S5371—VMD: Visualization and Analysis of Biomolecular Complexes with GPU Computing

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http://www.ks.uiuc.edu/Research/gpu/

S5371, GPU Technology Conference

9:00-9:50, Room LL21C, San Jose Convention Center,

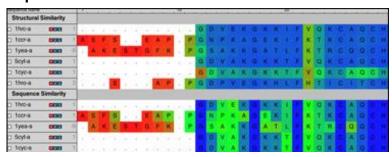
San Jose, CA, Wednesday March 18, 2015





VMD - "Visual Molecular Dynamics"

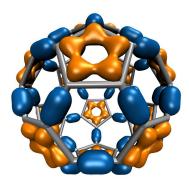
- Visualization and analysis of:
 - molecular dynamics simulations
 - particle systems and whole cells
 - cryoEM densities, volumetric data
 - quantum chemistry calculations
 - sequence information
- User extensible w/ scripting and plugins
- http://www.ks.uiuc.edu/Research/vmd/



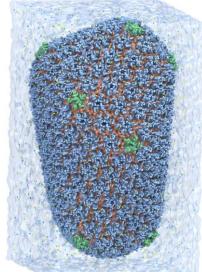
Sequence Data



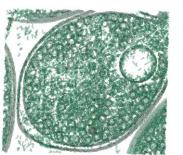
Whole Cell Simulation



Quantum Chemistry



MD Simulations

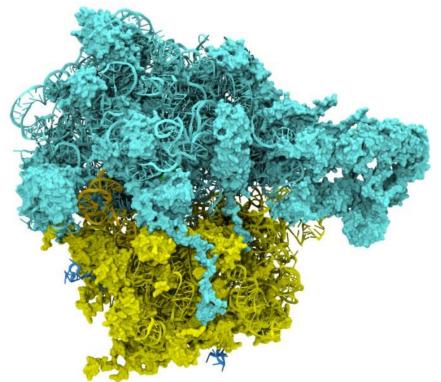


CryoEM, Cellular Tomography

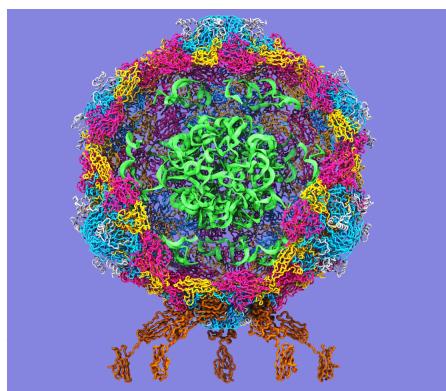
Goal: A Computational Microscope

Study the molecular machines in living cells

Ribosome: target for antibiotics

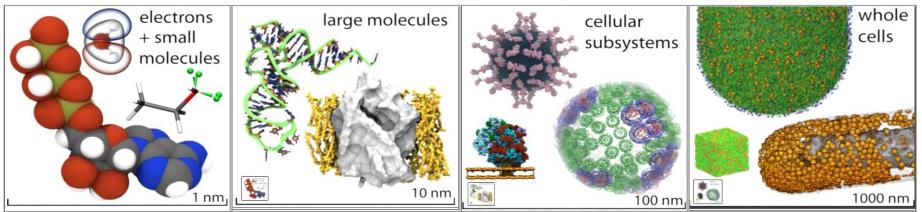


Poliovirus



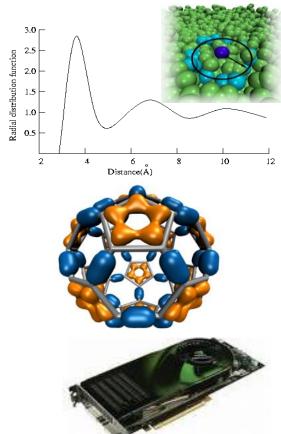
VMD Interoperability Serves Many Communities

- VMD 1.9.1 user statistics:
 - 100,000 unique registered users from all over the world
- Uniquely interoperable with a broad range of tools: AMBER, CHARMM, CPMD, DL_POLY, GAMESS, GROMACS, HOOMD, LAMMPS, NAMD, and many more ...
- Supports key data types, file formats, and databases, e.g. electron microscopy, quantum chemistry, MD trajectories, sequence alignments, super resolution light microscopy
- Incorporates tools for simulation preparation, visualization, and analysis



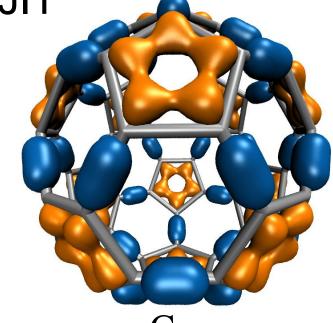
CUDA GPU-Accelerated Trajectory Analysis and Visualization in VMD

VMD GPU-Accelerated Feature or GPU Kernel	Exemplary speedup vs. contemporary 4-core CPU
Molecular orbital display	30x
Radial distribution function	23x
Molecular surface display	15x
Electrostatic field calculation	11x
Ray tracing w/ shadows, AO lighting	7x
cryoEM cross correlation quality-of-fit	7x
Ion placement	6x
MDFF density map synthesis	6x
Implicit ligand sampling	6x
Root mean squared fluctuation	6x
Radius of gyration	5x
Close contact determination	5x
Dipole moment calculation	4x



