilon r_{ij}}}_{U_{nonbond}}$$

U_{bond} = oscillations about the equilibrium bond length

U_{angle} = oscillations of 3 atoms about an equilibrium bond angle

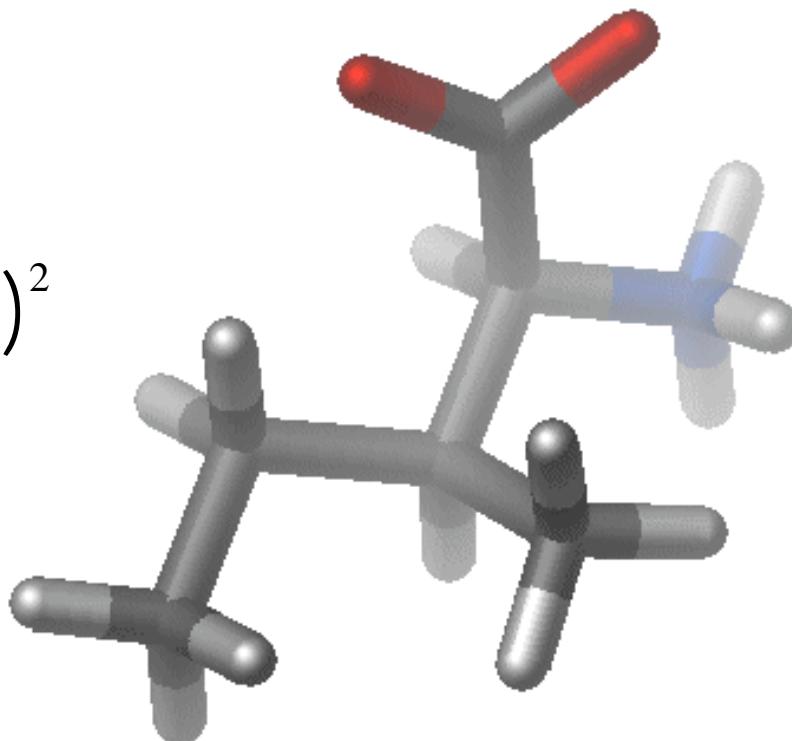
$U_{dihedral}$ = torsional rotation of 4 atoms about a central bond

$U_{nonbond}$ = non-bonded energy terms (electrostatics and Lenard-Jones)

Interactions between bonded atoms

$$V_{angle} = K_\theta (\theta - \theta_o)^2$$

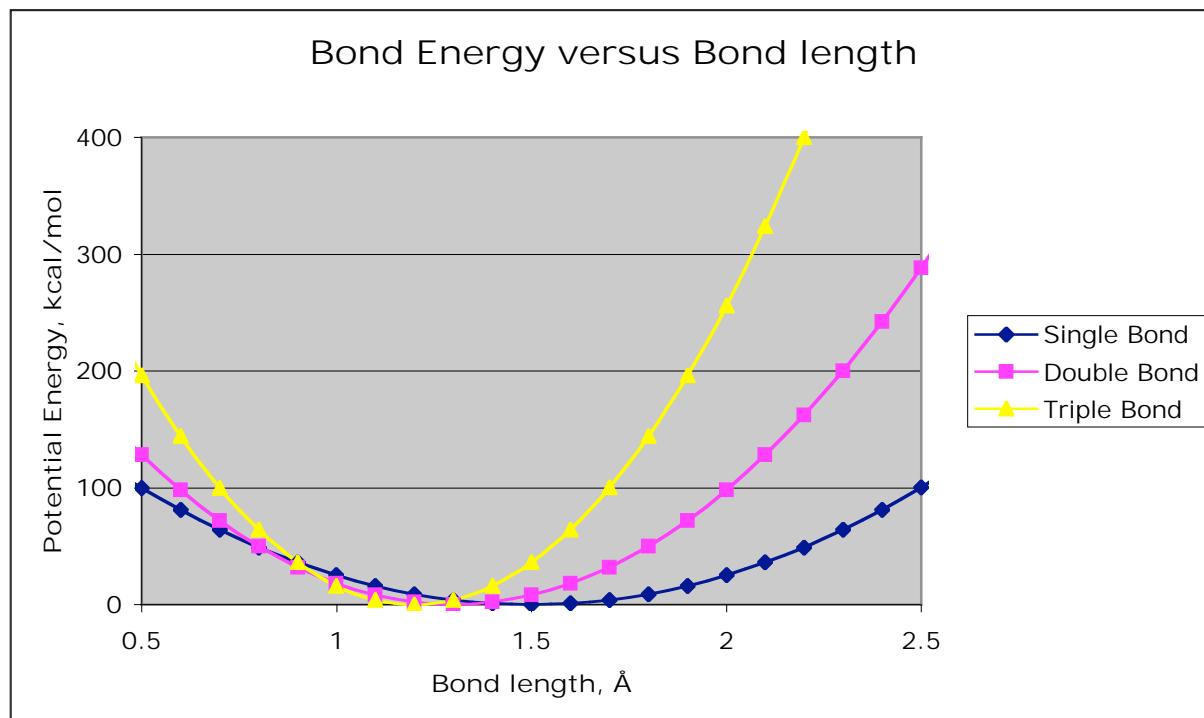
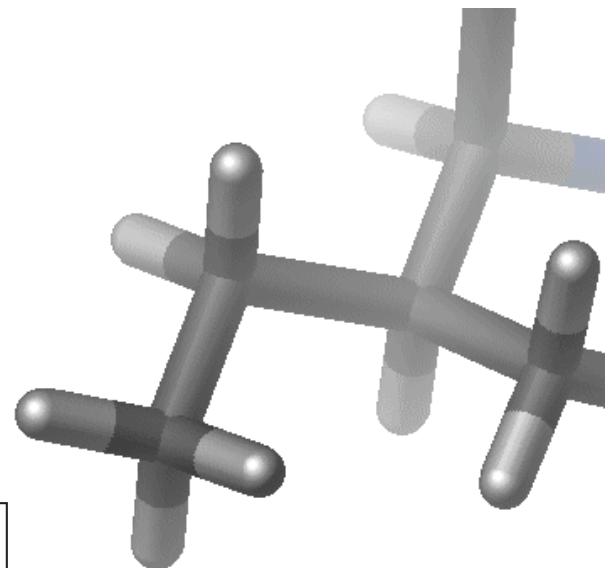
$$V_{bond} = K_b (b - b_o)^2$$



$$V_{dihedral} = K_\phi (1 + \cos(n\phi - \delta))$$

$$V_{bond} = K_b (b - b_o)^2$$

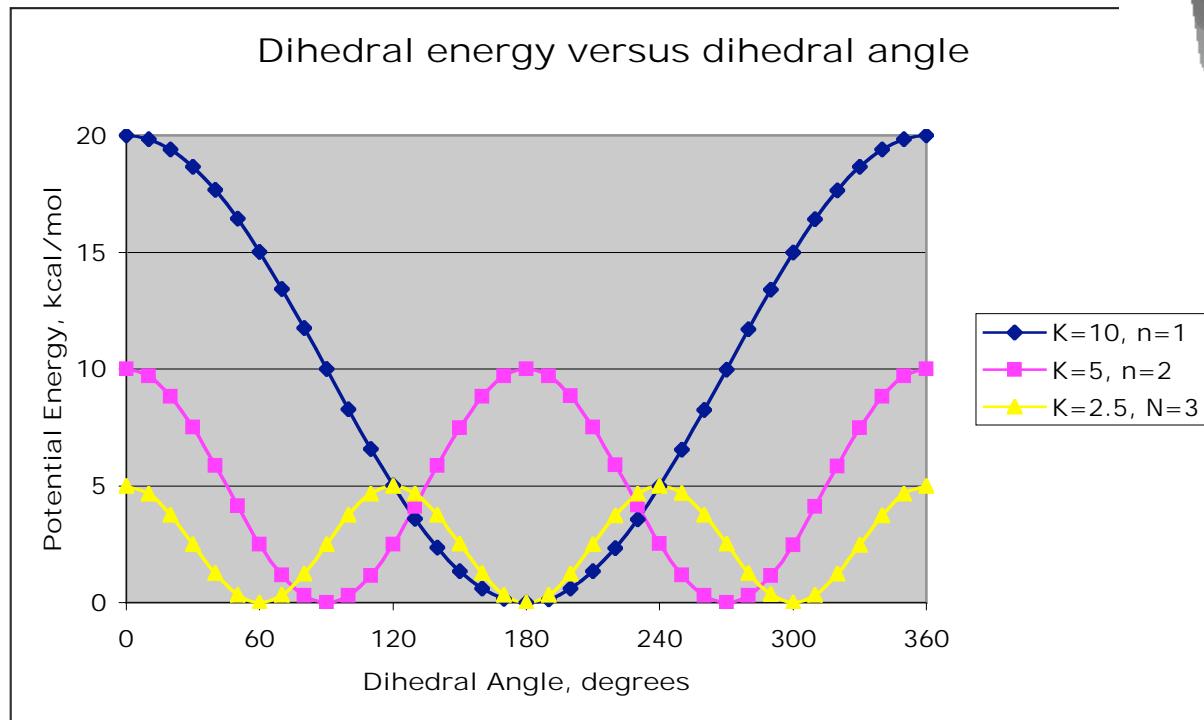
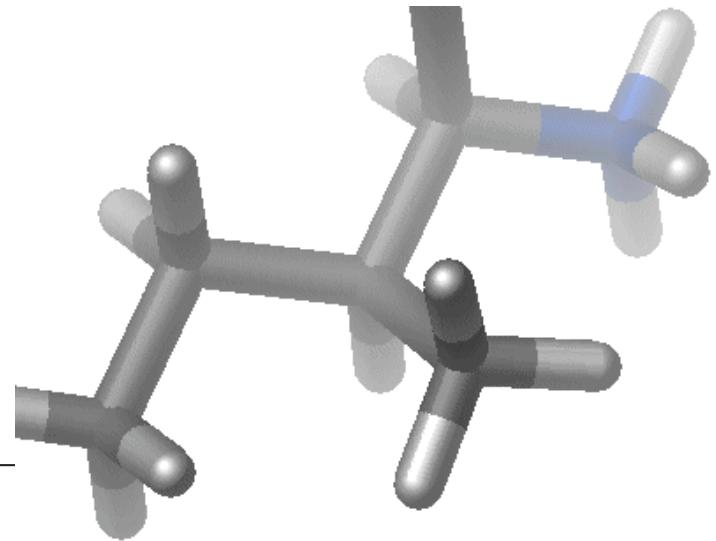
Chemical type	K_{bond}	b_o
C-C	100 kcal/mole/Å ⁻²	1.5 Å
C=C	200 kcal/mole/Å ⁻²	1.3 Å
C≡C	400 kcal/mole/Å ⁻²	1.2 Å



Bond angles and *improper terms* have similar quadratic forms, but with softer spring constants. The force constants can be obtained from vibrational analysis of the molecule (experimentally or theoretically).

