### Programming for Hybrid Architectures Today and in the Future

#### John E. Stone

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> LSU Third Annual HPC User Symposium Louisiana State University, June 5, 2014

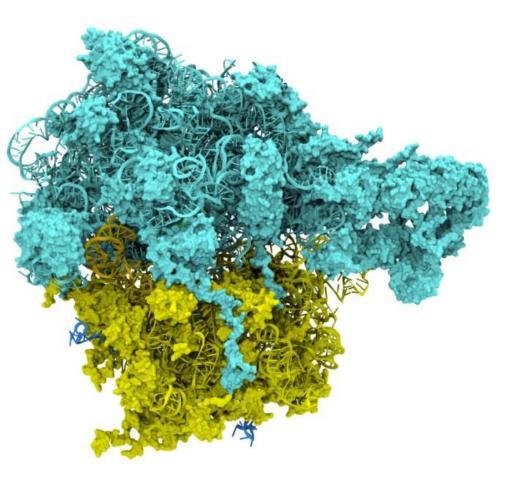


NIH BTRC for Macromolecular Modeling and Bioinformatics http://www.ks.uiuc.edu/

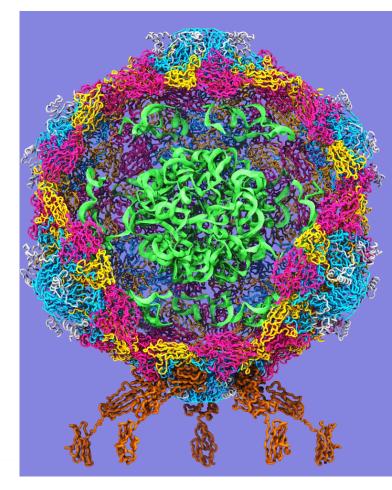
### Goal: A Computational Microscope

Study the molecular machines in living cells

Ribosome: target for antibiotics

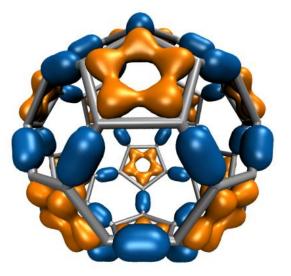


Poliovirus

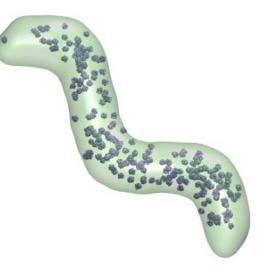


### VMD – "Visual Molecular Dynamics"

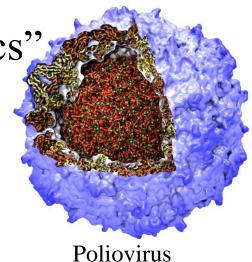
- Visualization and analysis of:
  - molecular dynamics simulations
  - quantum chemistry calculations
  - particle systems and whole cells
  - sequence data
- User extensible w/ scripting and plugins
- http://www.ks.uiuc.edu/Research/vmd/

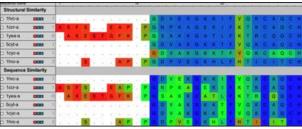


Electrons in Vibrating Buckyball



Cellular Tomography, Cryo-electron Microscopy



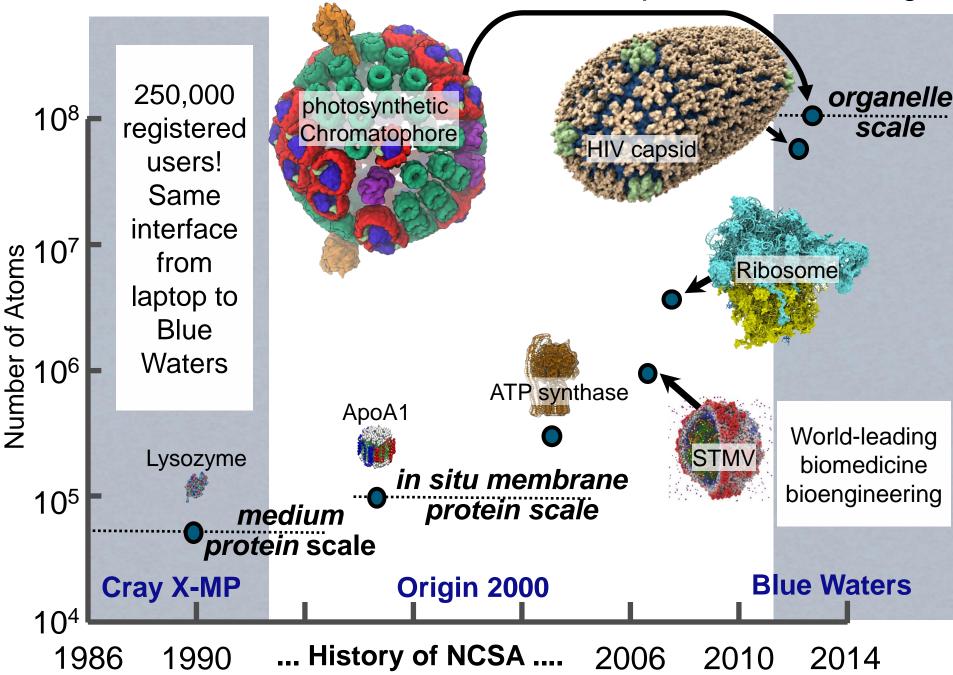


**Ribosome Sequences** 



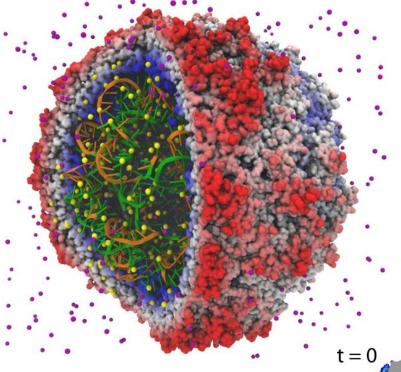
Whole Cell Simulations

#### NAMD/VMD Effort Towards Cell-scale Computational Modeling



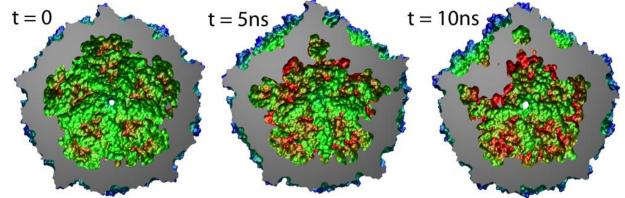
### First Simulation of a Virus Capsid (2006)

Satellite Tobacco Mosaic Virus (STMV)



- First MD simulation of a complete virus capsid
- STMV smallest available capsid structure
- STMV simulation, visualization, and analysis pushed us toward GPU computing!

MD showed that STMV capsid collapses without its RNA core



1 million atoms A huge system for 2006

Freddolino et al., Structure, 14:437 (2006)