Molecular Orbitals w/ NVRTC JIT

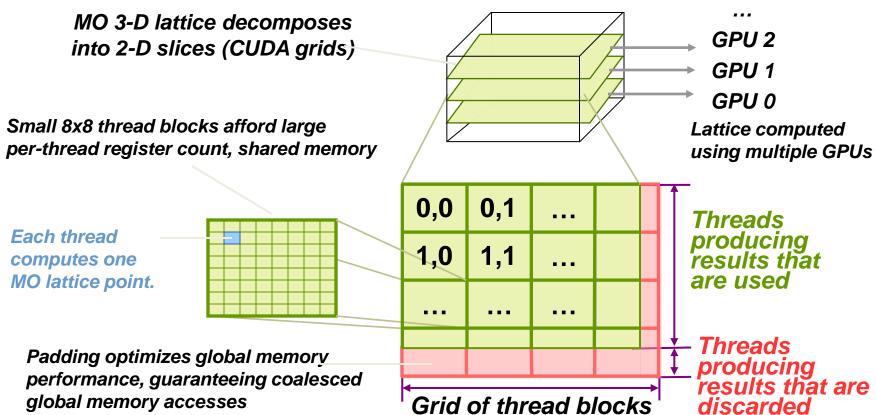
- Visualization of MOs aids in understanding the chemistry of molecular system
- MO spatial distribution is correlated with probability density for an electron(s)
- Animation of (classical mechanics) molecular dynamics trajectories provides insight into simulation results
 - To do the same for QM or QM/MM simulations MOs must be computed at 10 FPS or more
 - Large GPU speedups (up to 30x vs. 4-core CPU) over existing tools makes this possible!
- Run-time code generation (JIT) and compilation via CUDA 7.0 NVRTC enable further optimizations and the highest performance to date: 1.8x faster than previous best result



 C_{60}

High Performance Computation and Interactive Display of Molecular Orbitals on GPUs and Multicore CPUs. J. E. Stone, J. Saam, D. Hardy, K. Vandivort, W. Hwu, K. Schulten, 2nd Workshop on General-Purpose Computation on Graphics Processing Units (GPGPU-2), ACM International Conference Proceeding Series, volume 383, pp. 9-18, 2009.

MO GPU Parallel Decomposition



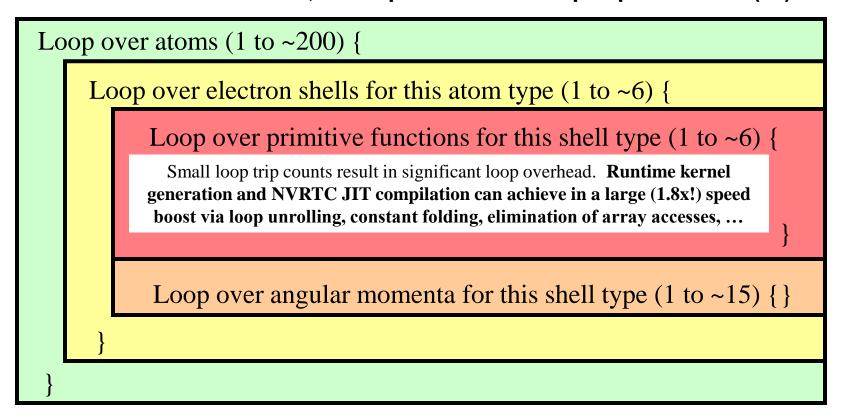




MO Kernel for One Grid Point (Naive C)

```
for (at=0; at<numatoms; at++) {
                                                                              Loop over atoms
  int prim_counter = atom_basis[at];
  calc distances to atom(&atompos[at], &xdist, &vdist, &zdist, &dist2, &xdiv);
  for (contracted_gto=0.0f, shell=0; shell < num_shells_per_atom[at]; shell++) {
                                                                               Loop over shells
    int shell_type = shell_symmetry[shell_counter];
    for (prim=0; prim < num_prim_per_shell[shell_counter]; prim++) {
                                                                              Loop over primitives:
       float exponent
                         = basis_array[prim_counter
      float contract_coeff = basis_array[prim_counter + 1];
                                                                               largest component of
       contracted_gto += contract_coeff * expf(-exponent*dist2);
                                                                              runtime, due to expf()
       prim counter += 2;
                                                                                 Loop over angular
    for (tmpshell=0.0f, j=0, zdp=1.0f; j<=shell_type; j++, zdp*=zdist) {
      int imax = shell_type - j;
                                                                                        momenta
      for (i=0, ydp=1.0f, xdp=pow(xdist, imax); i<=imax; i++, ydp*=ydist, xdp*=xdiv)
        tmpshell += wave f[ifunc++] * xdp * ydp * zdp;
                                                                               (unrolled in real code)
    value += tmpshell * contracted gto;
    shell counter++;
```

MO Kernel Structure, Opportunity for NRTC JIT... Data-driven execution, but representative loop trip counts in (...)



Molecular Orbital Computation and Display Process Runtime Kernel Generation, NVRTC Just-In-Time (JIT) Compilation

One-time initialization

Initialize Pool of GPU Worker Threads Read QM simulation log file, trajectory

Preprocess MO coefficient data eliminate duplicates, sort by type, etc...