Dihedral Potential

$$V_{dihedral} = K_\phi (1 + \cos(n\phi - \delta))$$



$$\delta = 0^\circ$$

Nonbonded Parameters

$$\sum_{nonbonded} \frac{q_i q_j}{4\pi D r_{ij}} + \epsilon_{ij} \left[\left(\frac{R_{min,ij}}{r_{ij}} \right)^{12} - 2 \left(\frac{R_{min,ij}}{r_{ij}} \right)^6 \right]$$

q_i : partial atomic charge

D : dielectric constant

ϵ : Lennard-Jones (LJ, vdW) well-depth

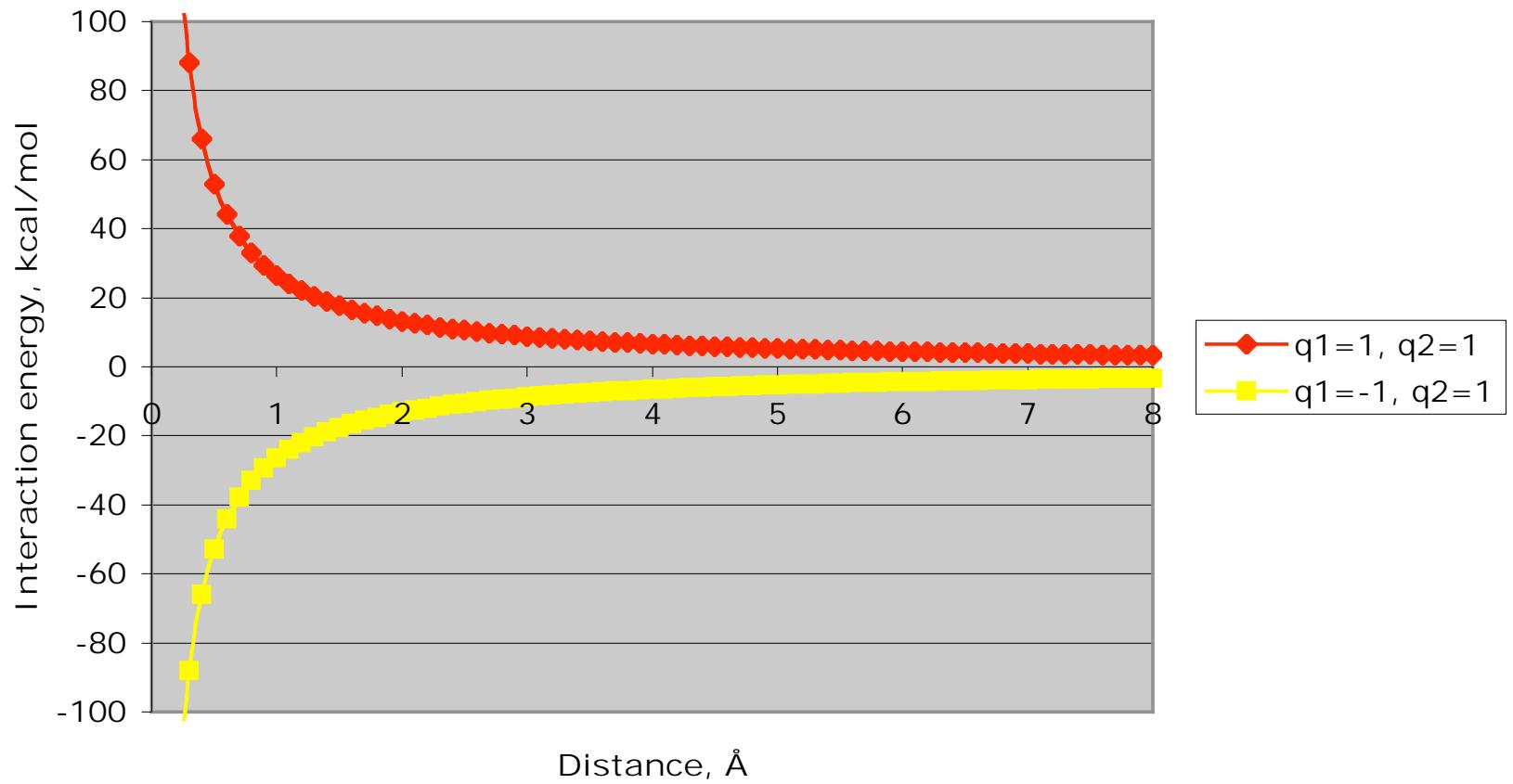
R_{min} : LJ radius ($R_{min}/2$ in CHARMM)

Combining rules (CHARMM, Amber)

$$R_{min\ i,j} = R_{min\ i} + R_{min\ j}$$

$$\epsilon_{i,j} = \text{SQRT}(\epsilon_i * \epsilon_j)$$

Electrostatic Energy versus Distance



Note that the effect is long range.

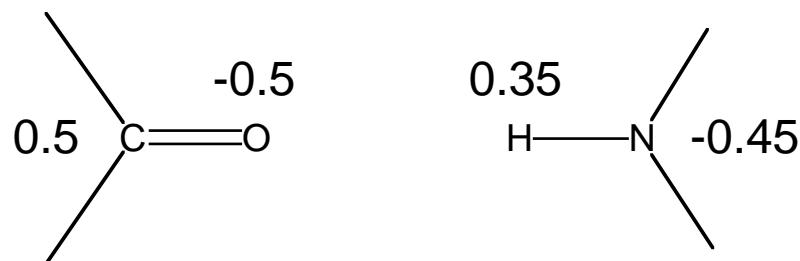
From MacKerell

Charge Fitting Strategy

CHARMM- Mulliken*

AMBER(ESP/RESP)

Partial atomic charges



*Modifications based on interactions with TIP3 water

CHARMM Potential Function

$$U(\vec{R}) = \underbrace{\sum_{bonds} k_i^{bond} (r_i - r_0)^2}_{U_{bond}} + \underbrace{\sum_{angles} k_i^{angle} (\theta_i - \theta_0)^2}_{U_{angle}} + \underbrace{\sum_{dihedrals} k_i^{dih} [1 + \cos(n_i \phi_i + \delta_i)]}_{U_{dihedral}} + \underbrace{\sum_i \sum_{j \neq i} 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]}_{U_{nonbond}} + \underbrace{\sum_i \sum_{j \neq i} \frac{q_i q_j}{\epsilon r_{ij}}}_{U_{electrostatic}}$$

Diagram illustrating the components of the CHARMM Potential Function:

- PDB file** provides **geometry** (bonds, angles, dihedrals).
- Topology PSF file** provides **parameters** (bond, angle, dihedral, nonbond, electrostatic parameters).
- Parameter file** provides **parameters** (bond, angle, dihedral, nonbond, electrostatic parameters).

Blue arrows point from the parameter files to the corresponding terms in the potential function. Red arrows point from the topology file to the bond, angle, dihedral, and nonbond terms.

File Format/Structure

- The structure of a pdb file
- The structure of a psf file
- The topology file
- The parameter file
- Connection to potential energy terms

Structure of a PDB file

	<i>index</i>		<i>resname</i>		<i>chain</i>	<i>resid</i>	<i>x</i>	<i>y</i>	<i>z</i>		<i>segname</i>
ATOM	22	N	ALA	B	3	-4.073	-7.587	-2.708	1.00	0.00	BH
ATOM	23	HN	ALA	B	3	-3.813	-6.675	-3.125	1.00	0.00	BH
ATOM	24	CA	ALA	B	3	-4.615	-7.557	-1.309	1.00	0.00	BH
ATOM	25	HA	ALA	B	3	-4.323	-8.453	-0.704	1.00	0.00	BH
ATOM	26	CB	ALA	B	3	-4.137	-6.277	-0.676	1.00	0.00	BH
ATOM	27	HB1	ALA	B	3	-3.128	-5.950	-0.907	1.00	0.00	BH
ATOM	28	HB2	ALA	B	3	-4.724	-5.439	-1.015	1.00	0.00	BH
ATOM	29	HB3	ALA	B	3	-4.360	-6.338	0.393	1.00	0.00	BH
ATOM	30	C	ALA	B	3	-6.187	-7.538	-1.357	1.00	0.00	BH
ATOM	31	O	ALA	B	3	-6.854	-6.553	-1.264	1.00	0.00	BH
ATOM	32	N	ALA	B	4	-6.697	-8.715	-1.643	1.00	0.00	BH
ATOM	33	HN	ALA	B	4	-6.023	-9.463	-1.751	1.00	0.00	BH
ATOM	34	CA	ALA	B	4	-8.105	-9.096	-1.934	1.00	0.00	BH
ATOM	35	HA	ALA	B	4	-8.287	-8.878	-3.003	1.00	0.00	BH
ATOM	36	CB	ALA	B	4	-8.214	-10.604	-1.704	1.00	0.00	BH
ATOM	37	HB1	ALA	B	4	-7.493	-11.205	-2.379	1.00	0.00	BH
ATOM	38	HB2	ALA	B	4	-8.016	-10.861	-0.665	1.00	0.00	BH
ATOM	39	HB3	ALA	B	4	-9.245	-10.914	-1.986	1.00	0.00	BH
ATOM	40	C	ALA	B	4	-9.226	-8.438	-1.091	1.00	0.00	BH
ATOM	41	O	ALA	B	4	-10.207	-7.958	-1.667	1.00	0.00	BH

>>> It is an ascii, fixed-format file <<<

"No connectivity information"

Checking file structures

- PDB file
- Topology file
- PSF file
- Parameter file

Parameter Optimization Strategies

Check if it has been parameterized by somebody else

Literature

Google

Minimal optimization

By analogy (i.e. direct transfer of known parameters)

Quick, starting point

Maximal optimization

Time-consuming

Requires appropriate experimental and target data

Choice based on goal of the calculations

Minimal

database screening

NMR/X-ray structure determination

Maximal

free energy calculations, mechanistic studies,
subtle environmental effects

Getting Started

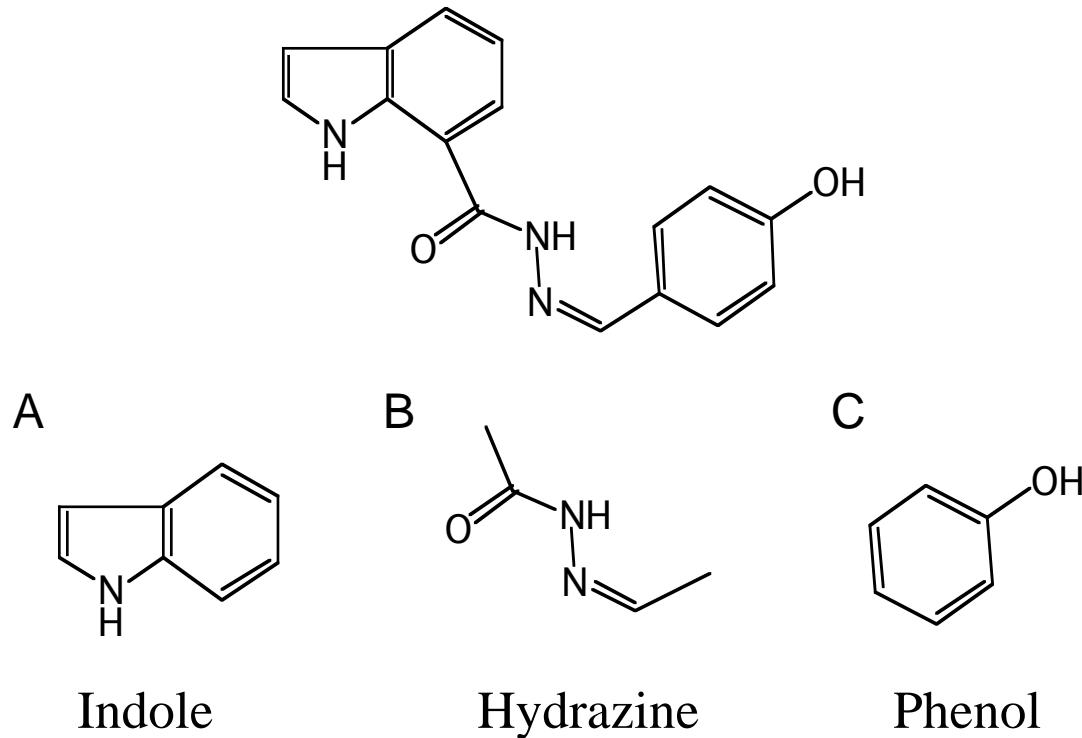
- Identify previously parameterized compounds
- Access topology information – assign atom types, connectivity, and charges – **annotate changes**