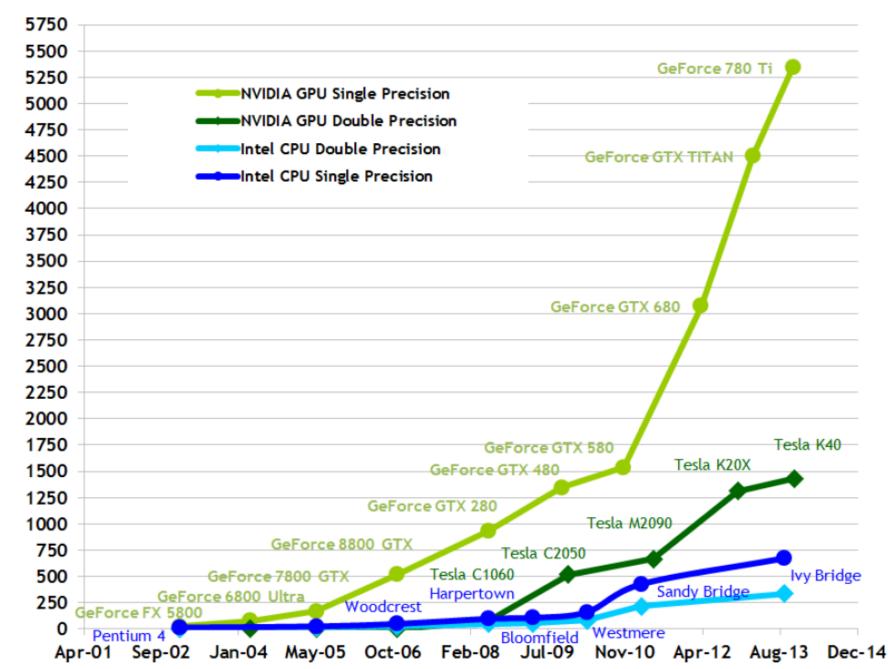
## GPU Computing

- Commodity devices, omnipresent in modern computers (over a **million** sold per **week**)
- Massively parallel hardware, hundreds of processing units, **throughput oriented architecture**
- Standard integer and floating point types supported
- Programming tools allow software to be written in dialects of familiar C/C++ and integrated into legacy software
- GPU algorithms are often multicore friendly due to attention paid to **data locality** and **data-parallel** work decomposition



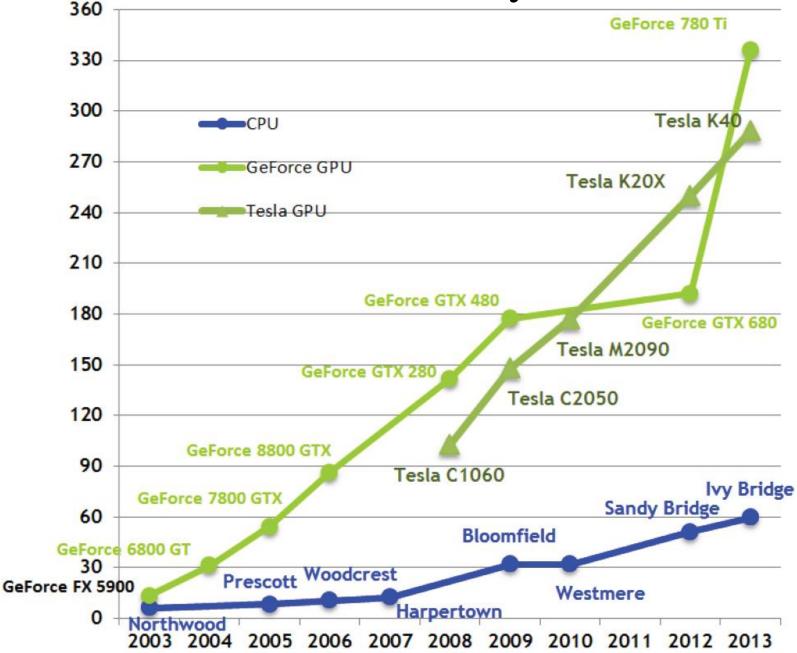
#### Theoretical GFLOP/s

#### Peak Arithmetic Performance Trend



#### Theoretical GB/s

### Peak Memory Bandwidth Trend



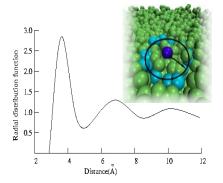
## What Speedups Can GPUs Achieve?

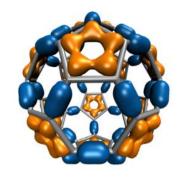
- Single-GPU speedups of 2.5x to 8x vs. one CPU socket are common
- Best speedups can reach **25x** or more, attained on codes dominated by floating point arithmetic, especially native GPU machine instructions, e.g. expf(), rsqrtf(), ...
- Amdahl's Law can prevent legacy codes from achieving peak speedups with shallow GPU acceleration efforts



### CUDA GPU-Accelerated Trajectory Analysis and Visualization in VMD

VMD GPU-Accelerated Feature or Kernel	Typical speedup vs. multi- core CPU (e.g. 4-core CPU)		
Molecular orbital display	30x		
<b>Radial distribution function</b>	23x		
Molecular surface display	15x		
Electrostatic field calculation	11x		
Ray tracing w/ shadows, AO lighting	7x		
Ion placement	6x		
MDFF density map synthesis	6x		
Implicit ligand sampling	6x		
Root mean squared fluctuation	6x		
Radius of gyration	5x		
Close contact determination	5x		
Dipole moment calculation	4x		





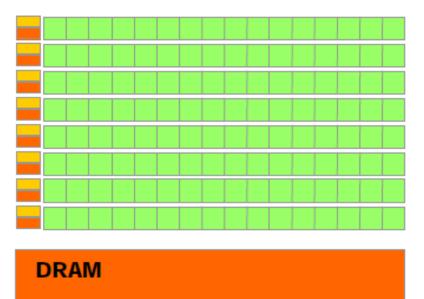


### Comparison of CPU and GPU Hardware Architecture

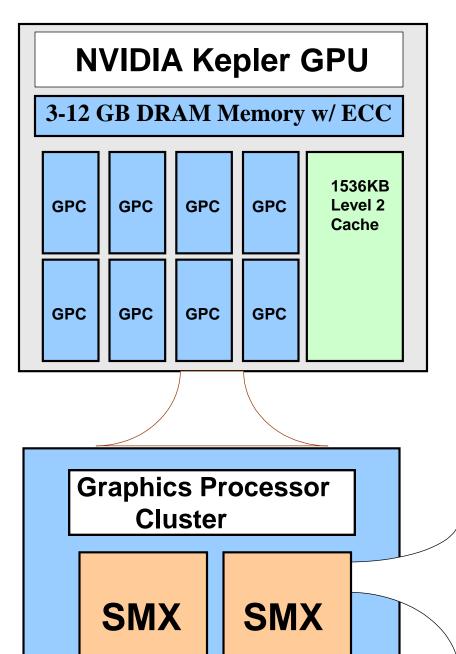
**CPU**: Cache heavy, focused on individual thread performance

Control	ALU	ALU	
	ALU	ALU	
Cache			
DRAM			

**GPU**: ALU heavy, massively parallel, throughput oriented





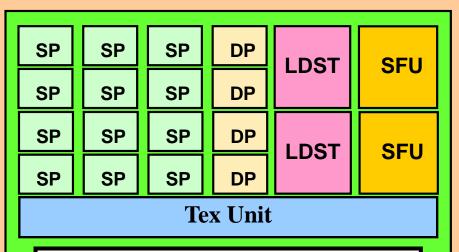


#### **Streaming Multiprocessor - SMX**

64 KB Constant Cache

64 KB L1 Cache / Shared Memory

48 KB Tex + Read-only Data Cache



16 × Execution block = 192 SP, 64 DP, 32 SFU, 32 LDST

### Hybrid Systems Lead Top500, Green500

- Four of the top ten Top500 systems are hybrid architectures
  - #1 NSCC Tianhe-2
  - #2 ORNL Titan
  - #6 CSCS Piz Daint
  - #7 TACC Stampede
- All of top ten Green500 systems are GPU-based hybrid architectures