Generate/compile basis set-specific CUDA kernel

For each trj frame, for each MO shown

For current frame and MO index, retrieve MO wavefunction coefficients

Compute 3-D grid of MO wavefunction amplitudes using basis set-specific CUDA kernel

Extract isosurface mesh from 3-D MO grid

Render the resulting surface

```
for (shell=0; shell < maxshell; shell++) {</pre>
 float contracted_gto = 0.0f;
 // Loop over the Gaussian primitives of CGTO
 int maxprim = const_num_prim_per_shell[shell_counter];
 int shell_type = const_shell_symmetry[shell_counter];
 for (prim=0; prim < maxprim; prim++) {</pre>
  float exponent
                      = const basis array[prim counter
  float contract coeff = const basis array[prim counter + 1];
  contracted_gto += contract_coeff * expf(-exponent*dist2);
  prim_counter += 2;
```

contracted_gto = 1.832937 * expf(-7.868272*dist2); contracted_gto += 1.405380 * expf(-1.881289*dist2); contracted_gto += 0.701383 * expf(-0.544249*dist2); General loop-based data-dependent MO CUDA kernel

Runtime-generated data-specific MO CUDA kernel compiled via CUDA 7.0 NVRTC JIT...

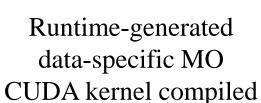


1.8x Faster

```
for (shell=0; shell < maxshell; shell++) {</pre>
   float contracted_gto = 0.0f;
   // Loop over the Gaussian primitives of CGTO
   int maxprim = const_num_prim_per_shell[shell_counter];
   int shell_type = const_shell_symmetry[shell_counter];
   for (prim=0; prim < maxprim; prim++) {</pre>
                        = const_basis_array[prim_counter
    float exponent
    float contract coeff = const basis array[prim counter + 1];
    contracted_gto += contract_coeff * expf(-exponent*dist2);
    prim_counter += 2;
   float tmpshell=0;
   switch (shell_type) {
    case S SHELL:
     value += const_wave_f[ifunc++] * contracted_gto;
     break;
[.....]
    case D_SHELL:
     tmpshell += const_wave_f[ifunc++] * xdist2;
     tmpshell += const_wave_f[ifunc++] * ydist2;
     tmpshell += const_wave_f[ifunc++] * zdist2;
```

tmpshell += const wave f[ifunc++] * xdist * vdist;

General loop-based data-dependent MO CUDA kernel



NVRTC JIT...

via CUDA 7.0



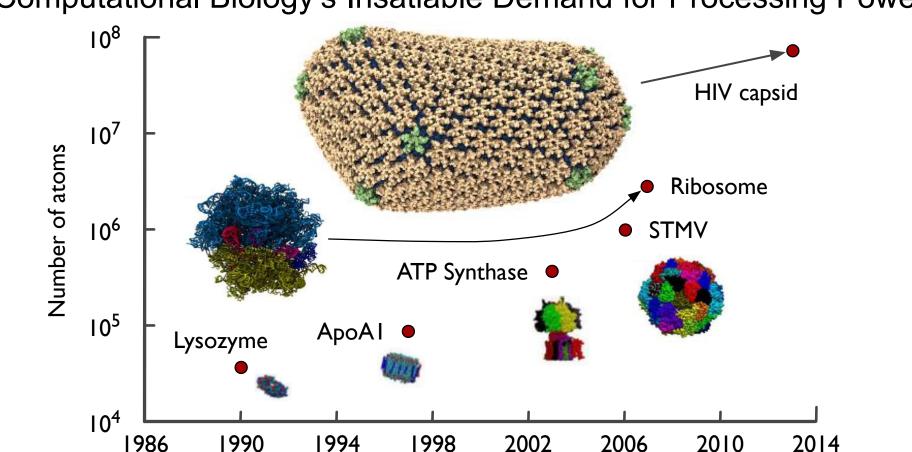
1.8x Faster

```
contracted gto = 1.832937 * \exp(-7.868272*dist2);
contracted gto += 1.405380 * \exp(-1.881289* \text{dist2});
contracted_gto += 0.701383 * expf(-0.544249*dist2);
// P_SHELL
tmpshell = const wave f[ifunc++] * xdist;
tmpshell += const_wave_f[ifunc++] * ydist;
tmpshell += const wave f[ifunc++] * zdist;
value += tmpshell * contracted_gto;
contracted gto = 0.187618 * \exp(-0.168714* \text{dist2});
// S SHELL
value += const wave f[ifunc++] * contracted gto;
contracted_gto = 0.217969 * expf(-0.168714*dist2);
// P SHELL
tmpshell = const_wave_f[ifunc++] * xdist;
```

tmpshell += const_wave_f[ifunc++] * ydist; tmpshell += const_wave_f[ifunc++] * zdist; value += tmpshell * contracted_gto;

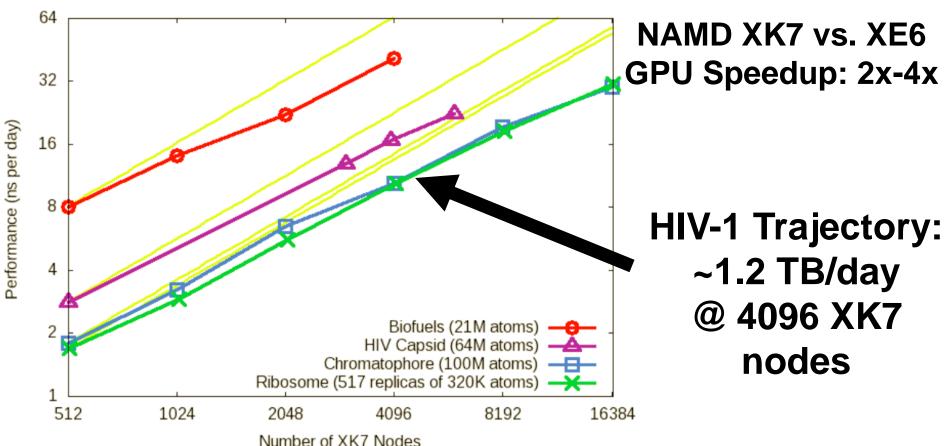
contracted_gto = 3.858403 * expf(-0.800000*dist2);
// D_SHELL
tmpshell = const_wave_f[ifunc++] * xdist2;
tmpshell += const_wave_f[ifunc++] * ydist2;