CHARMM topology (parameter files)

top_all22_model.inp (par_all22_prot.inp)
top_all22_prot.inp (par_all22_prot.inp)
top_all22_sugar.inp (par_all22_sugar.inp)
top_all27_lipid.rtf (par_all27_lipid.prm)
top_all27_na.rtf (par_all27_na.prm)
top_all27_na_lipid.rtf (par_all27_na_lipid.prm)
top_all27_prot_lipid.rtf (par_all27_prot_lipid.prm)
top_all27_prot_na.rtf (par_all27_prot_na.prm)
troph19.inp (param19.inp)

NA and lipid force fields have new LJ parameters for the alkanes, representing increased optimization of the protein alkane parameters. Tests have shown that these are compatible (e.g. in protein-nucleic acid simulations). For new systems it is suggested that the new LJ parameters be used. Note that only the LJ parameters were changed; the internal parameters are identical

Break Desired Compound into 3 Smaller Ones



When creating a covalent link between model compounds move the charge on the deleted H into the carbon to maintain integer charge
(i.e. methyl ($q_{\text{C}}=-0.27$, $q_{\text{H}}=0.09$) to methylene ($q_{\text{C}}=-0.18$, $q_{\text{H}}=0.09$))

From top_all22_model.inp

```
RESI PHEN      0.00 ! phenol, adm jr.  
GROUP  
ATOM CG   CA    -0.115 !  
ATOM HG   HP     0.115 !          HD1   HE1  
GROUP  
ATOM CD1  CA    -0.115 !          |     |  
ATOM HD1  HP     0.115 !          CD1--CE1  
ATOM //    \\  
GROUP  
ATOM CD2  CA    -0.115 !          HG--CG      CZ--OH  
ATOM HD2  HP     0.115 !          \       /       \  
ATOM CD2==CE2 HH  
GROUP  
ATOM CE1  CA    -0.115 !          |     |  
ATOM HE1  HP     0.115 !          HD2   HE2  
ATOM HE2  HP     0.115  
GROUP  
ATOM CZ   CA     0.110  
ATOM OH   OH1    -0.540  
ATOM HH   H      0.430  
BOND CD2 CG CE1 CD1 CZ CE2 CG HG CD1 HD1  
BOND CD2 HD2 CE1 HE1 CE2 HE2 CZ OH OH HH  
DOUBLE CD1 CG CE2 CD2 CZ CE1
```

Top_all22_model.inp contains all protein model compounds. Lipid, nucleic acid and carbohydrate model compounds are in the full topology files.

HG will ultimately be deleted. Therefore, move HG (hydrogen) charge into CG, such that the CG charge becomes 0.00 in the final compound.

Use remaining charges/atom types without any changes.

Do the same with indole

Creation of topology for central model compound

```
RESI Mod1 ! Model compound 1
```

```
Group
```

```
ATOM C1 CT3 -0.27
```

```
ATOM H11 HA3 0.09
```

```
ATOM H12 HA3 0.09
```

```
ATOM H13 HA3 0.09
```

```
GROUP
```

```
ATOM C2 C 0.51
```

```
ATOM O2 O -0.51
```

```
GROUP
```

```
ATOM N3 NH1 -0.47
```

```
ATOM H3 H 0.31
```

```
ATOM N4 NR1 0.16 !new atom
```

```
ATOM C5 CEL1 -0.15
```

```
ATOM H51 HEL1 0.15
```

```
ATOM C6 CT3 -0.27
```

```
ATOM H61 HA 0.09
```

```
ATOM H62 HA 0.09
```

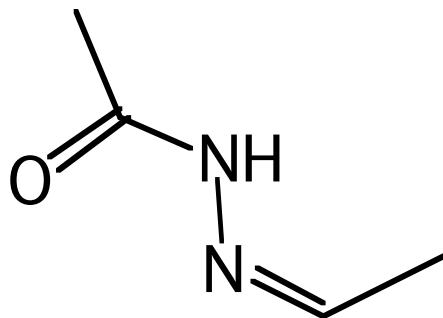
```
ATOM H63 HA 0.09
```

```
BOND C1 H11 C1 H12 C1 H13 C1 C2 C2 O2 C2 N3 N3
```

```
H3
```

```
BOND N3 N4 C5 H51 C5 C6 C6 H61 C6 H62 C6 H63
```

```
DOUBLE N4 C5 (DOUBLE only required for MMFF)
```



Start with alanine dipeptide.

Note use of new aliphatic LJ parameters and, importantly, atom types.

NR1 from histidine unprotonated ring nitrogen.
Charge (very bad) initially set to yield unit charge for the group.

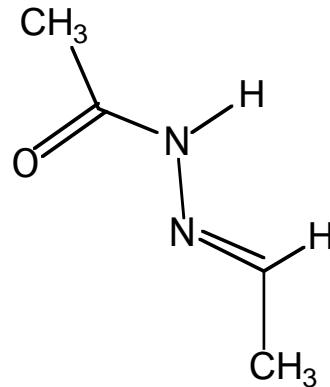
Note use of large group to allow flexibility in charge optimization.

Partial Atomic Charge Determination

Method Dependent Choices

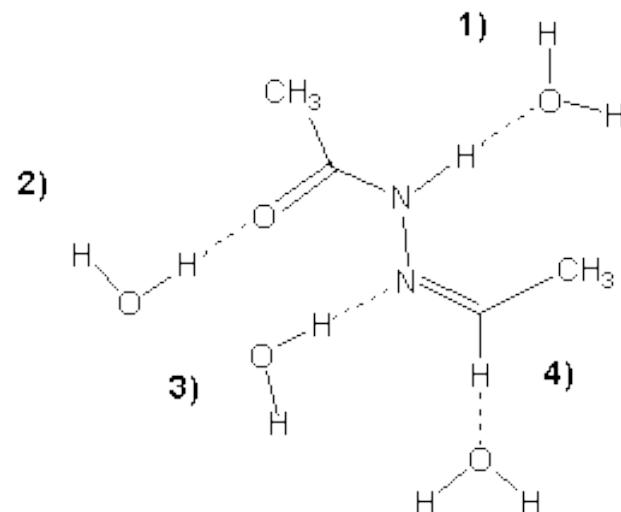
1. RESP: HF/6-31G overestimates dipole moments (AMBER)
2. Interaction based optimization (CHARMM)

For a particular force field do NOT change the QM level of theory. This is necessary to maintain consistency with the remainder of the force field.



Starting charges??
Mulliken population analysis
Analogy comparison

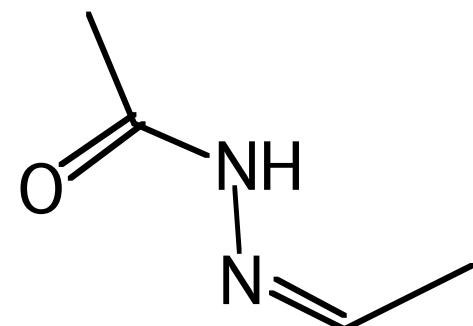
Final charges (methyl, vary q_C to maintain integer charge, $q_H = 0.09$)
interactions with water (HF/6-31G*, monohydrates!)



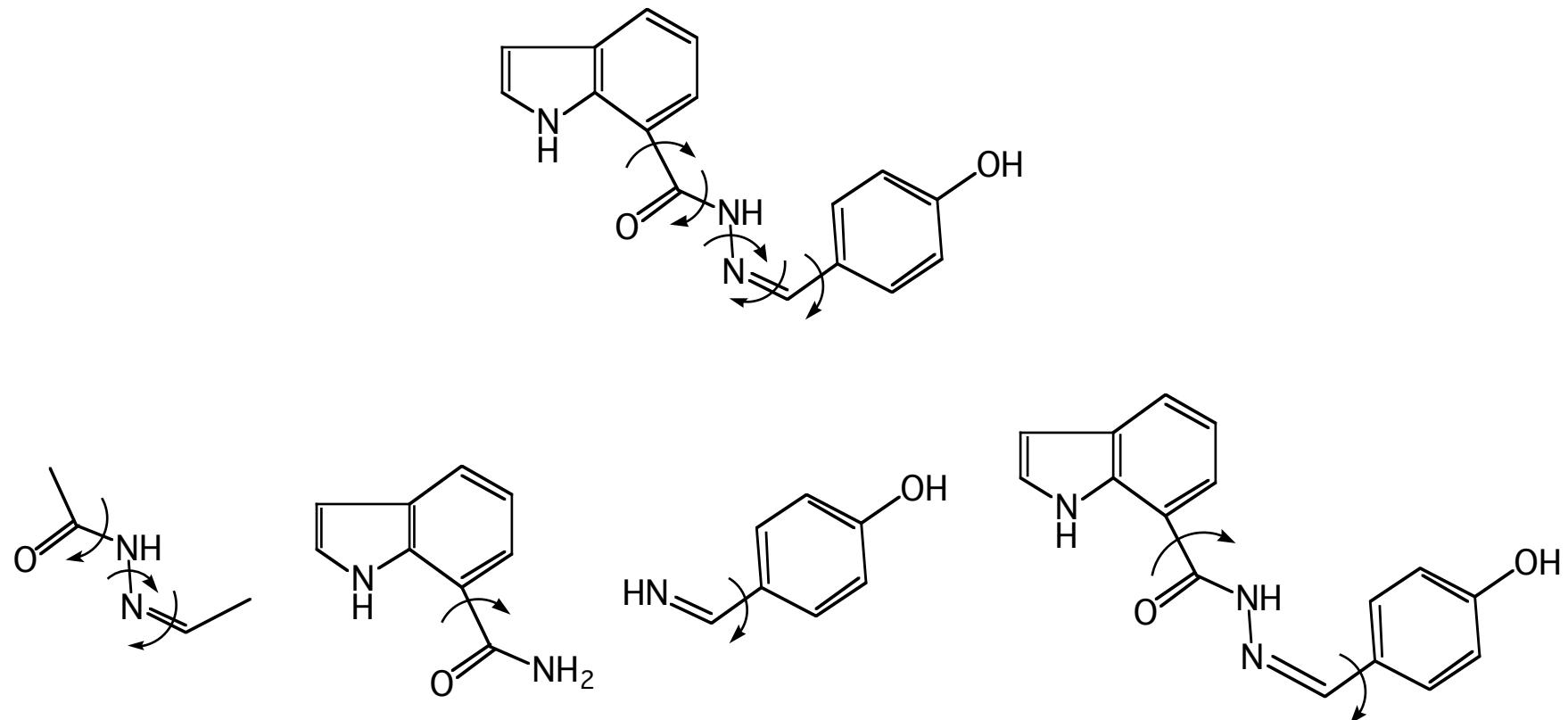
From MacKerell

Comparison of analogy and optimized charges

Name	Type	Analogy	Optimized
C1	CT3	-0.27	-0.27
H11	HA3	0.09	0.09
H12	HA3	0.09	0.09
H13	HA3	0.09	0.09
C2	C	0.51	0.58
O2	O	-0.51	-0.50
N3	NH1	-0.47	-0.32
H3	H	0.31	0.33
N4	NR1	0.16	-0.31
C5	CEL1	-0.15	-0.25
H51	HEL1	0.15	0.29
C6	CT3	-0.27	-0.09
H61	HA	0.09	0.09
H62	HA	0.09	0.09
H63	HA	0.09	0.09