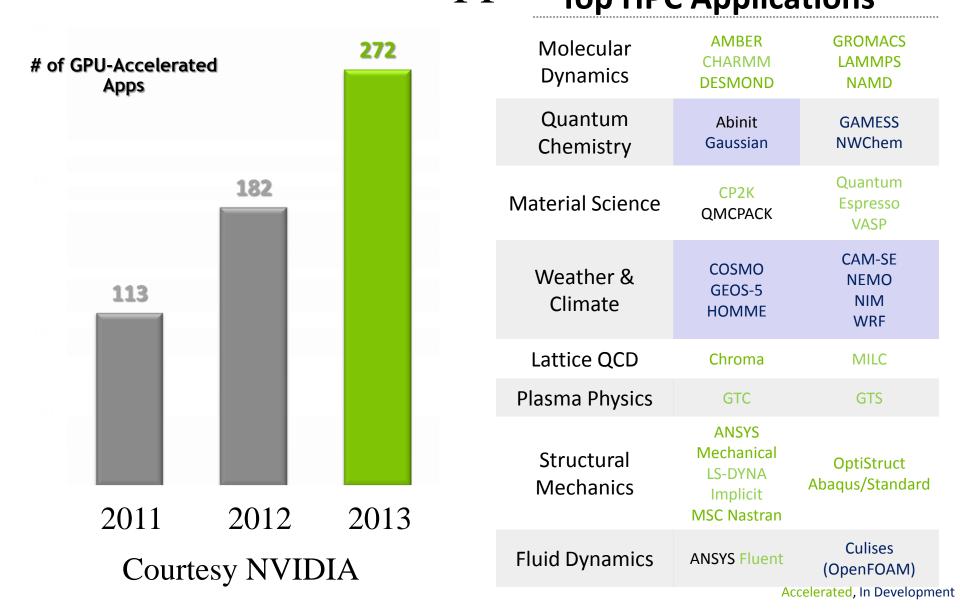


Hybrid Architectures Becoming Common for Mid-range Systems

- Upcoming LSU Cluster: ~960 GPUs
- 2013: Indiana Big Red II: ~600 GPUs
- 2012: Georgia Tech Keeneland: 792 GPUs



## Solid Growth of GPU Accelerated Apps Top HPC Applications



### Major Approaches For Programming Hybrid Architectures

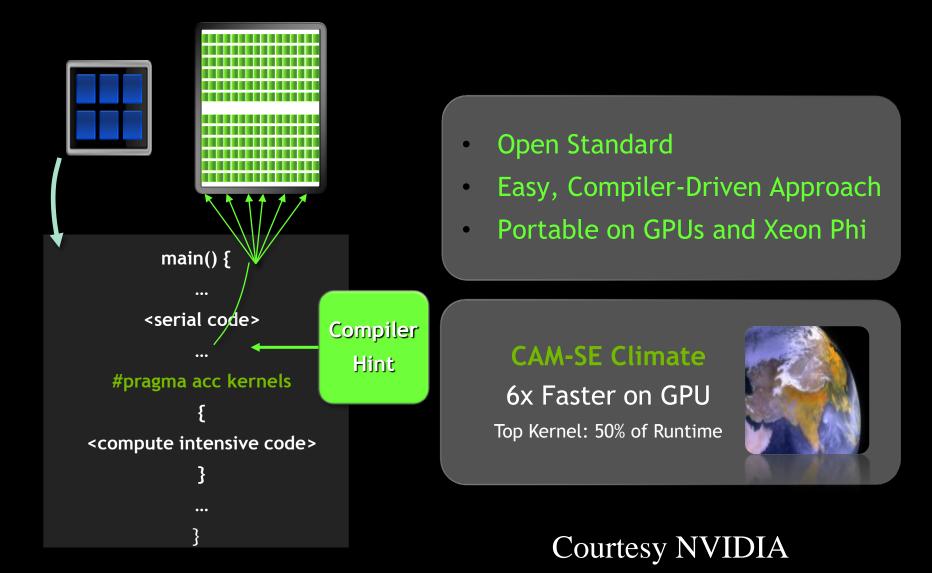
- Use drop-in libraries in place of CPU-based libraries
  - Little or no code development
  - Speedups limited by Amdahl's Law and overheads associated with data movement between CPUs and GPU accelerators
  - Examples: MAGMA, BLAS-variants, FFT libraries, etc.
- Generate accelerator code as a variant of CPU source, e.g. using OpenMP w/ OpenACC, similar methods
- Write lower-level accelerator-specific code, e.g. using CUDA, OpenCL, other approaches



#### GPU Accelerated Libraries "Drop-in" Acceleration for your Applications



### OpenACC: Open, Simple, Portable



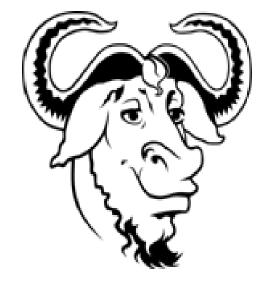
## Linux GCC Compiler to Support GPU Accelerators

#### Open Source

•GCC Efforts by Samsung & Mentor Graphics

#### Pervasive Impact

•Free to all Linux users



#### Mainstream

Most Widely Used HPC Compiler

"

Incorporating OpenACC into GCC is an excellent example of open source and open standards working together to make accelerated computing broadly accessible to all Linux developers.

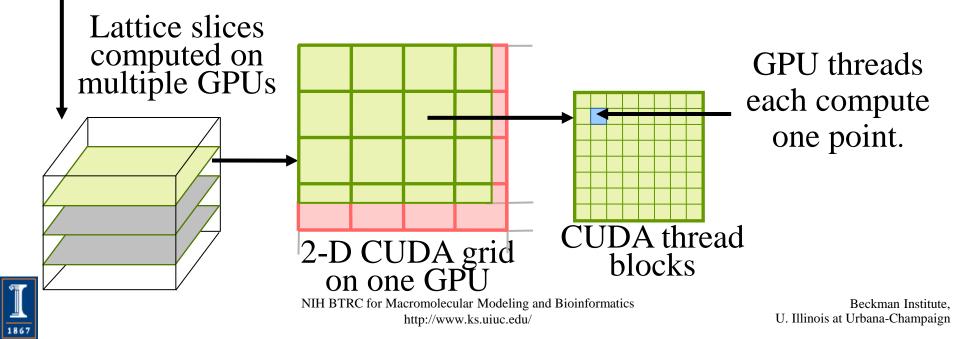


Oak Ridge National Laboratories

Oscar Hernandez

GPU Solution: Computing C<sub>60</sub> Molecular Orbitals

3-D orbital lattice: millions of points	Device	CPUs,	Runtime	Speedup
		GPUs	(s)	
	2x Intel X5550-SSE	8	4.13	1
	GeForce GTX 480	1	0.255	16
	GeForce GTX 480	4	0.081	51



#### Molecular Orbital Inner Loop, Hand-Coded x86 SSE Hard to Read, Isn't It? (And this is the "pretty" version!)

for (shell=0; shell < maxshell; shell++) {</pre>

 $\_m128 Cgto = \_mm\_setzero\_ps();$ 

for (prim=0; prim<num\_prim\_per\_shell[shell\_counter]; prim++) {</pre>

float exponent = -basis\_array[prim\_counter ];

float contract\_coeff = basis\_array[prim\_counter + 1];

\_\_m128 expval = \_mm\_mul\_ps(\_mm\_load\_ps1(&exponent), dist2);

\_\_m128 ctmp = \_mm\_mul\_ps(\_mm\_load\_ps1(&contract\_coeff), exp\_ps(expval));

Cgto = \_mm\_add\_ps(contracted\_gto, ctmp);

prim\_counter += 2;

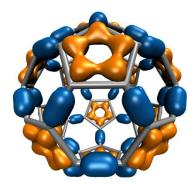
}

\_\_m128 tshell = \_mm\_setzero\_ps();
switch (shell\_types[shell\_counter]) {
 case S\_SHELL:

Writing SSE kernels for CPUs requires assembly language, compiler intrinsics, various libraries, or a really smart autovectorizing compiler **and lots of luck...** 

value = \_mm\_add\_ps(value, \_mm\_mul\_ps(\_mm\_load\_ps1(&wave\_f[ifunc++]), Cgto)); break; case P\_SHELL:

tshell = \_mm\_add\_ps(tshell, \_mm\_mul\_ps(\_mm\_load\_ps1(&wave\_f[ifunc++]), xdist)); tshell = \_mm\_add\_ps(tshell, \_mm\_mul\_ps(\_mm\_load\_ps1(&wave\_f[ifunc++]), ydist)); tshell = \_mm\_add\_ps(tshell, \_mm\_mul\_ps(\_mm\_load\_ps1(&wave\_f[ifunc++]), zdist)); value = \_mm\_add\_ps(value, \_mm\_mul\_ps(tshell, Cgto)); break;