NAMD and VMD Use GPUs and Petascale Computing to Meet Computational Biology's Insatiable Demand for Processing Power



NAMD Titan XK7 Performance August 2013

NAMD on Titan Cray XK7 (2fs timestep with PME)



VMD Petascale Visualization and Analysis

- Analyze/visualize large trajectories too large to transfer off-site:
 - User-defined parallel analysis operations, data types
 - Parallel rendering, movie making
- Supports GPU-accelerated Cray XK7 nodes for both visualization and analysis:
 - GPU accelerated trajectory analysis w/ CUDA
 - OpenGL and GPU ray tracing for visualization and movie rendering
- Parallel I/O rates up to 275 GB/sec on 8192 Cray
 XE6 nodes can read in 231 TB in 15 minutes!

Parallel VMD currently available on:

ORNL Titan, NCSA Blue Waters, Indiana Big Red II, CSCS Piz Daint, and similar systems

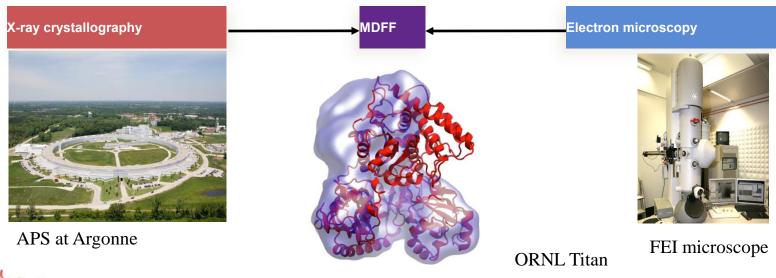


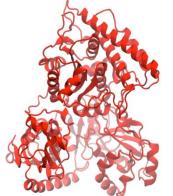
NCSA Blue Waters Hybrid Cray XE6 / XK7 22,640 XE6 dual-Opteron CPU nodes 4,224 XK7 nodes w/ Telsa K20X GPUs



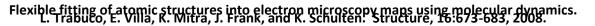


Molecular Dynamics Flexible Fitting (MDFF)











Molecular Dynamics Flexible Fitting - Theory

Two terms are added to the MD potential

$$U_{total} = U_{MD} + U_{EM} + U_{SS}$$

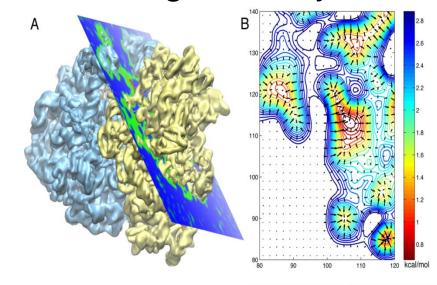
An external potential derived from the EM map is defined on a grid as

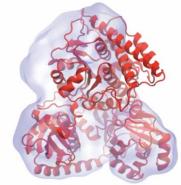
$$U_{EM}(\mathbf{R}) = \sum_{j} w_{j} V_{EM}(\mathbf{r}_{j})$$

$$V_{EM}(\mathbf{r}) = \begin{cases} \xi \left(1 - \frac{\Phi(\mathbf{r}) - \Phi_{thr}}{\Phi_{max} - \Phi_{thr}} \right) & \text{if } \Phi(\mathbf{r}) \ge \Phi_{thr}, \\ \xi & \text{if } \Phi(\mathbf{r}) < \Phi_{thr}. \end{cases}$$

A mass-weighted force is then applied to each atom

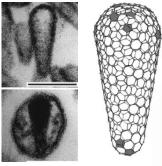
$$\mathbf{f}_{i}^{EM} = -\nabla U_{EM}(\mathbf{R}) = -w_{i}\partial V_{EM}(\mathbf{r}_{i})/\partial r_{i}$$



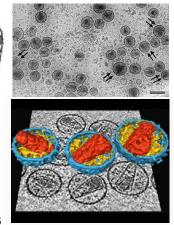


Structural Route to the all-atom HIV-1 Capsid

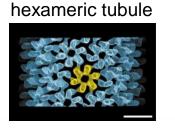
1st TEM (1999) 1st tomography (2003)



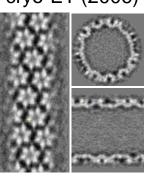
Ganser et al. Science, 1999 Briggs et al. EMBO J, 2003 Briggs et al. Structure, 2006



cryo-ET (2006)