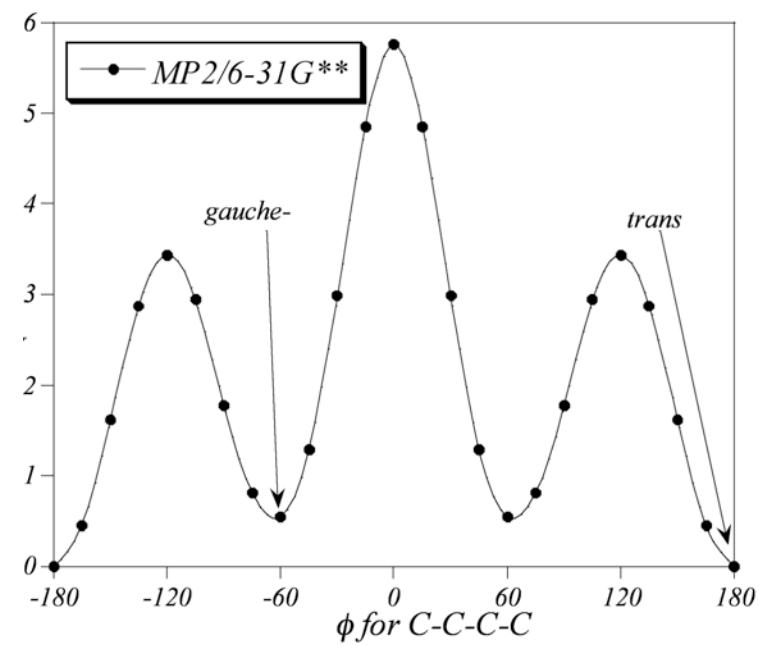
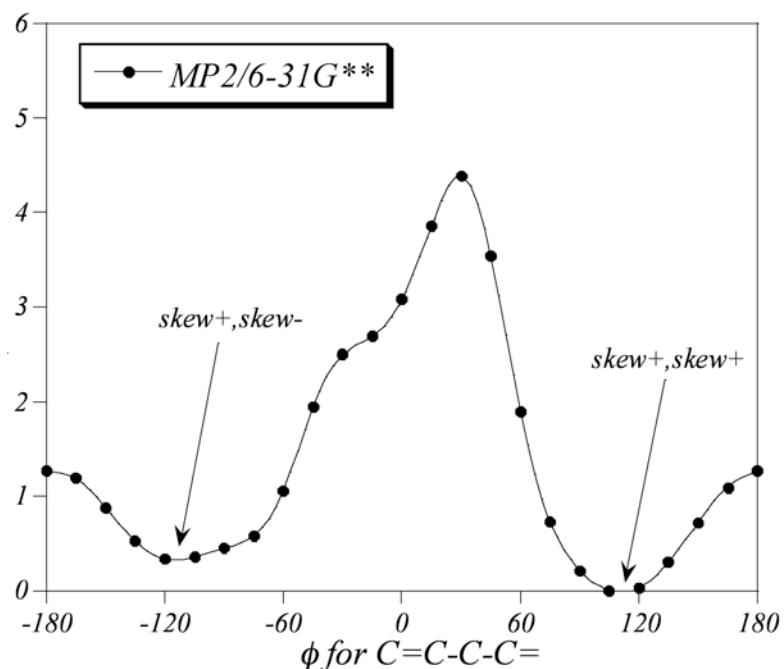
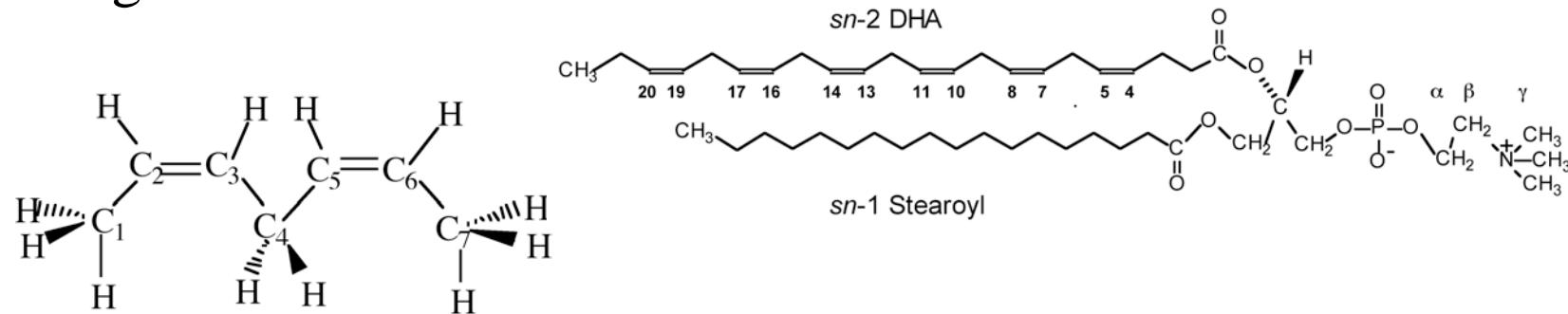
Dihedral optimization based on QM potential energy surfaces (HF/6-31G* or MP2/6-31G*).



From MacKerell

Parameterization of unsaturated lipids

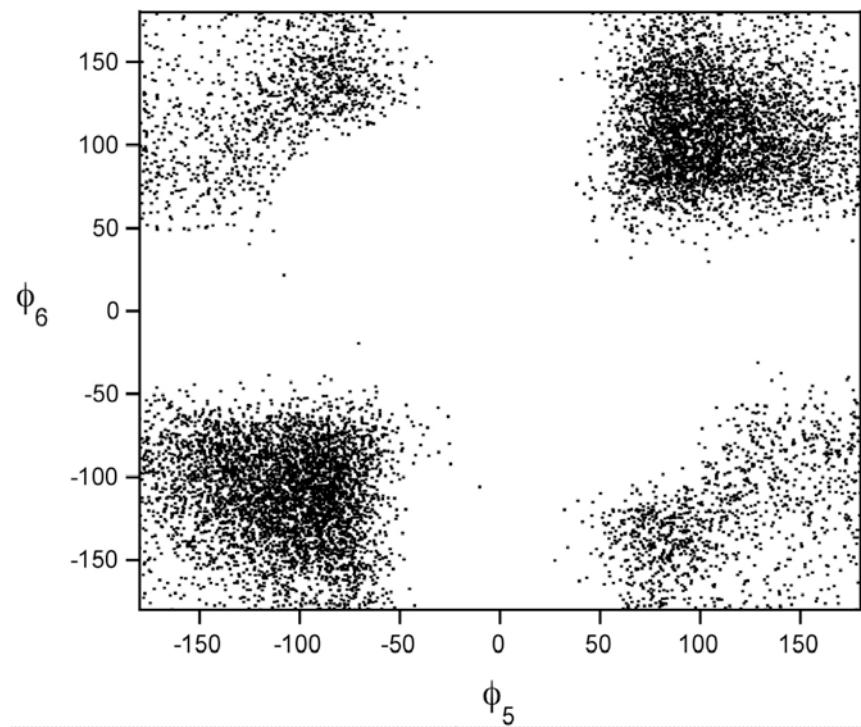
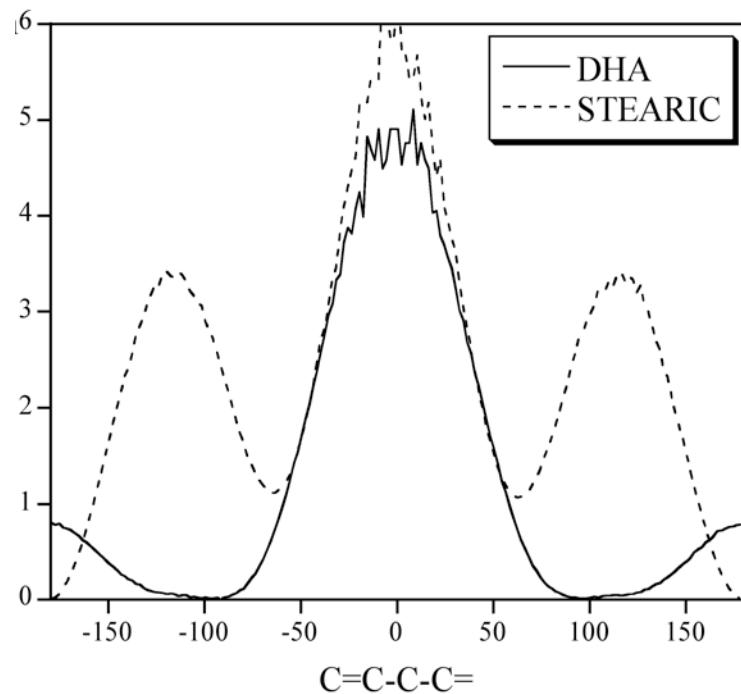
- All C=C bonds are cis, what does rotation about neighboring single bonds look like?



Courtesy of Scott Feller, Wabash College

DHA conformations from MD

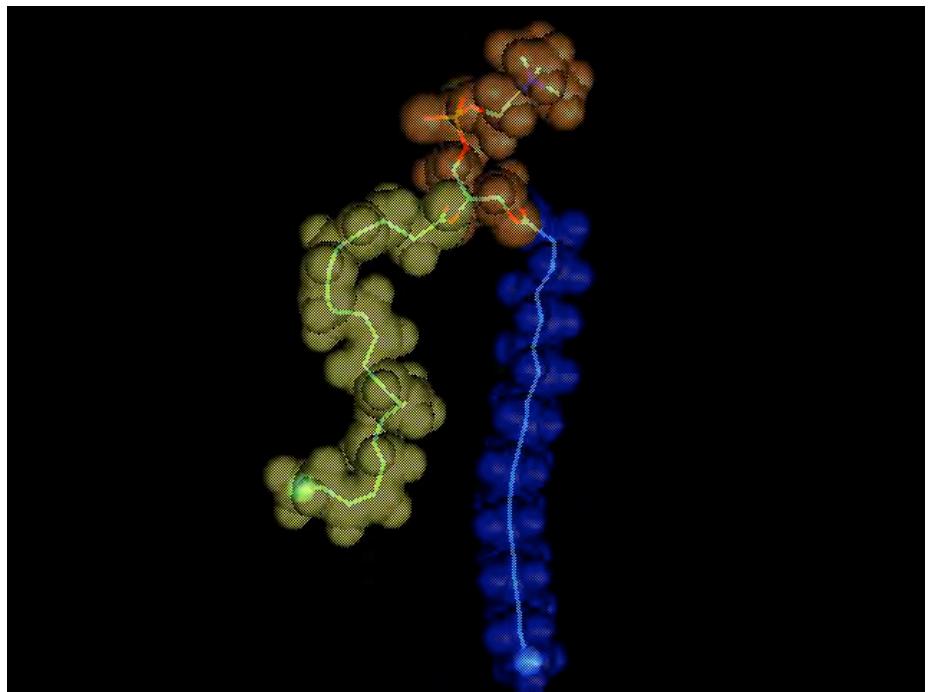
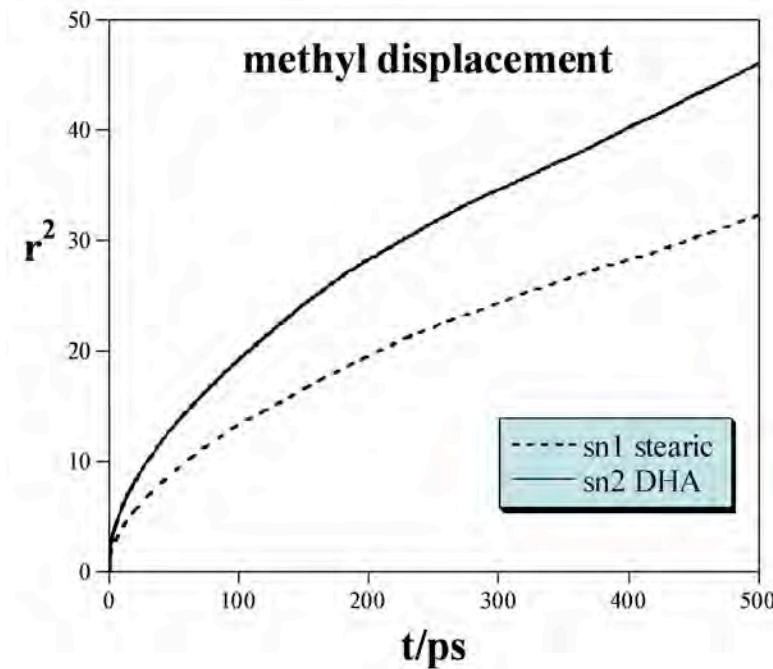
- rotational barriers are extremely small
- many conformers are accessible w/ short lifetimes