### **Molecular Orbital Inner Loop in CUDA**

```
for (shell=0; shell < maxshell; shell++) {</pre>
```

```
float contracted_gto = 0.0f;
```

for (prim=0; prim<num\_prim\_per\_shell[shell\_counter]; prim++) {</pre>

float exponent = const\_basis\_array[prim\_counter ];

float contract\_coeff = const\_basis\_array[prim\_counter + 1];

contracted\_gto += contract\_coeff \* exp2f(-exponent\*dist2);

prim\_counter += 2;

float tmpshell=0;

```
switch (const_shell_symmetry[shell_counter]) {
  case S_SHELL:
```

```
value += const_wave_f[ifunc++] * contracted_gto; break;
```

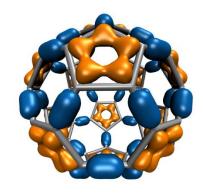
```
case P_SHELL:
```

```
tmpshell += const_wave_f[ifunc++] * xdist;
```

```
tmpshell += const_wave_f[ifunc++] * ydist
```

```
tmpshell += const_wave_f[ifunc++] * zdist;
```

value += tmpshell \* contracted\_gto; break;



#### Aaaaahhhh....

Data-parallel CUDA kernel looks like normal C code for the most part....

## GPU On-Board Global Memory

- GPU arithmetic rates dwarf memory bandwidth
- For Kepler K40 hardware:
  - ~4.3 SP TFLOPS vs. ~288 GB/sec
  - The ratio is roughly 60 FLOPS per memory reference for single-precision floating point
- Peak performance achieved with "coalesced" memory access patterns – patterns that result in a single hardware memory transaction for a SIMD "warp" – a contiguous group of 32 threads



### Getting Performance From GPUs

- Don't worry (much) about counting arithmetic operations...at least until you have nothing else left to do
- GPUs provide tremendous memory bandwidth, but even so, **memory bandwidth often ends up being the performance limiter**
- Keep/reuse data in **registers** as long as possible
- The main consideration when programming GPUs is **accessing memory efficiently**, and storing operands in the **most appropriate memory system** according to data size and access pattern



### Using the CPU to Optimize GPU Performance

- GPU performs best when the work evenly divides into the number of threads/processing units
- Optimization strategy:
  - Use the CPU to *"regularize"* the GPU workload
  - Use fixed size bin data structures, with "empty" slots skipped or producing zeroed out results
  - Handle exceptional or irregular work units on the CPU;
     GPU processes the bulk of the work concurrently
  - On average, the GPU is kept highly occupied, attaining a high fraction of peak performance



## GPU On-Chip Memory Systems

- GPU arithmetic rates dwarf global memory bandwidth
- GPUs include multiple fast **on-chip** memories to help **narrow the gap**:
  - Registers
  - Constant memory (64KB)
  - Shared memory (48KB / 16KB)
  - Read-only data cache / Texture cache (~48KB)
    - Hardware-assisted 1-D, 2-D, 3-D locality
    - Hardware range clamping, type conversion, interpolation



Avoiding Shared Memory Bank Conflicts: Array of Structures (AOS) vs. Structure of Arrays (SOA)

- AOS: typedef struct { float x; float y; float z;
- } myvec; myvec aos[1024]; aos[threadIdx.x].x = 0; aos[threadIdx.x].y = 0;

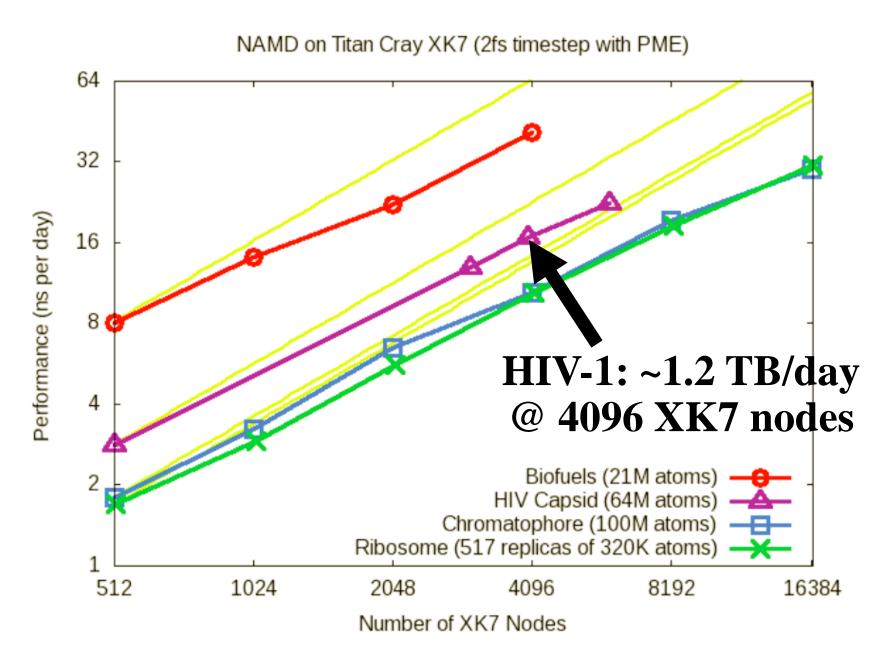
- SOA: typedef struct { float x[1024]; float y[1024]; float z[1024]; } myvecs; myvecs soa;
- soa.x[threadIdx.x] = 0; soa.y[threadIdx.x] = 0;



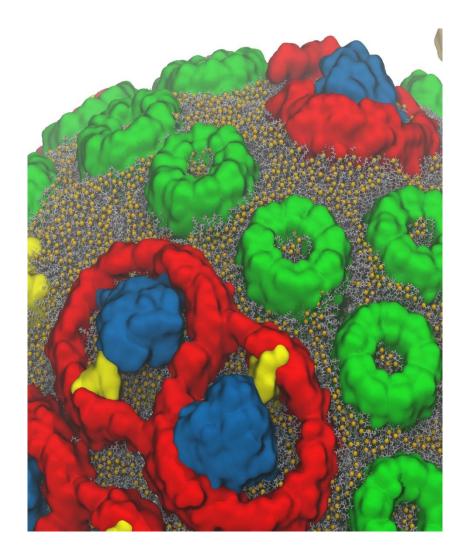


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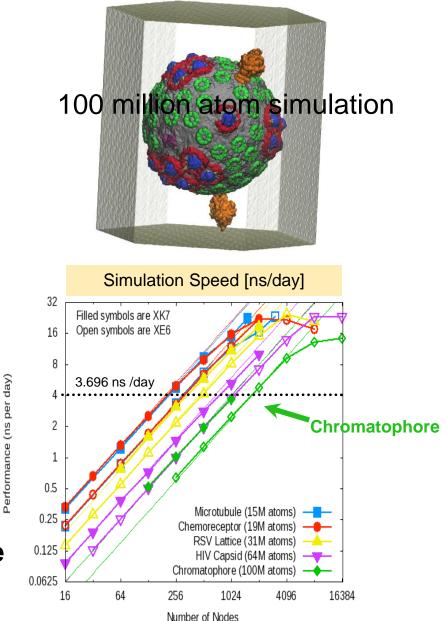
### NAMD Titan XK7 Performance August 2013



### **100-million Atom Simulation of Chromatophore**



## segment of simulated chromatophore showing lipids



### VMD Petascale Visualization and Analysis

- Analyze/visualize large trajectories too large to transfer off-site:
  - Compute time-averaged electrostatic fields, MDFF quality-of-fit, etc.
  - User-defined parallel analysis operations, data types
  - Parallel rendering, movie making
- Parallel I/O rates up to 275 GB/sec on 8192 Cray XE6 nodes – can read in 231 TB in 15 minutes!
- Multi-level dynamic load balancing tested with up to 262,144 CPU cores
- Supports GPU-accelerated Cray XK7 nodes for both visualization and analysis usage