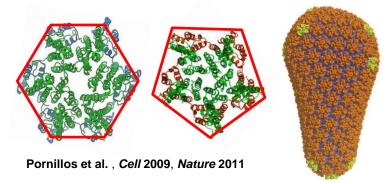


Li et al., Nature, 2000

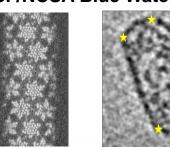


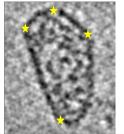
Byeon et al., Cell 2009

Crystal structures of separated hexamer and pentamer



High res. EM of hexameric tubule, tomography of capsid, all-atom model of capsid by MDFF w/ NAMD & VMD, **NSF/NCSA Blue Waters computer at Illinois**



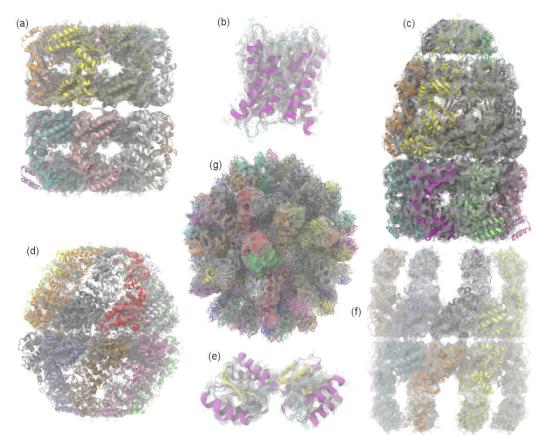




Zhao et al., *Nature* 497: 643-646 (2013)

Evaluating Quality-of-Fit for Structures Solved by Hybrid Fitting Methods

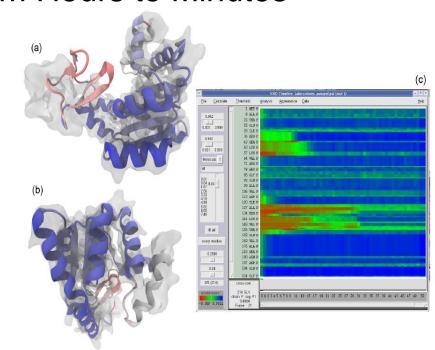
Compute Pearson correlation to evaluate the fit of a reference cryo-EM density map with a simulated density map produced from an all-atom structure.



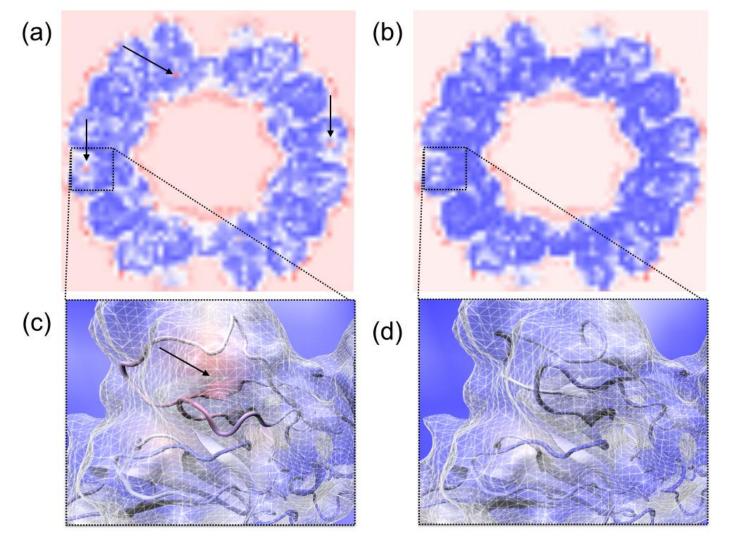
GPUs Can Reduce MDFF Trajectory Analysis Runtimes from Hours to Minutes

GPUs enable laptops and desktop workstations to handle tasks that would have previously required a cluster, or a *very long wait...*

GPU-accelerated petascale supercomputers enable analyses that were previously impractical, allowing detailed study of very large structures such as viruses



GPU-accelerated MDFF Cross Correlation Timeline
Regions with poor fit Regions with good fit

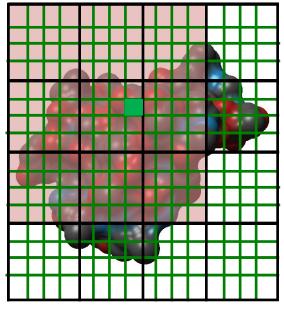


MDFF Density Map Algorithm

- Build spatial acceleration data structures, optimize data for GPU
- Compute 3-D density map:

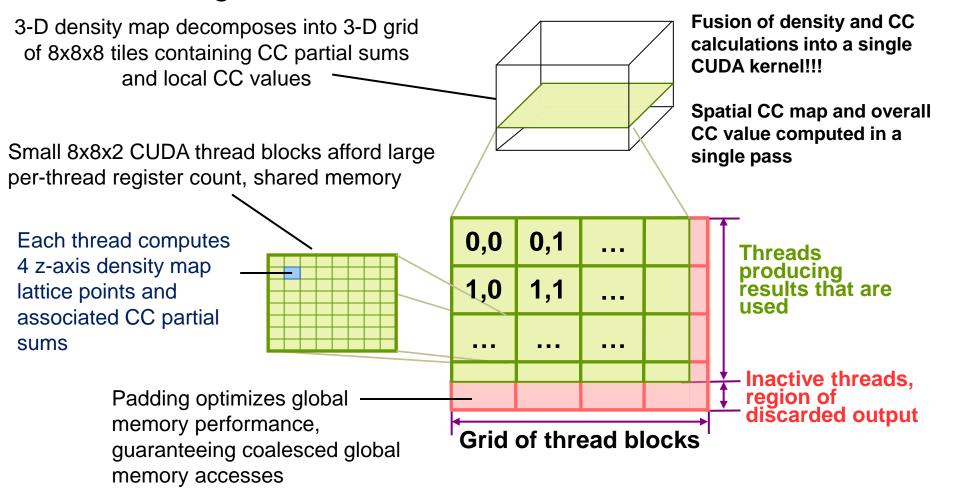
$$\rho(\vec{r}; \vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = \sum_{i=1}^{N} e^{\frac{-|\vec{r} - \vec{r}_i|^2}{2\alpha^2}}$$