Courtesy of Scott Feller, Wabash College

Dynamics of saturated vs. polyunsaturated lipid chains

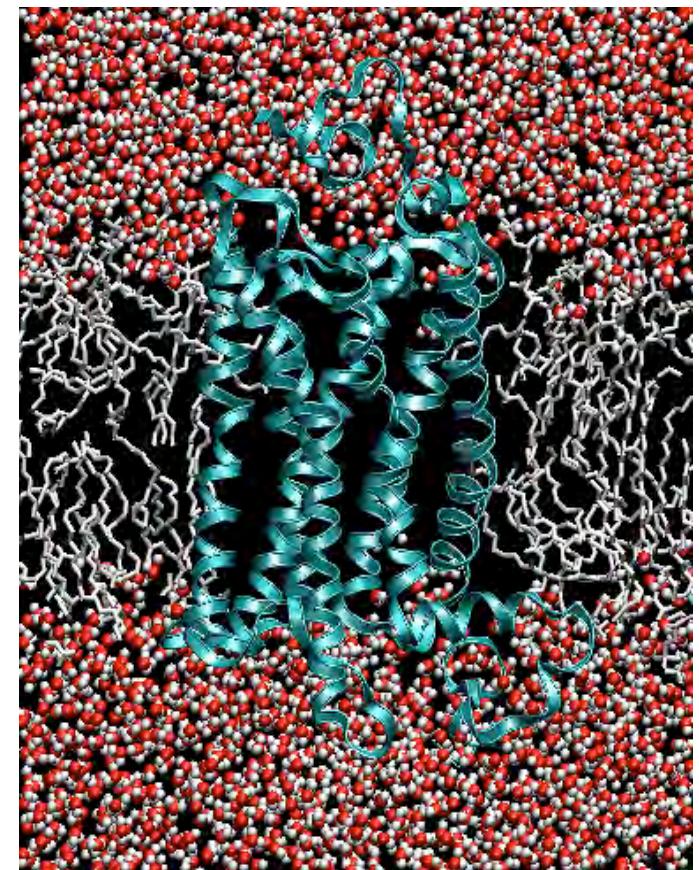
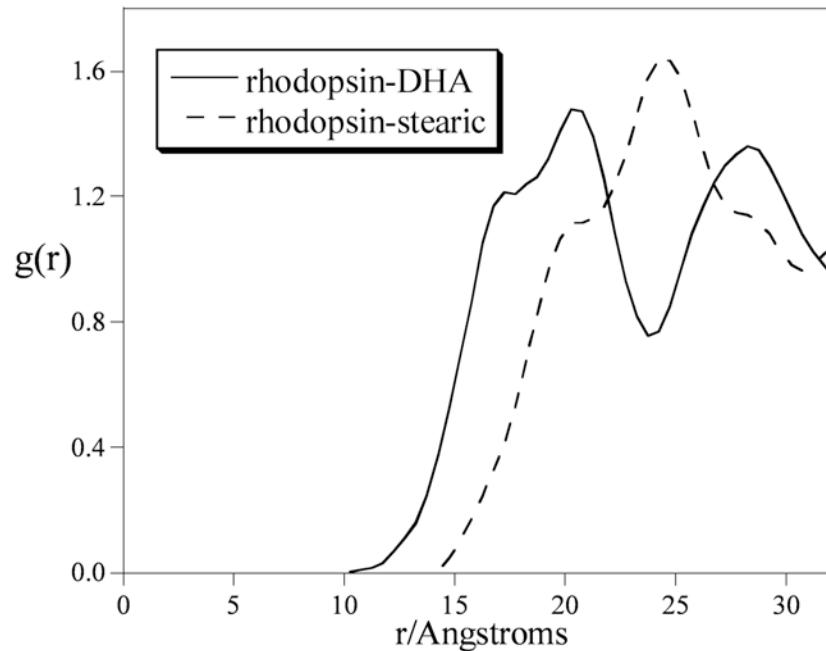
- $sn1$ stearic acid = blue
- $sn2$ DHA = yellow
- 500 ps of dynamics



Movie courtesy of Mauricio Carrillo Tripp

Lipid-protein interactions

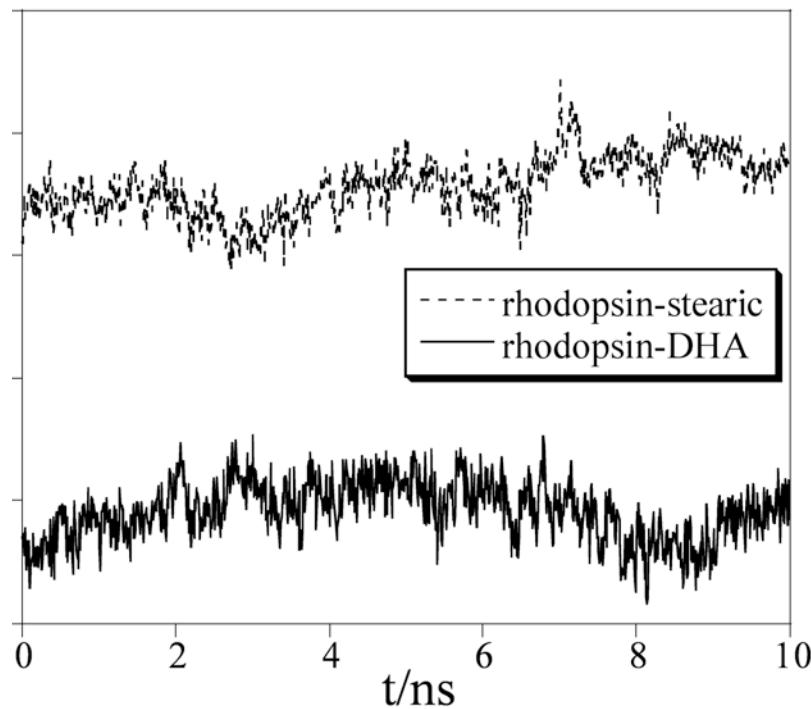
- Radial distribution around protein shows distinct layering of acyl chains



Courtesy of Scott Feller, Wabash College

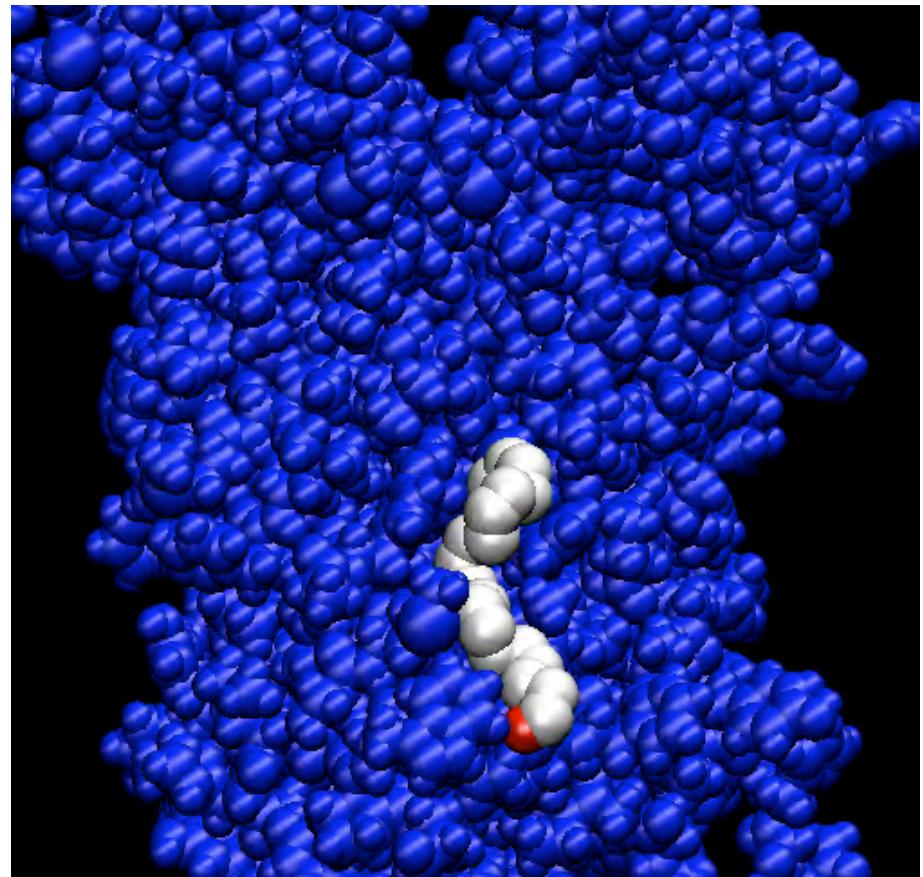
Lipid-protein interactions

- Decomposition of non-bonded interaction shows rhodopsin is strongly attracted to unsaturated chain
- All hydrophobic residues are stabilized by DHA



<u>resname</u>	U_{DHA}	$U_{stearic}$	<u>ratio</u>
PHE	-44.9	-22.6	2.0
ILE	-30.0	-10.1	3.0
VAL	-24.0	-9.6	2.5
LEU	-23.1	-13.0	1.8
MET	-22.8	-9.7	2.4
TYR	-18.6	-10.4	1.8
ALA	-11.4	-3.0	3.8
TRP	-10.3	-2.4	4.2