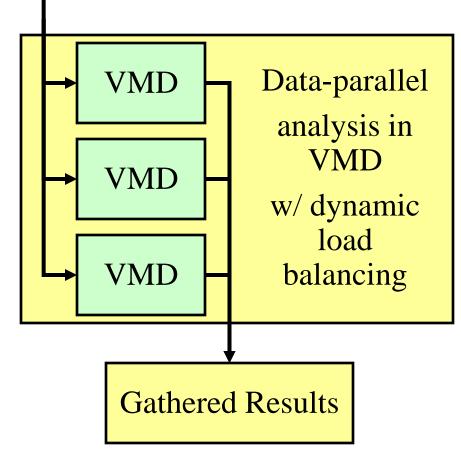
NCSA Blue Waters Hybrid Cray XE6 / XK7 Supercomputer 22,640 XE6 CPU nodes

4,224 XK7 nodes w/ GPUs support fast VMD OpenGL movie rendering and visualization

#### VMD for Demanding Analysis Tasks Parallel VMD Analysis w/ MPI

- Compute time-averaged electrostatic fields, MDFF quality-of-fit, etc.
- Parallel rendering, movie making
- User-defined parallel reduction operations, data types
- Parallel I/O on Blue Waters:
  - 109 GB/sec on 512 nodes
  - 275 GB/sec on 8,192 nodes
- Timeline per-residue SASA calc. achieves 800x speedup @ 1000 BW XE6 nodes
- Supports GPU-accelerated clusters and supercomputers

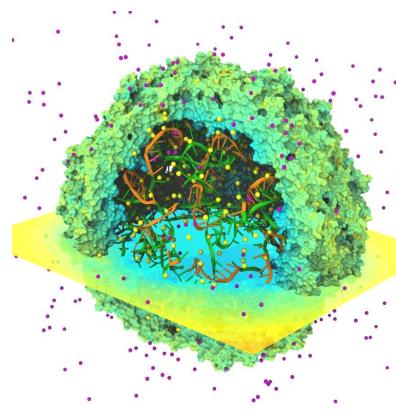
Sequence/Structure Data, Trajectory Frames, etc...



### Time-Averaged Electrostatics Analysis on Energy-Efficient GPU Cluster

- 1.5 hour job (CPUs) reduced to 3 min (CPUs+GPU)
- Electrostatics of thousands of trajectory frames averaged
- Per-node power consumption on NCSA "AC" GPU cluster:
  - CPUs-only: 448 Watt-hours
  - CPUs+GPUs: 43 Watt-hours
- GPU Speedup: 25.5x
- Power efficiency gain: **10.5**x

Quantifying the Impact of GPUs on Performance and Energy Efficiency in HPC Clusters. J. Enos, C. Steffen, J. Fullop, M. Showerman, G. Shi, K. Esler, V. Kindratenko, J. Stone, J. Phillips. *The Work in Progress in Green Computing*, pp. 317-324, 2010.

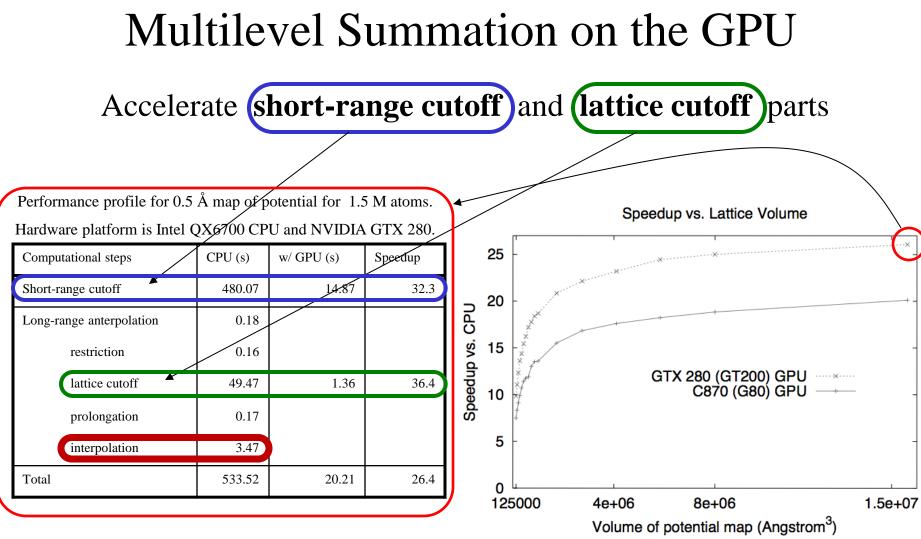


# Time-Averaged Electrostatics Analysis on NCSA Blue Waters

NCSA Blue Waters Node Type	Seconds per trajectory frame for one compute node
Cray XE6 Compute Node: 32 CPU cores (2xAMD 6200 CPUs)	9.33
Cray XK6 GPU-accelerated Compute Node: 16 CPU cores + NVIDIA X2090 (Fermi) GPU	2.25
Speedup for GPU XK6 nodes vs. CPU XE6 nodes	XK6 nodes are 4.15x faster overall
Tests on XK7 nodes indicate MSM is CPU-bound with the Kepler K20X GPU. Performance is not much faster (yet) than Fermi X2090 Need to move spatial hashing, prolongation, interpolation onto the GPU	In progress XK7 nodes 4.3x faster overall

Preliminary performance for VMD time-averaged electrostatics w/ Multilevel Summation Method on the NCSA Blue Waters Early Science System





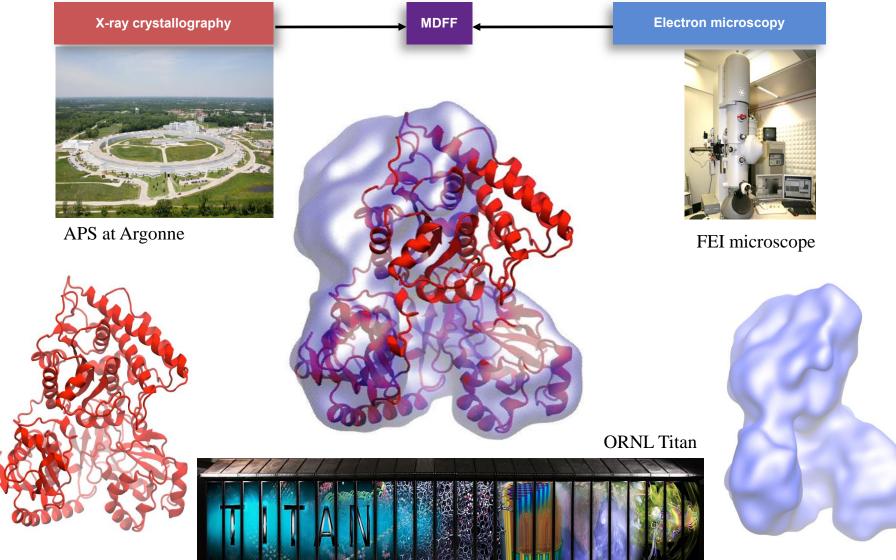
#### Multilevel summation of electrostatic potentials using graphics processing units.

D. Hardy, J. Stone, K. Schulten. J. Parallel Computing, 35:164-177, 2009.



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#### Molecular Dynamics Flexible Fitting (MDFF)



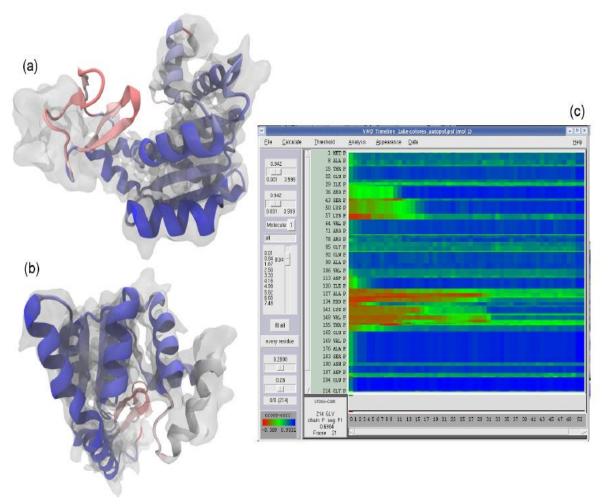
Acetyl - CoA Synthase

Flexible fitting of atomic structures into electron microscopy maps using molecular dynamics. L. Trabuco, E. Villa, K. Mitra, J. Frank, and K. Schulten. Structure, 16:673-683, 2008.