 Truncated Gaussian and spatial acceleration grid ensure linear time-complexity



3-D density map lattice point and the neighboring spatial acceleration cells it references

Single-Pass MDFF GPU Cross-Correlation



VMD GPU Cross Correlation Performance

	RHDV	Mm-cpn open	GroEL	Aquaporin
Resolution (Å)	6.5	8	4	3
Atoms	702K	61K	54K	1.6K
VMD-CUDA	0.458s	0.06s	0.034s	0.007s
Quadro K6000	34.6x	25.7x	36.8x	55.7x
VMD-CPU-SSE	0.779s	0.085s	0.159s	0.033s
32-threads, 2x Xeon E5-2687W	20.3x	18.1x	7.9x	11.8x
Chimera	15.86s	1.54s	1.25s	0.39s
1-thread Xeon E5-2687W	1.0x	1.0x	1.0x	1.0x

GPU-Accelerated Analysis and Visualization of Large Structures Solved by Molecular Dynamics Flexible Fitting. J. E. Stone, R. McGreevy, B. Isralewitz, and K. Schulten. Faraday Discussions 169:265-283, 2014.

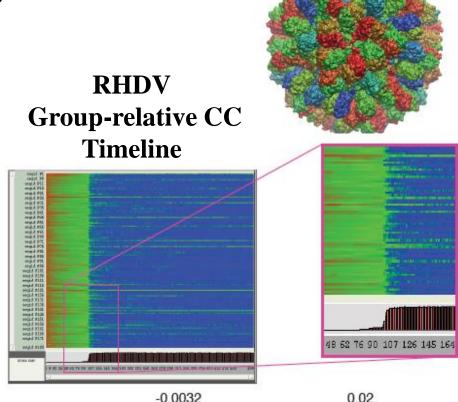




VMD RHDV Cross Correlation Timeline on Cray XK7

	RHDV
Atoms	702K
Traj. Frames	10,000
Component Selections	720
Single-node XK7 (projected)	336 hours (14 days)
128-node XK7	3.2 hours 105x speedup
2048-node XK7	19.5 minutes 1035x speedup

Calculation would take **5 years** using original serial CC calculation on a workstation!







Visualization Goals, Challenges

- Increased GPU acceleration for visualization of petascale molecular dynamics trajectories
- Overcome GPU memory capacity limits, enable high quality visualization of >100M atom systems
- Use GPU to accelerate not only interactive-rate visualizations, but also photorealistic ray tracing with artifact-free ambient occlusion lighting, etc.
- Maintain ease-of-use, intimate link to VMD analytical features, atom selection language, etc.





VMD "QuickSurf" Representation, Ray Tracing



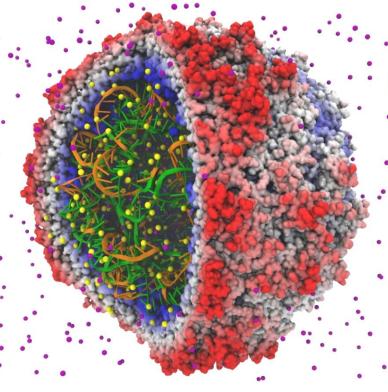
All-atom HIV capsid simulations w/ up to 64M atoms on Blue Waters

VMD "QuickSurf" Representation

- Displays continuum of structural detail:
 - All-atom, coarse-grained, cellular models
 - Smoothly variable detail controls
- Linear-time algorithm, scales to millions of particles, as limited by memory capacity
- Uses multi-core CPUs and GPU acceleration to enable smooth interactive animation of molecular dynamics trajectories w/ up to ~1-2 million atoms
- GPU acceleration yields 10x-15x speedup vs. multi-core CPUs

Fast Visualization of Gaussian Density Surfaces for Molecular Dynamics and Particle System Trajectories.

M. Krone, J. E. Stone, T. Ertl, K. Schulten. *EuroVis Short Papers*, pp. 67-71, 2012



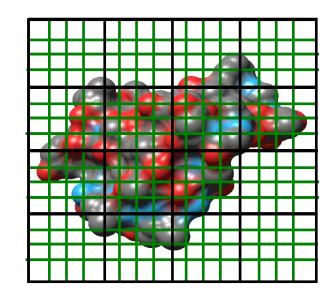
Satellite Tobacco Mosaic Virus

VMD 1.9.2 QuickSurf Algorithm Improvements

- 50%-66% memory use, 1.5x-2x speedup
- Build spatial acceleration data structures, optimize data for GPU
- Compute 3-D density map, 3-D color texture map with data-parallel "gather" algorithm:

$$\rho(\vec{r}; \vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = \sum_{i=1}^{N} e^{\frac{-|\vec{r} - \vec{r}_i|^2}{2\alpha^2}}$$