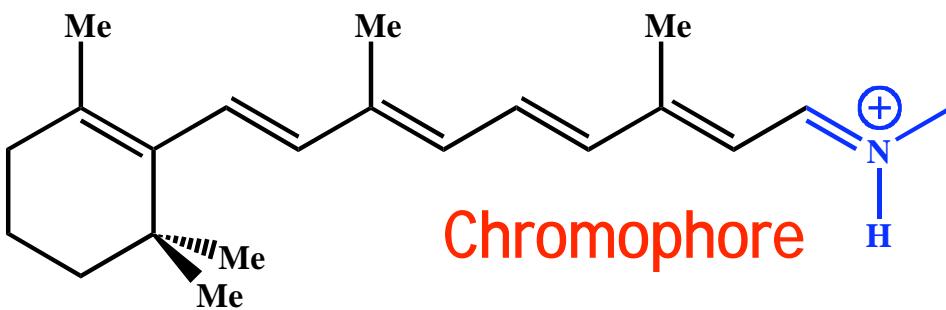
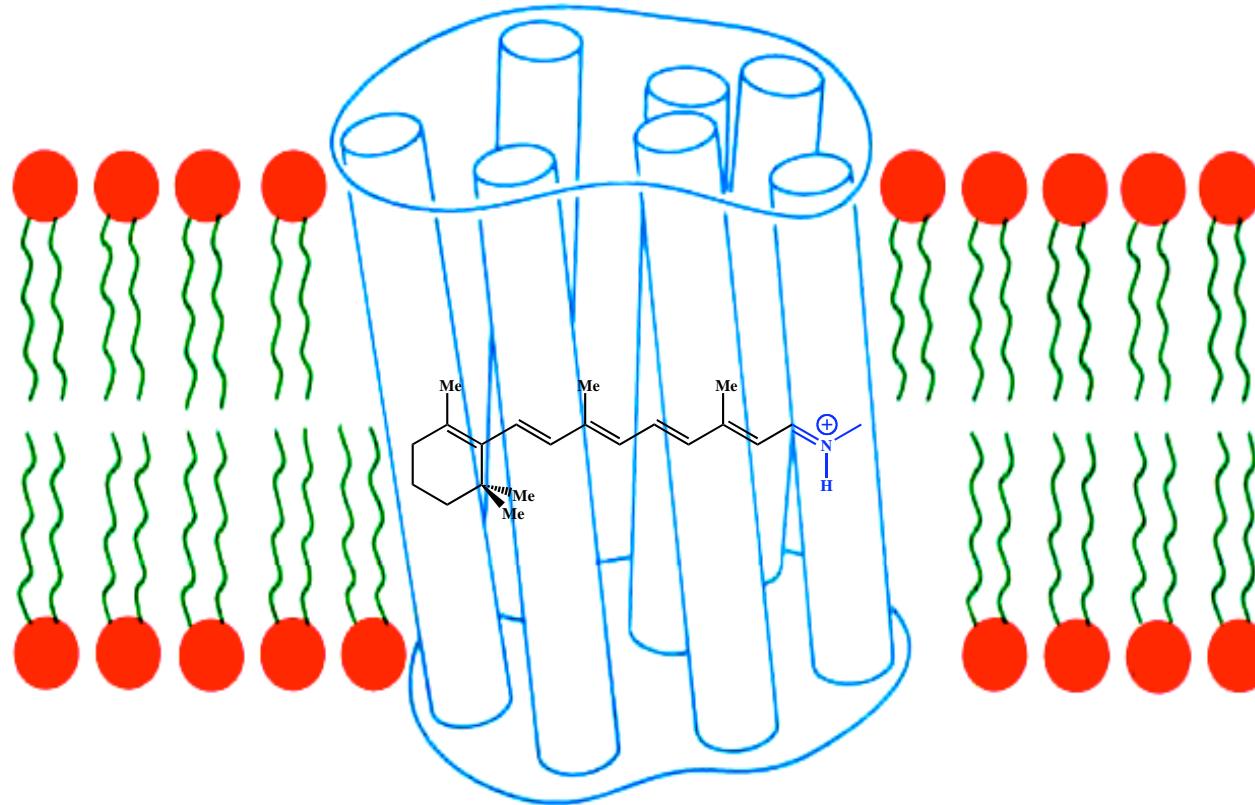
Origin of protein:DHA attraction



- Flexibility of the DHA chain allows solvation of the rough protein surface to occur with little intra-molecular energy cost

Courtesy of Scott Feller, Wabash College

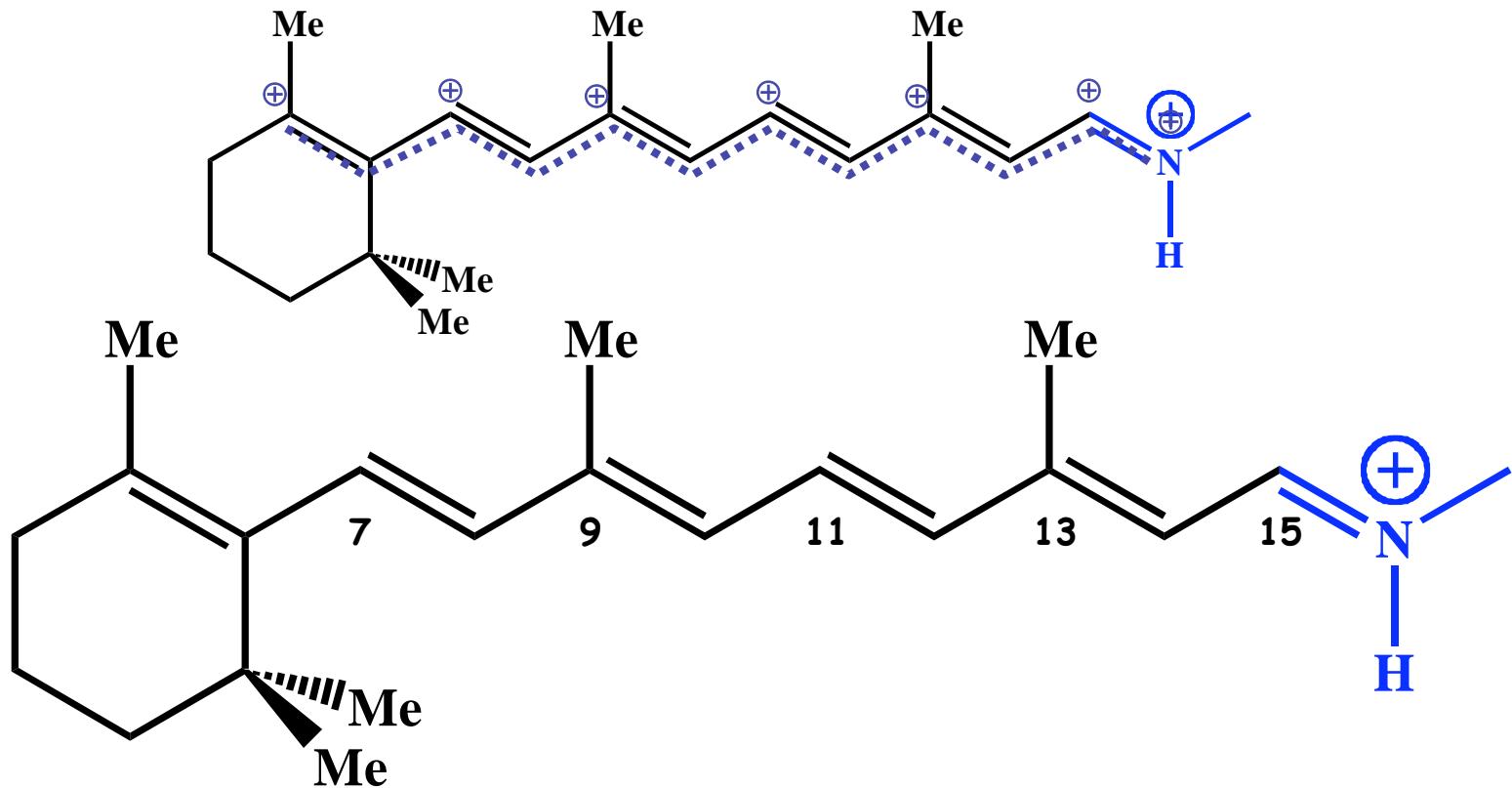
Retinal Proteins -- Rhodopsins



Chromophore

- Covalently linked to a lysine
- Usually protonated *Schiff base*
- *all-trans* and *11-cis* isomers

Unconventional chemistry



Isomerization Barriers in retinal

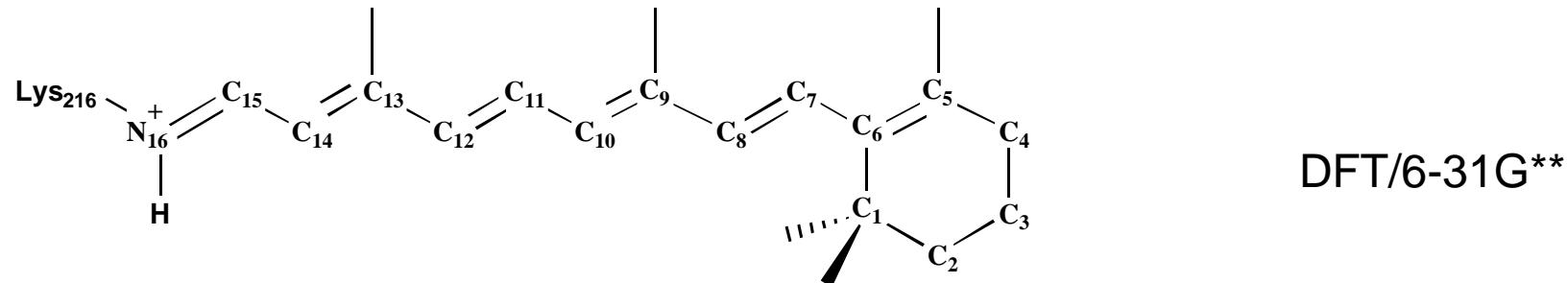


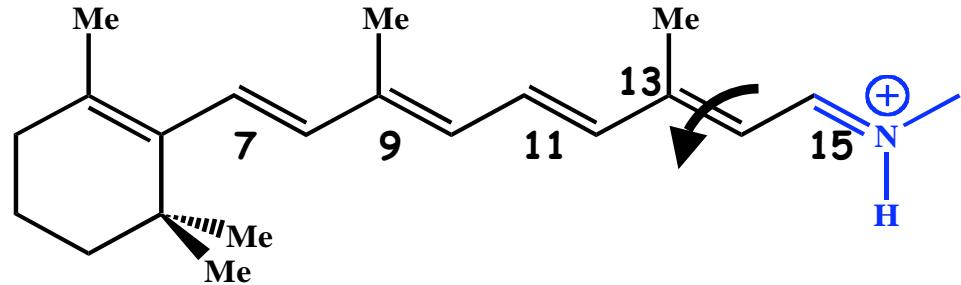
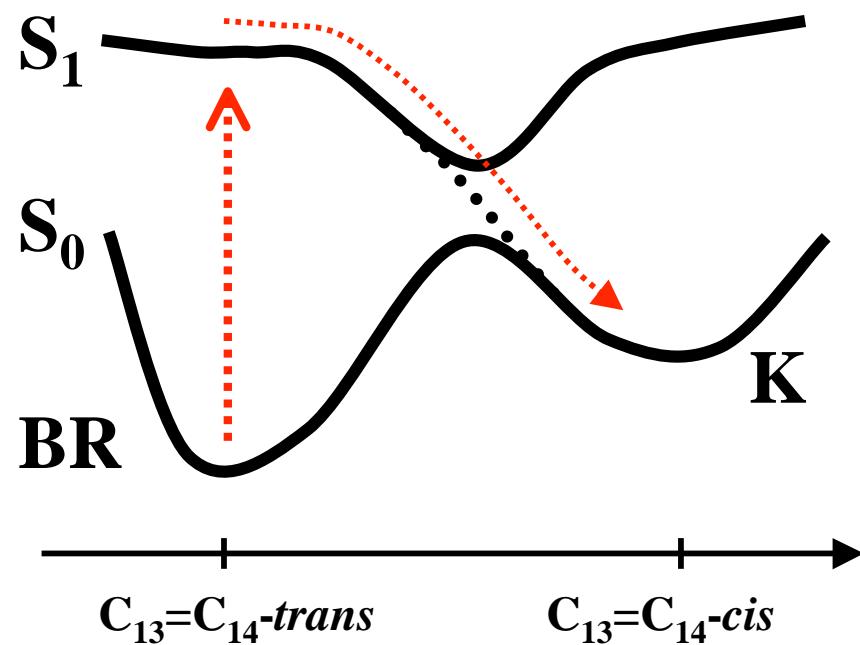
TABLE 2 The parameter set B used for the torsional potentials of the main polyene chain of the retinal Schiff base