#### GPUs Can Reduce Trajectory Analysis Runtimes from Hours to Minutes

GPUs enable laptops and desktop workstations to handle tasks that would have previously required a cluster, or a very long wait...

GPU-accelerated petascale supercomputers enable analyses that were previously impractical, allowing detailed study of very large structures such as viruses



## GPU-accelerated MDFF Cross Correlation TimelineRegions with poor fitRegions with good fit

### VMD GPU Cross Correlation Performance

	RHDV	Mm-cpn open	GroEL	Aquaporin
<b>Resolution</b> (Å)	6.5	8	4	3
Atoms	702K	61K	54K	1.6K
VMD-CUDA	0.458s	0.06s	0.034s	0.007s
Quadro K6000	34.6x	25.7x	36.8x	55.7x
VMD-CPU-SSE	0.779s	0.085s	0.159s	0.033s
32-threads, 2x Xeon E5-2687W	20.3x	18.1x	7.9x	11.8x
Chimera	15.86s	1.54s	1.25s	0.39s
1-thread Xeon E5-2687W	1.0x	1.0x	1.0x	1.0x
VMD CPU-SEQ (plugin)	62.89s	2.9s	1.57s	0.04s
1-thread Xeon E5-2687W	0.25x	0.53x	0.79x	9.7x

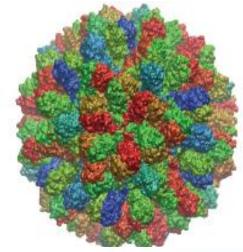
**GPU-accelerated analysis and visualization of large structures solved by molecular dynamics flexible fitting.** J. E. Stone, R. McGreevy, B. Isralewitz, and K. Schulten. Faraday Discussion 169, 2014.



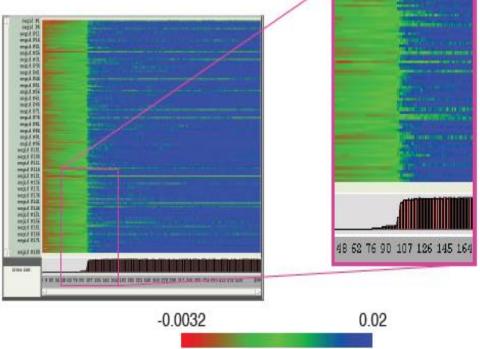
## VMD RHDV Cross Correlation Timeline on Cray XK7

	RHDV
Atoms	702K
Traj. Frames	10,000
Component Selections	720
Single-node XK7 (projected)	336 hours (14 days)
128-node XK7	3.2 hours 105x speedup
2048-node XK7	19.5 minutes 1035x speedup

Calculation would take **5 years** using original serial VMD CC plugin on a workstation!

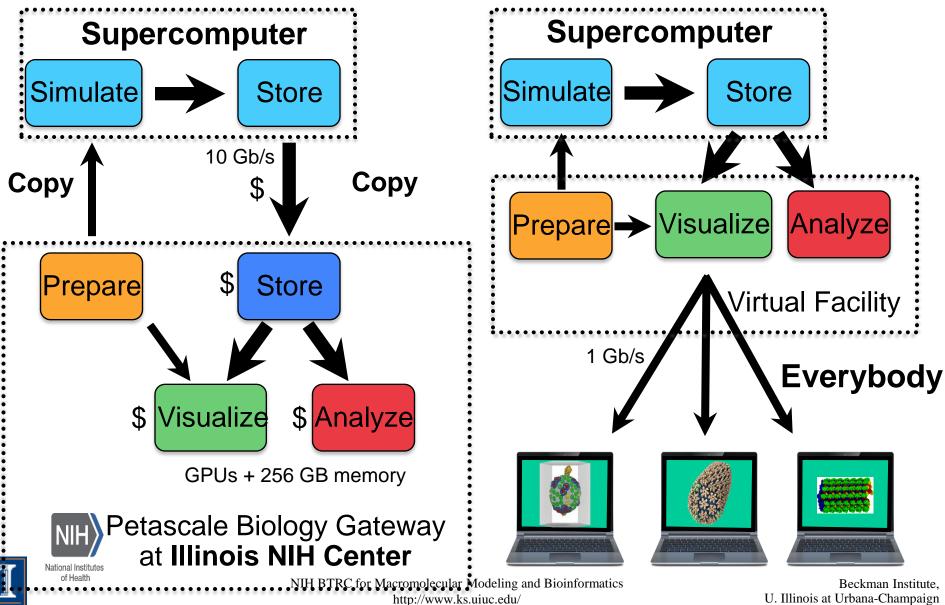


#### **RHDV CC Timeline**



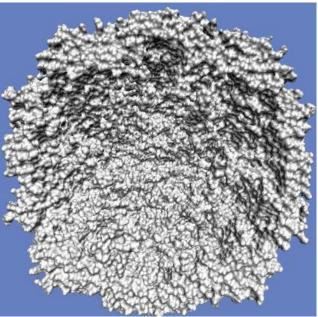


Large Memory Remote Visualization & Analysis Nodes Would Broaden User Base and Accelerate Discovery

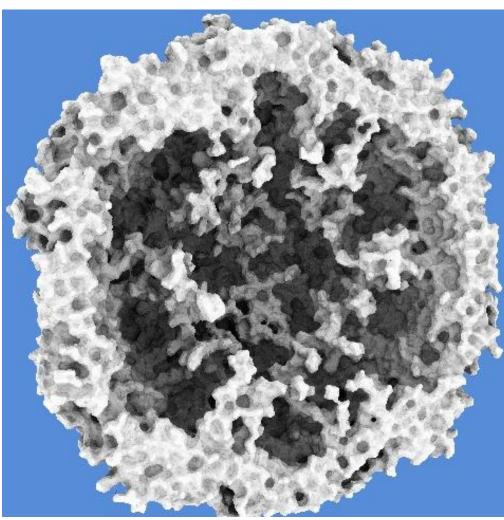


## Ray Tracing Molecular Graphics w/ OptiX+CUDA

- Ambient occlusion lighting, shadows, reflections, transparency, and more...
- Satellite tobacco mosaic virus capsid w/ ~75K atoms

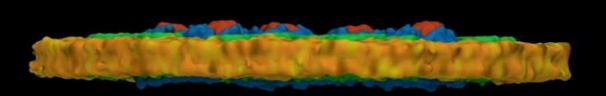






# Prototype VMD/OptiX GPU ray tracing w/ ambient occlusion lighting

## **BW VMD/Tachyon Movie Generation**

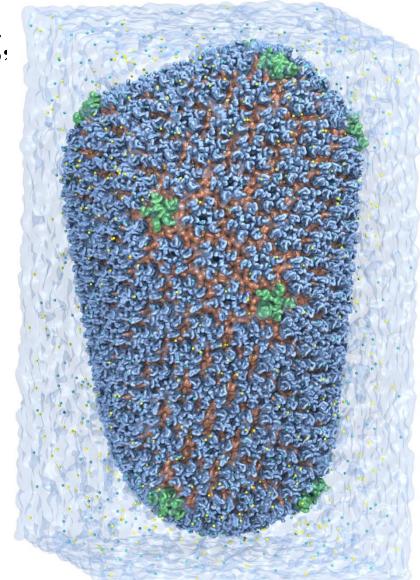


#### 20 M atom chromatophore patch

### 360 XE6 nodes for 3h50m @ 4096x2400

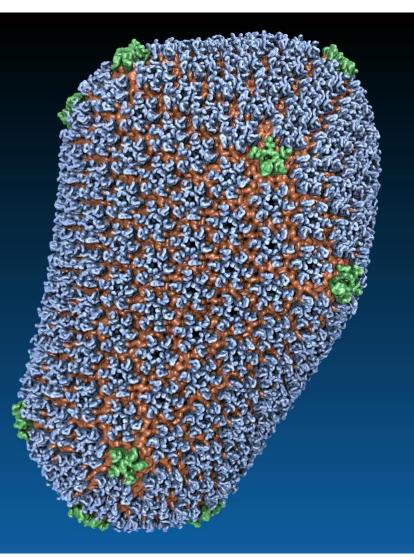
GPU Ray Tracing of HIV-1 on Blue Waters

- Ambient occlusion lighting, shadows, transparency, antialiasing, depth cueing, 144 rays/pixel minimum
- 64 million atom virus simulation
- 1000+ movie frames
- Surface generation and ray tracing stages each use >= 75% of GPU memory