- Normalize, quantize, and compress density, color, surface normal data while in registers, before writing out to GPU global memory
- Extract isosurface, maintaining quantized/compressed data representation
- Centralized GPU memory management among all molecules+representations: enables graceful eviction of surface data for ray tracing, or other GPU-memory-capacity-constrained operations



3-D density map lattice, spatial acceleration grid, and extracted surface

VMD GPU-Accelerated Ray Tracing Engine

- Complementary to VMD OpenGL GLSL renderer that uses fast, low-cost, interactivity-oriented rendering techniques
- Key ray tracing benefits:
 - Ambient occlusion lighting and hard shadows
 - High quality transparent surfaces
 - Depth of field focal blur and similar optical effects
 - Mirror reflection
 - Single-pass stereoscopic rendering
 - Special cameras: planetarium dome master format

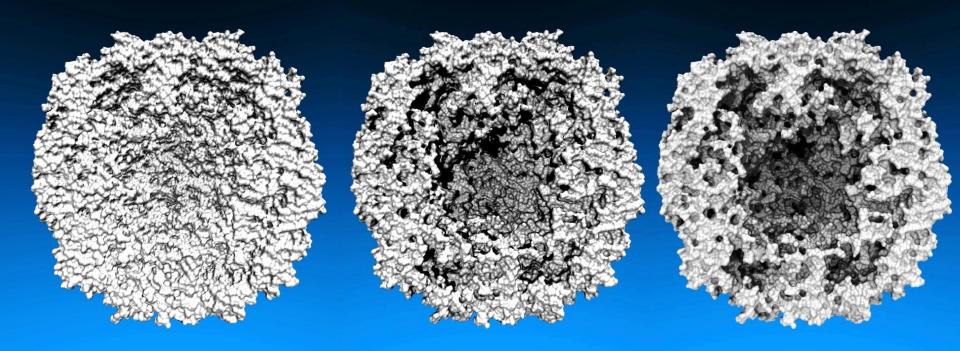




Lighting Comparison, STMV Capsid

Two lights, no shadows

Two lights, hard shadows, <u>1 shadow ray per light</u> Ambient occlusion + two lights, 144 AO rays/hit

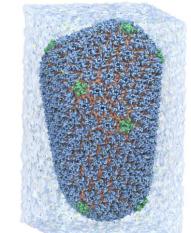


VMD HIV-1 Parallel Movie Rendering 1.9.2 on Blue Waters Cray XE6/XK7

HIV-1 "HD" 1920x1080 movie rendering: GPUs speed up geom+ray tracing by **up to eight times**

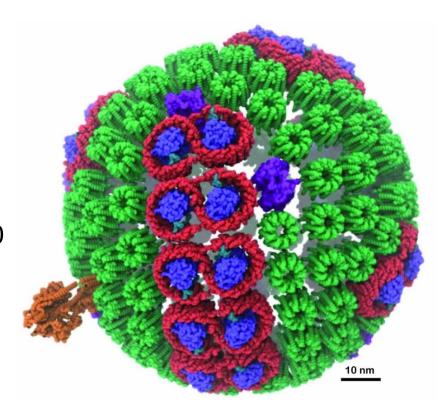


GPU-Accelerated Molecular Visualization on Petascale Supercomputing Platforms, Stone et al. UltraVis'13: Eighth Workshop on Ultrascale Visualization Proceedings, 2013.

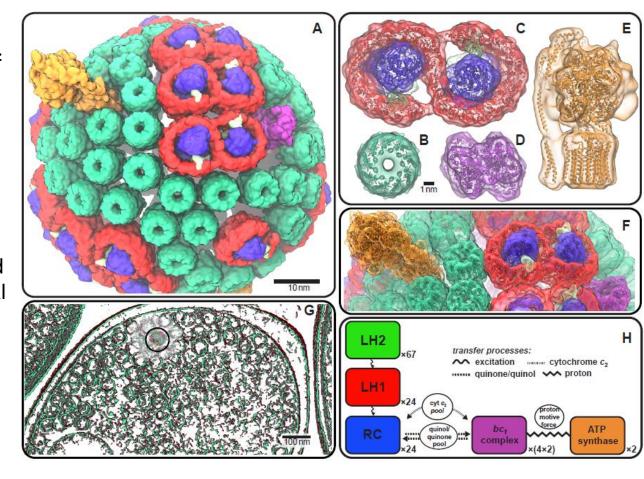


Photosynthetic Chromatophore of Purple Bacteria

- Purple bacteria live in lightstarved conditions at the bottom of ponds, with ~1% sunlight
- Chromatophore system
 - 100M atoms, 700 Å³ volume
 - Contains over 100 proteins, ~3,000 bacteriochlorophylls for collection of photons
 - Energy conversion process synthesizes ATP, which fuels cells...