ϕ_i	k_i (kcal/mol)*	n_i	δ_i (deg)
C ₅ =C ₆ —C ₇ =C ₈	11.24	2.0	180.00
C ₆ —C ₇ =C ₈ —C ₉	39.98	2.0	180.00
C ₇ =C ₈ —C ₉ =C ₁₀	17.03	2.0	180.00
C ₈ —C ₉ =C ₁₀ —C ₁₁	37.28	2.0	180.00
C ₉ =C ₁₀ —C ₁₁ =C ₁₂	22.50	2.0	180.00
C ₁₀ —C ₁₁ =C ₁₂ —C ₁₃	35.08	2.0	180.00
C ₁₁ =C ₁₂ —C ₁₃ =C ₁₄	28.30	2.0	180.00
C ₁₂ —C ₁₃ =C ₁₄ —C ₁₅	29.46	2.0	180.00
C ₁₃ =C ₁₄ —C ₁₅ =N ₁₆	30.43	2.0	180.00
C ₁₄ —C ₁₅ =N ₁₆ —C _s	28.76	2.0	180.00

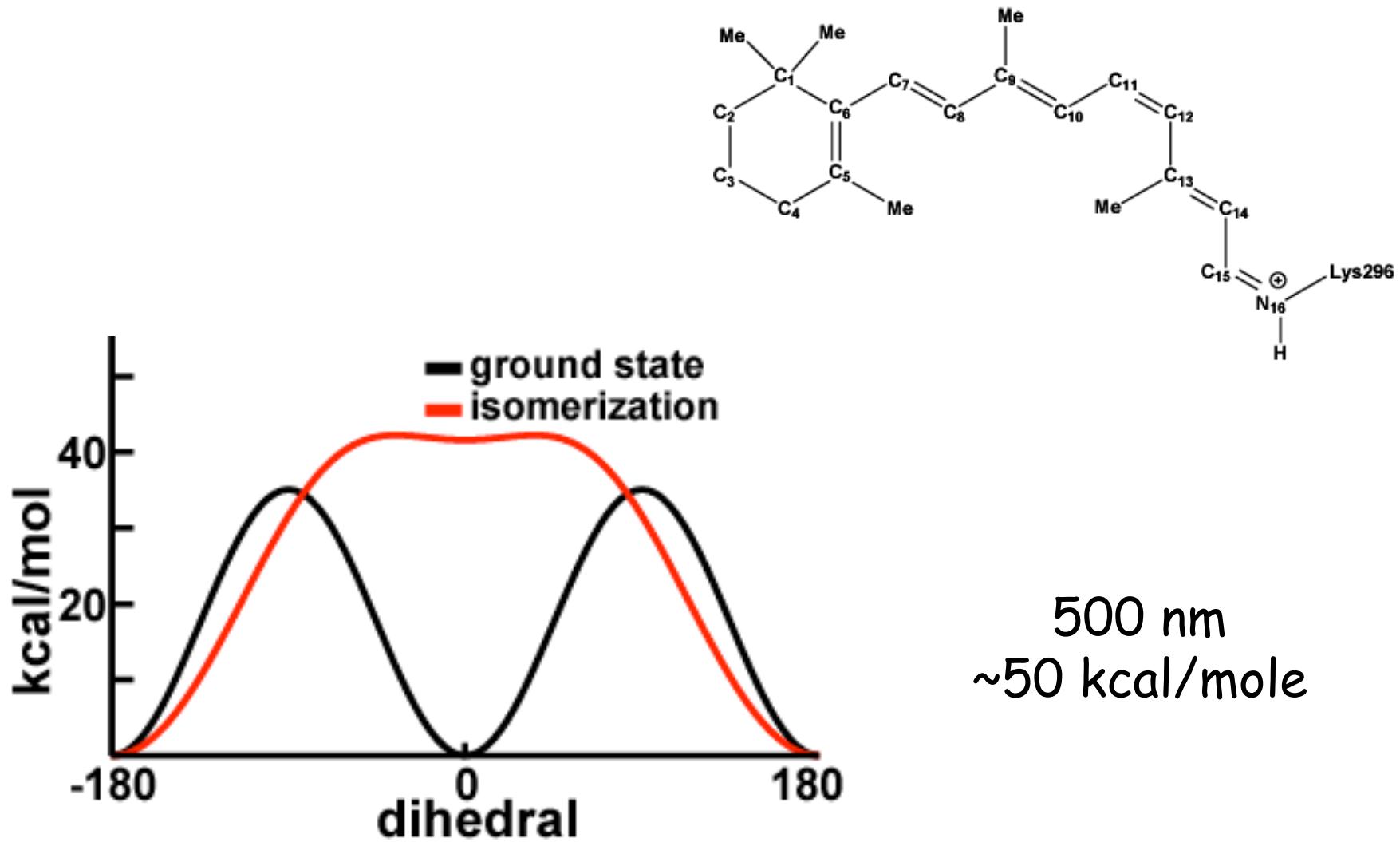
Tajkhorshid et al., 1999.

* $E_i^{\text{dihedral}} = (1/2)k_i[1 + \cos(n_i\varphi_i - \delta_i)]$.

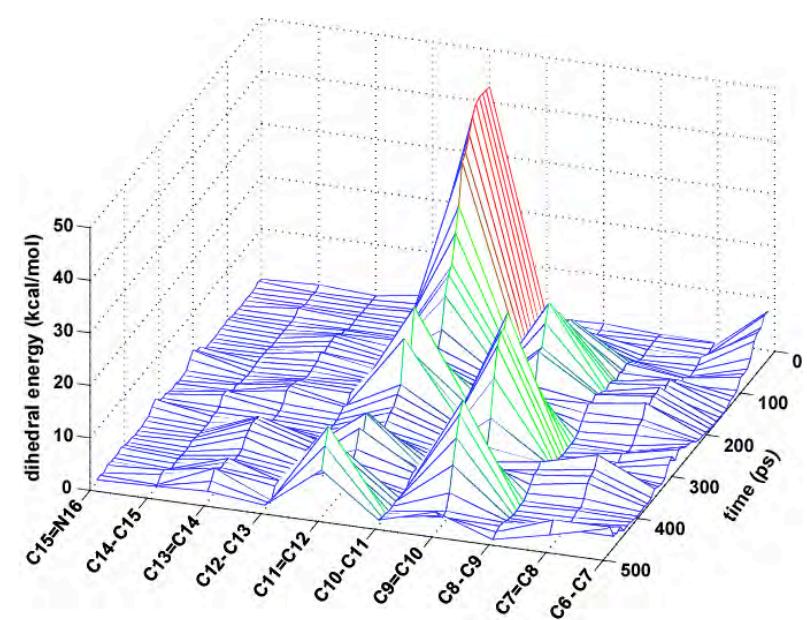
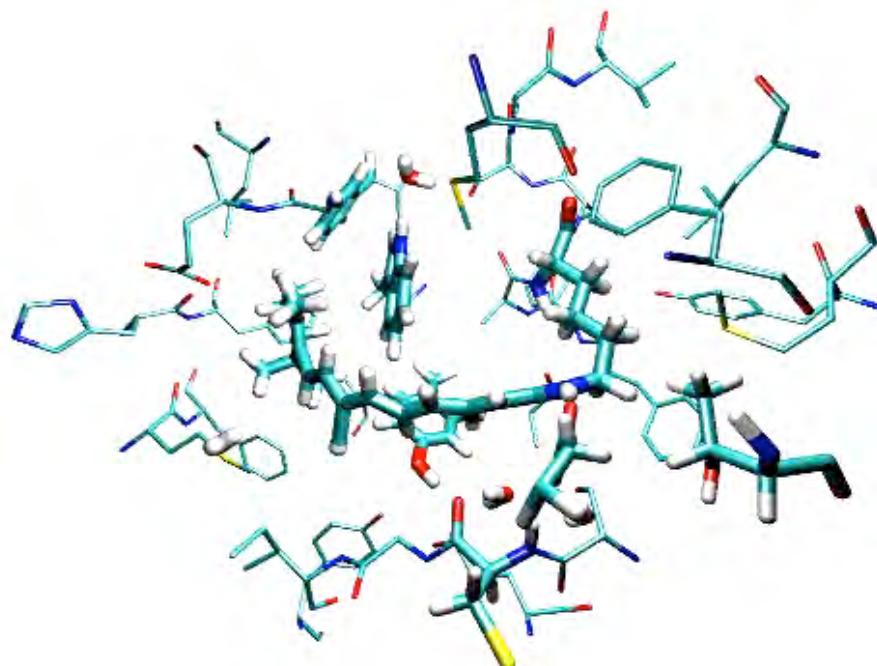
Coupling of electronic excitation and conformational change in bR