## VMD GPU Ray Tracing of HIV-1 Capsid





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### HIV-1 Parallel HD Movie Rendering on Blue Waters Cray XE6/XK7

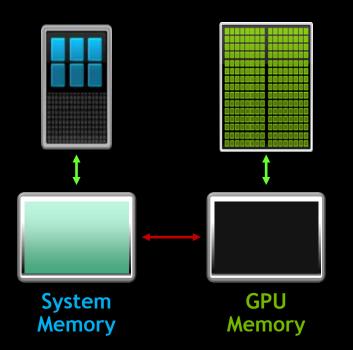
New "TachyonL-OptiX" on XK7 vs. Tachyon on XE6: K20X GPUs yield **up to eight times** geom+ray tracing speedup

Node Type and Count	Script Load Time	State Load Time	Geometry + Ray Tracing	Total Time
256 XE6 CPUs	7 s	160 s	1,374 s	1,541 s
512 XE6 CPUs	13 s	211 s	808 s	1,032 s
64 XK7 Tesla K20X GPUs	2 s	38 s	655 s	695 s
128 XK7 Tesla K20X GPUs	4 s	74 s	331 s	410 s
256 XK7 Tesla K20X GPUs	7 s	110 s	171 s	288 s

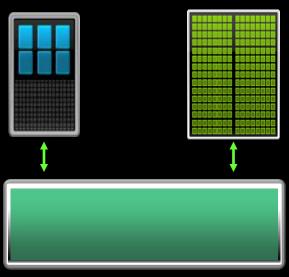
**GPU-Accelerated Molecular Visualization on Petascale Supercomputing Platforms.** Stone et al. In UltraVis'13: Eighth Workshop on Ultrascale Visualization Proceedings, 2013.

## Unified Memory Dramatically Lower Developer Effort

#### **Developer View Today**



#### Developer View With Unified Memory



**Unified Memory** 

#### **Courtesy NVIDIA**

## Super Simplified Memory Management Code

#### **CPU Code**

void sortfile(FILE \*fp, int N) {
 char \*data;
 data = (char \*)malloc(N);

fread(data, 1, N, fp);

qsort(data, N, 1, compare);

use\_data(data);

free(data);

}

#### CUDA 6 Code with Unified Memory

void sortfile(FILE \*fp, int N) {
 char \*data;
 cudaMallocManaged(&data, N);

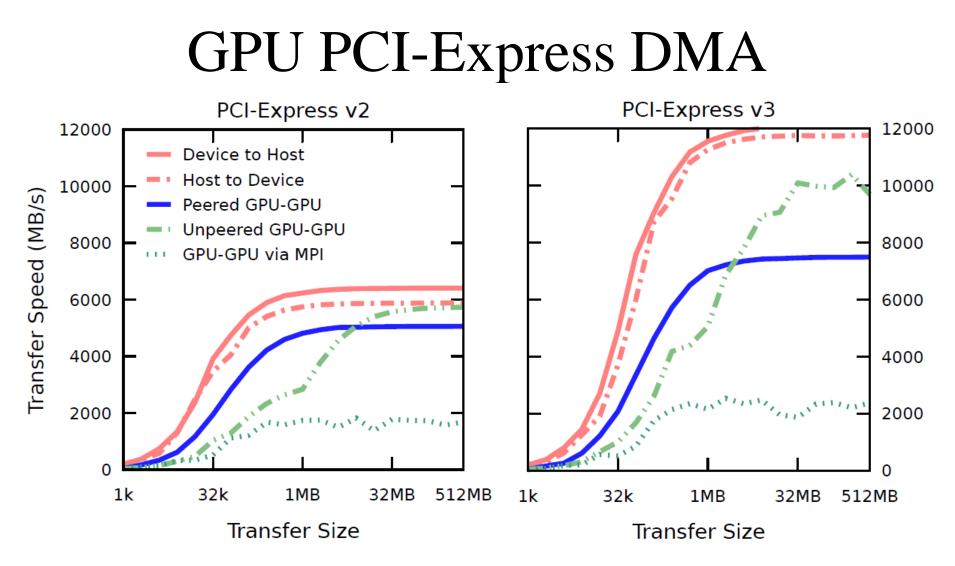
fread(data, 1, N, fp);

qsort<<<...>>>(data,N,1,compare);
 cudaDeviceSynchronize();

use\_data(data);

cudaFree(data);

**Courtesy NVIDIA** 



Simulation of reaction diffusion processes over biologically relevant size and time scales using multi-GPU workstations Michael J. Hallock, John E. Stone, Elijah Roberts, Corey Fry, and Zaida Luthey-Schulten. Journal of Parallel Computing, 2014. (In press) http://dx.doi.org/10.1016/j.parco.2014.03.009



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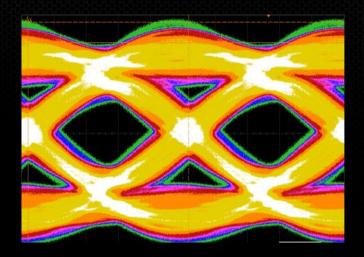
## **Future: NVLINK and Stacked Memory**

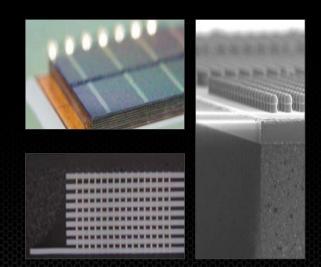
#### NVLINK

- GPU high speed interconnect
- 80-200 GB/s
- Planned support for POWER CPUs

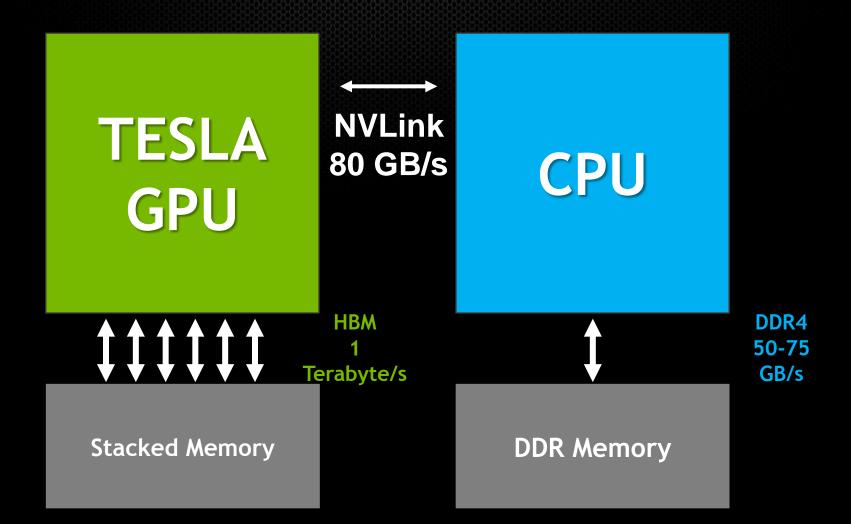
### **Stacked Memory**

- 4x Higher Bandwidth (~1 TB/s)
- 3x Larger Capacity
- 4x More Energy Efficient per bit