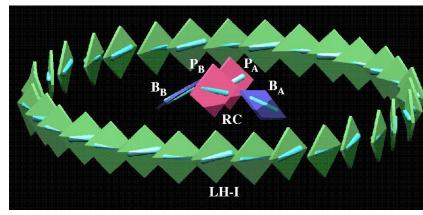


- Movie sums up ~40
 papers and 37 years of
 work by Schulten lab
 and collaborators
- Driving NAMD and VMD software design:
 - Two decades of simulation, analysis, and visualization of individual chromatophore components w/ NAMD+VMD



Role of Visualization

- MD simulation, analysis, visualization provide researchers a so-called "Computational Microscope"
- Visualization is heavily used at every step of structure building, simulation prep and run, analysis, and publication



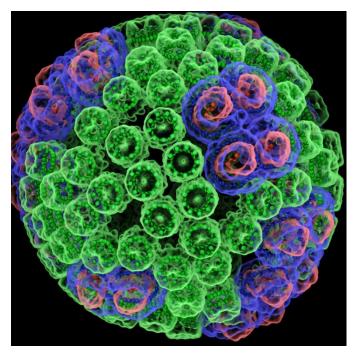
1998 VMD rendering of LH-I SGI Onyx2 InfiniteReality w/ IRIS GL





VMD Chromatophore Rendering on Blue Waters

- New representations, GPU-accelerated molecular surface calculations, memoryefficient algorithms for huge complexes
- VMD GPU-accelerated ray tracing engine w/ OptiX+CUDA+MPI+Pthreads
- Each revision: 7,500 frames render on ~96 Cray XK7 nodes in 290 node-hours, 45GB of images prior to editing



GPU-Accelerated Molecular Visualization on Petascale Supercomputing Platforms.

J. E. Stone, K. L. Vandivort, and K. Schulten. UltraVis'13, 2013.

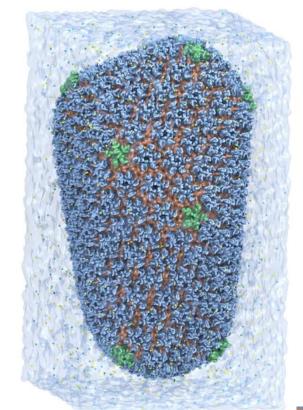
Visualization of Energy Conversion Processes in a Light Harvesting Organelle at Atomic Detail.

M. Sener, et al. SC'14 Visualization and Data Analytics Showcase, 2014.

***Winner of the SC'14 Visualization and Data Analytics Showcase

VMD 1.9.2 Interactive GPU Ray Tracing

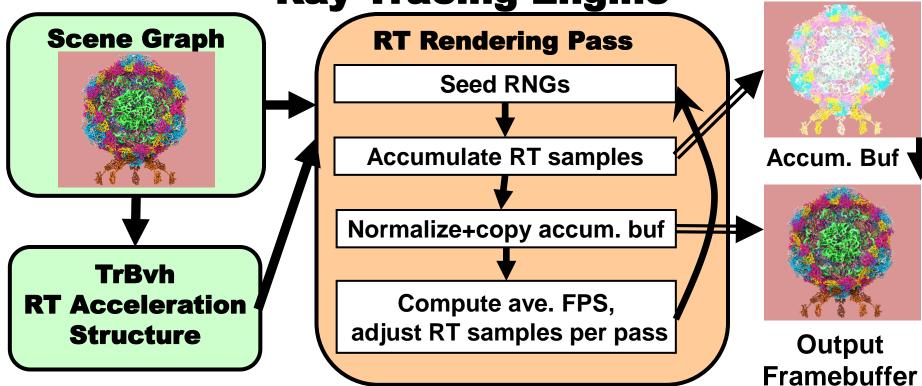
- Ray tracing heavily used for VMD publication-quality images/movies
- High quality lighting, shadows, transparency, depth-of-field focal blur, etc.
- VMD now provides interactive
 ray tracing on laptops, desktops,
 and remote visual supercomputers







VMD TachyonL-OptiX Interactive Ray Tracing Engine

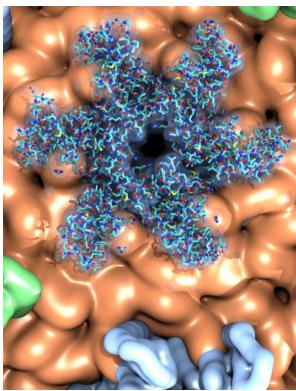






VMD-Next: Coming Soon

- Further integration of interactive ray tracing into VMD
 - Seamless interactive RT in main VMD display window
 - Support trajectory playback in interactive RT
 - o Enable multi-node interactive RT on HPC systems
- Improved movie making tools, off-screen OpenGL movie rendering, parallel movie rendering:
 - EGL for parallel graphics w/o X11 server
 - Built-in (basic) interactive remote visualization on HPC clusters and supercomputers
- Improved structure building tools
- Many new and updated user-contributed plugins:



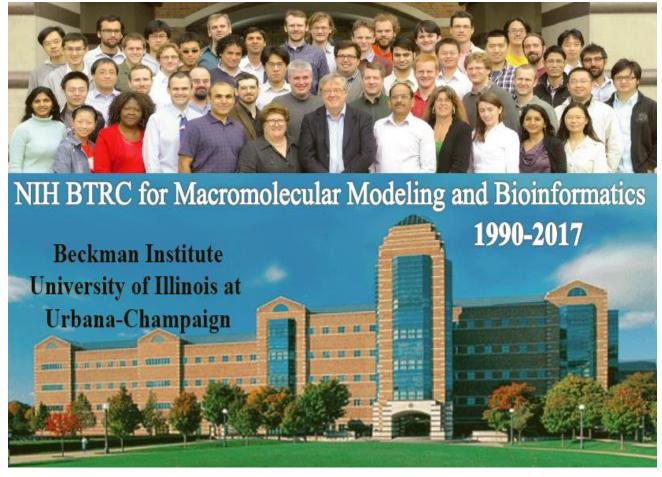
GPU Ray Tracing of HIV-1 Capsid Detail

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