Inducing isomerization

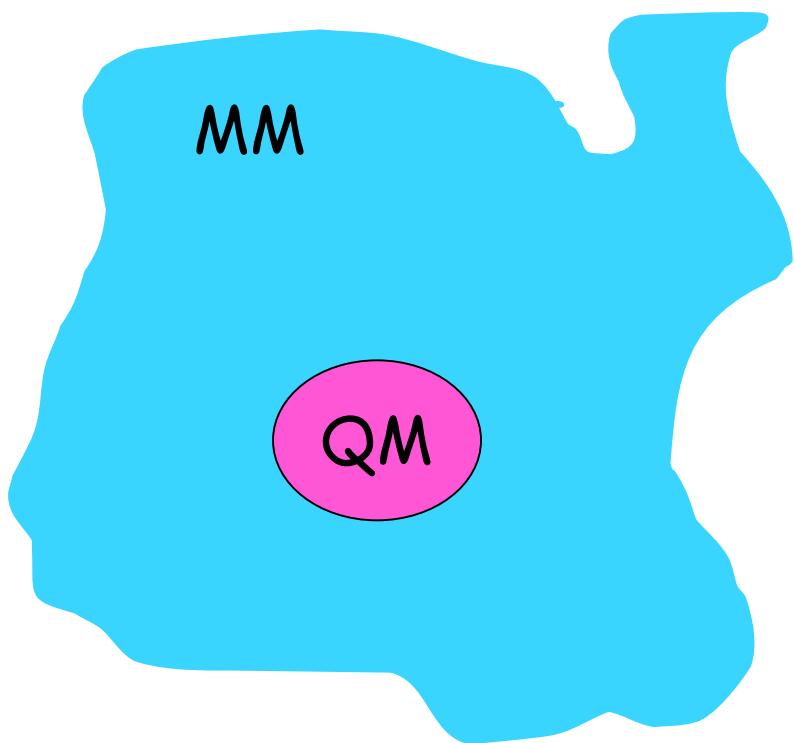


Classical Retinal Isomerization in Rhodopsin



Twist Propagation

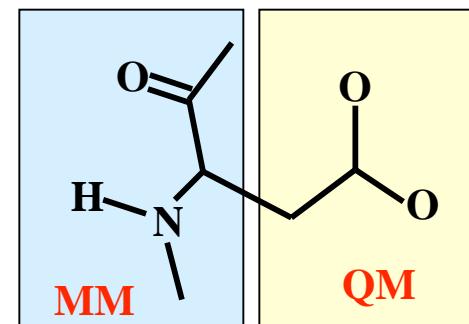
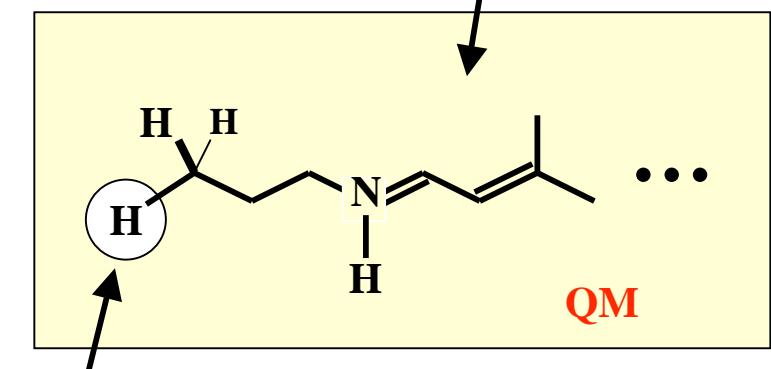
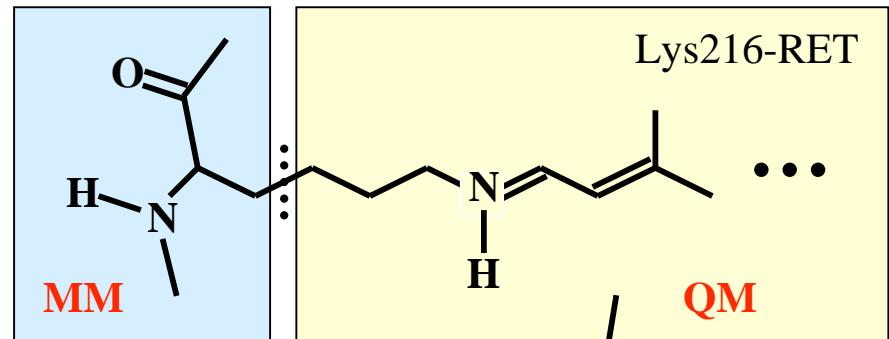
QM/MM calculations



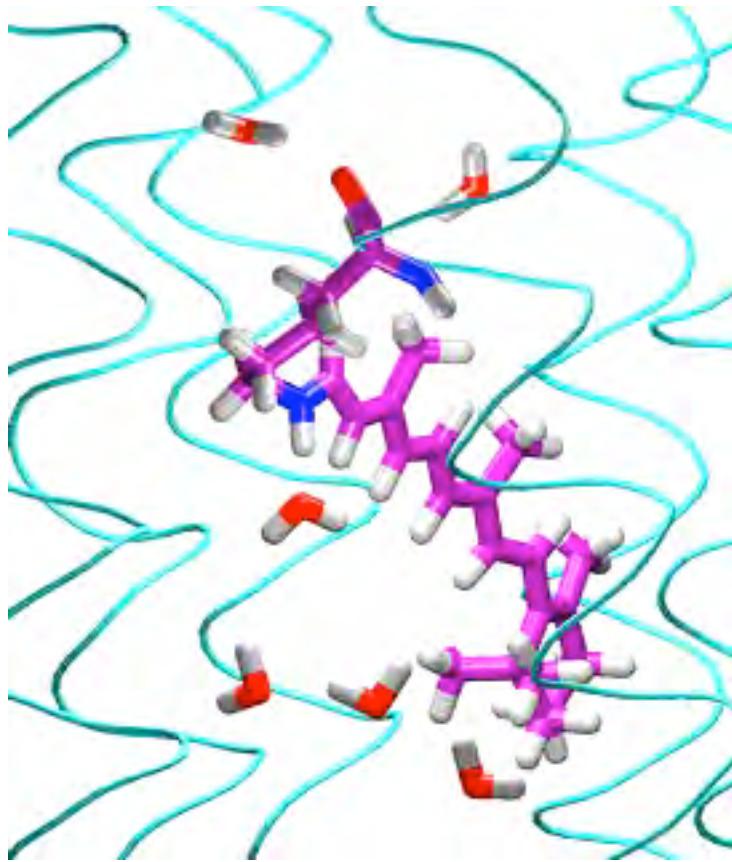
$$\hat{H} = \sum_i \frac{1}{2} p_i^2 + \sum_i \sum_A \frac{Z_A}{r_{iA}} + \sum_{i>j} \frac{1}{r_{ij}} + \sum_{A>B} \frac{Z_A Z_B}{r_{AB}}$$

$$+ \sum_i \sum_p \frac{q_p}{r_{ip}} + \sum_A \sum_p \frac{Z_A q_p}{r_{Ap}}$$

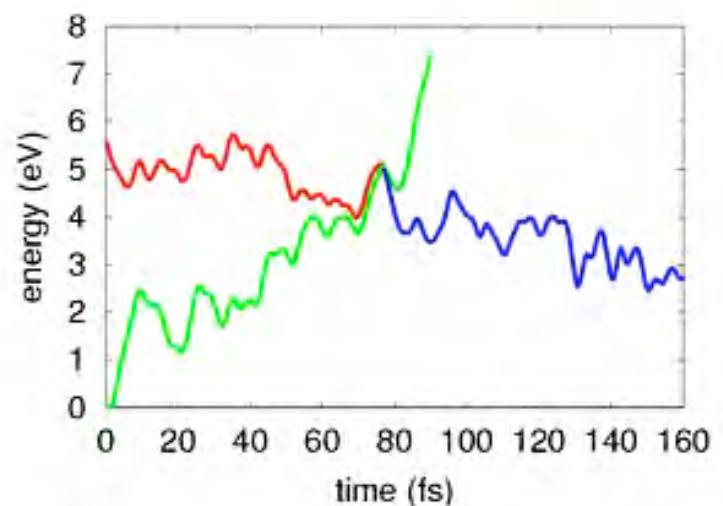
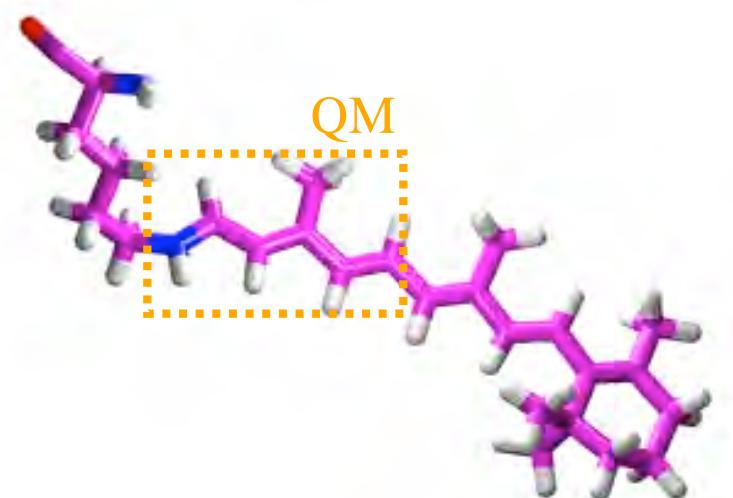
$$+ V_{QM-MM}^{MM} + V_{MM}^{MM}$$



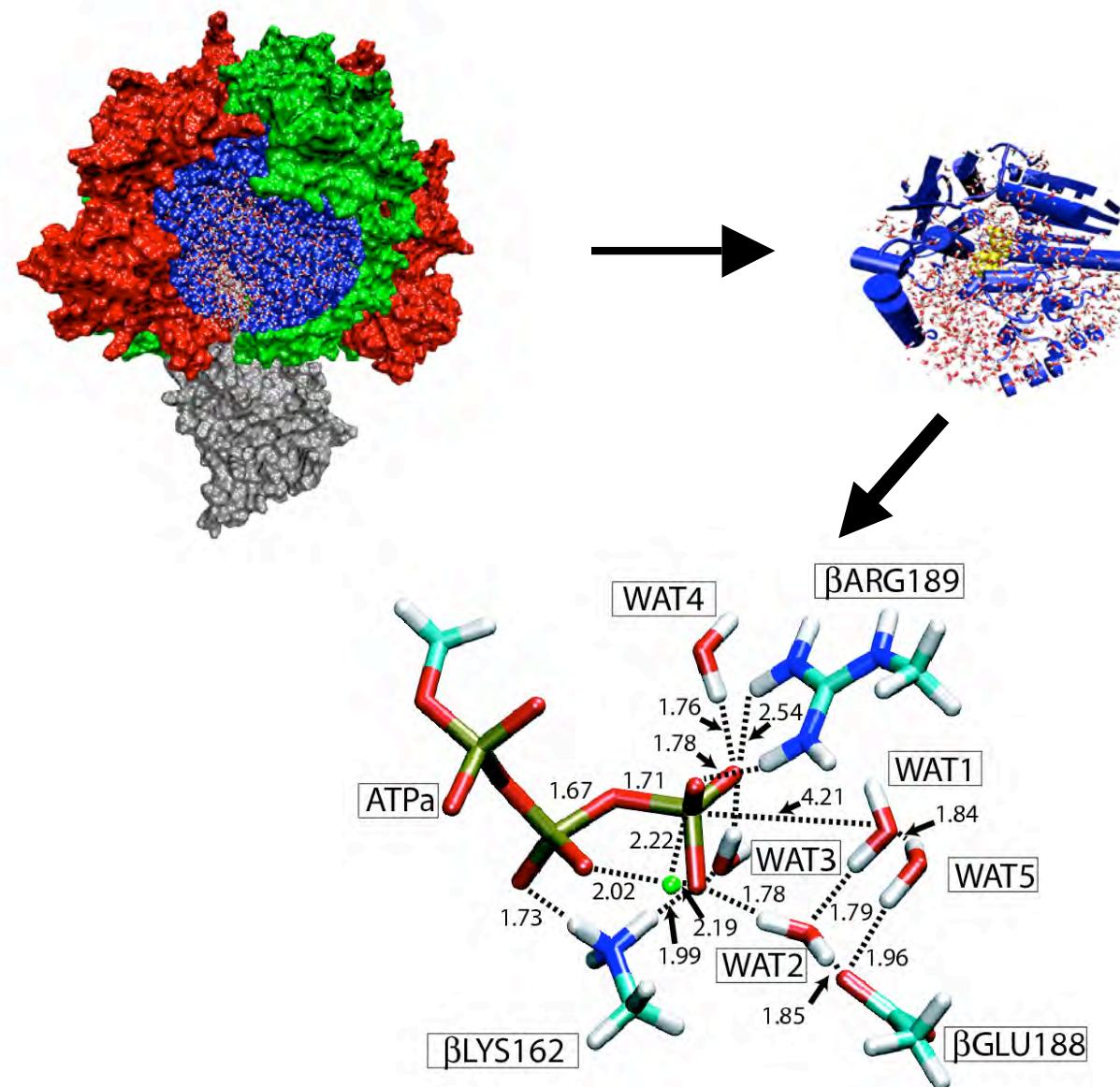
Ab Initio QM/MM Excited State MD Simulation



Quantum mechanical (QM)
treatment of the chromophore,
and force field (MM) treatment
of the embedding protein



QM/MM calculation of ATP hydrolysis



Coarse grain modeling of lipids

150 particles



9 particles!

(A)