## NVLink Enables Data Transfer At Speed of CPU Memory



## PASCAL

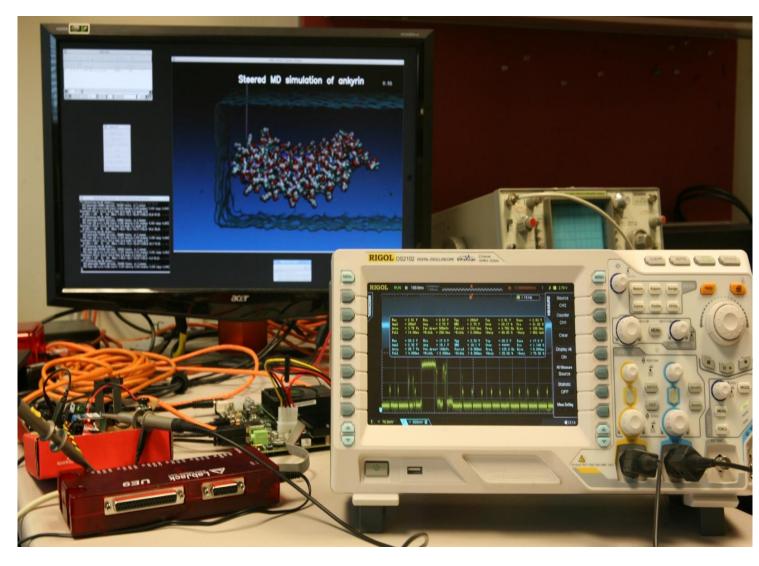
NVLink 3D Memory Module

5 to 12X PCIe 3.0 2 to 4X memory BW & size 1/3 size of PCIe card 125.50

## Optimizing GPU Algorithms for Power Consumption

NVIDIA "Carma", "Kayla", "Jetson" single board computers

Tegra+GPU energy efficiency testbed





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- Runtime and Architecture Support for Efficient Data Exchange in Multi-Accelerator Applications Javier Cabezas, Isaac Gelado, John E. Stone, Nacho Navarro, David B. Kirk, and Wen-mei Hwu. IEEE Transactions on Parallel and Distributed Systems, 2014. (Accepted)
- Unlocking the Full Potential of the Cray XK7 Accelerator Mark Klein and John E. Stone. Cray Users Group, 2014. (In press)
- Simulation of reaction diffusion processes over biologically relevant size and time scales using multi-GPU workstations Michael J. Hallock, John E. Stone, Elijah Roberts, Corey Fry, and Zaida Luthey-Schulten. Journal of Parallel Computing, 2014. (In press)
- **GPU-Accelerated Analysis and Visualization of Large Structures Solved by Molecular Dynamics Flexible Fitting** John E. Stone, Ryan McGreevy, Barry Isralewitz, and Klaus Schulten. Faraday Discussion 169, 2014. (In press)
- **GPU-Accelerated Molecular Visualization on Petascale Supercomputing Platforms.** J. Stone, K. L. Vandivort, and K. Schulten. UltraVis'13: Proceedings of the 8th International Workshop on Ultrascale Visualization, pp. 6:1-6:8, 2013.
- Early Experiences Scaling VMD Molecular Visualization and Analysis Jobs on Blue Waters. J. E. Stone, B. Isralewitz, and K. Schulten. In proceedings, Extreme Scaling Workshop, 2013.
- Lattice Microbes: High-performance stochastic simulation method for the reaction-diffusion master equation. E. Roberts, J. E. Stone, and Z. Luthey-Schulten. J. Computational Chemistry 34 (3), 245-255, 2013.



- Fast Visualization of Gaussian Density Surfaces for Molecular Dynamics and Particle System Trajectories. M. Krone, J. E. Stone, T. Ertl, and K. Schulten. *EuroVis Short Papers*, pp. 67-71, 2012.
- Fast Analysis of Molecular Dynamics Trajectories with Graphics Processing Units Radial Distribution Functions. B. Levine, J. Stone, and A. Kohlmeyer. J. Comp. Physics, 230(9):3556-3569, 2011.
- Immersive Out-of-Core Visualization of Large-Size and Long-Timescale Molecular Dynamics Trajectories. J. Stone, K. Vandivort, and K. Schulten. G. Bebis et al. (Eds.): *7th International Symposium on Visual Computing (ISVC 2011)*, LNCS 6939, pp. 1-12, 2011.
- Quantifying the Impact of GPUs on Performance and Energy Efficiency in HPC Clusters. J. Enos, C. Steffen, J. Fullop, M. Showerman, G. Shi, K. Esler, V. Kindratenko, J. Stone, J Phillips. *International Conference on Green Computing*, pp. 317-324, 2010.
- GPU-accelerated molecular modeling coming of age. J. Stone, D. Hardy, I. Ufimtsev, K. Schulten. J. Molecular Graphics and Modeling, 29:116-125, 2010.
- OpenCL: A Parallel Programming Standard for Heterogeneous Computing. J. Stone, D. Gohara, G. Shi. *Computing in Science and Engineering*, 12(3):66-73, 2010.



- An Asymmetric Distributed Shared Memory Model for Heterogeneous Computing Systems. I. Gelado, J. Stone, J. Cabezas, S. Patel, N. Navarro, W. Hwu. *ASPLOS '10: Proceedings of the 15<sup>th</sup> International Conference on Architectural Support for Programming Languages and Operating Systems*, pp. 347-358, 2010.
- **GPU Clusters for High Performance Computing**. V. Kindratenko, J. Enos, G. Shi, M. Showerman, G. Arnold, J. Stone, J. Phillips, W. Hwu. *Workshop on Parallel Programming on Accelerator Clusters (PPAC)*, In Proceedings IEEE Cluster 2009, pp. 1-8, Aug. 2009.
- Long time-scale simulations of in vivo diffusion using GPU hardware. E. Roberts, J. Stone, L. Sepulveda, W. Hwu, Z. Luthey-Schulten. In *IPDPS'09: Proceedings of the 2009 IEEE International Symposium on Parallel & Distributed Computing*, pp. 1-8, 2009.
- High Performance Computation and Interactive Display of Molecular Orbitals on GPUs and Multi-core CPUs. J. Stone, J. Saam, D. Hardy, K. Vandivort, W. Hwu, K. Schulten, 2nd Workshop on General-Purpose Computation on Graphics Pricessing Units (GPGPU-2), ACM International Conference Proceeding Series, volume 383, pp. 9-18, 2009.
- **Probing Biomolecular Machines with Graphics Processors**. J. Phillips, J. Stone. *Communications of the ACM*, 52(10):34-41, 2009.
- Multilevel summation of electrostatic potentials using graphics processing units. D. Hardy, J. Stone, K. Schulten. *J. Parallel Computing*, 35:164-177, 2009.



- Adapting a message-driven parallel application to GPU-accelerated clusters. J. Phillips, J. Stone, K. Schulten. *Proceedings of the 2008 ACM/IEEE Conference on Supercomputing*, IEEE Press, 2008.
- GPU acceleration of cutoff pair potentials for molecular modeling applications.
   C. Rodrigues, D. Hardy, J. Stone, K. Schulten, and W. Hwu. *Proceedings of the 2008 Conference On Computing Frontiers*, pp. 273-282, 2008.
- **GPU computing**. J. Owens, M. Houston, D. Luebke, S. Green, J. Stone, J. Phillips. *Proceedings* of the IEEE, 96:879-899, 2008.
- Accelerating molecular modeling applications with graphics processors. J. Stone, J. Phillips, P. Freddolino, D. Hardy, L. Trabuco, K. Schulten. *J. Comp. Chem.*, 28:2618-2640, 2007.
- Continuous fluorescence microphotolysis and correlation spectroscopy. A. Arkhipov, J. Hüve, M. Kahms, R. Peters, K. Schulten. *Biophysical Journal*, 93:4006-4017, 2007.

